



NA-MIC

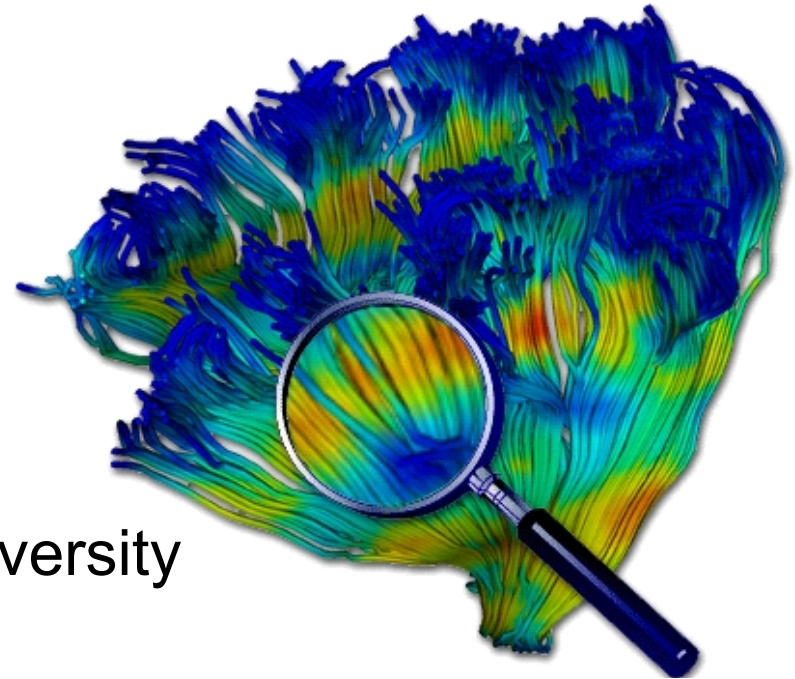
National Alliance for Medical Image Computing

<http://na-mic.org>

Diffusion Tensor Processing and Visualization

Guido Gerig, Ph.D.
University of Utah

Slides presented by
Sonia Pujol, Ph.D., Harvard University

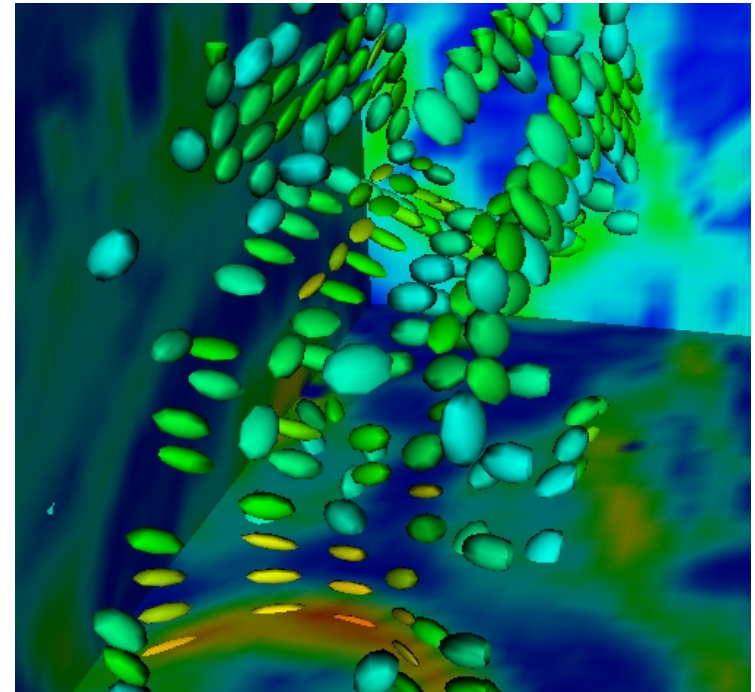




Acknowledgments

Contributors:

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- C. Goodlett
- J. Fallon



National Alliance for Medical Image Computing
(NIH U54EB005149)



Brain Anatomy

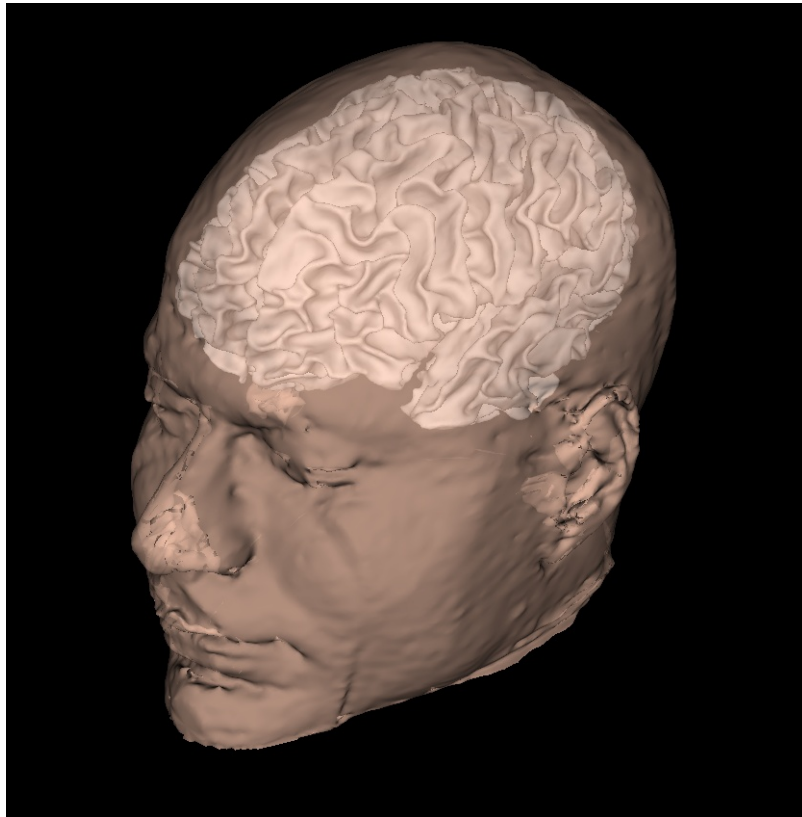


- 100 billions of neurons
- Complex neuronal networks

DT-MRI Tractography. S.Pujol.
Harvard-MIT Health Sciences and Technology HST.583



Brain Anatomy



- 100 billions of neurons
- Complex neuronal networks
- White matter ~45% of the brain

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Brain Anatomy



- 100 billions of neurons
- Complex neuronal networks
- White matter ~45% of the brain
- Myelinated nerve fibers (~ 10 μm axon diameter)

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White Matter Exploration

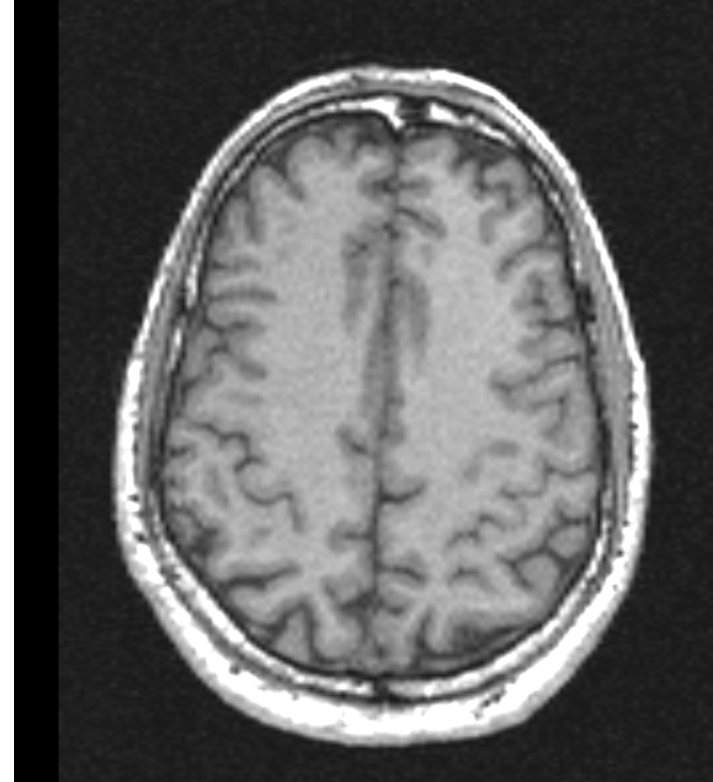
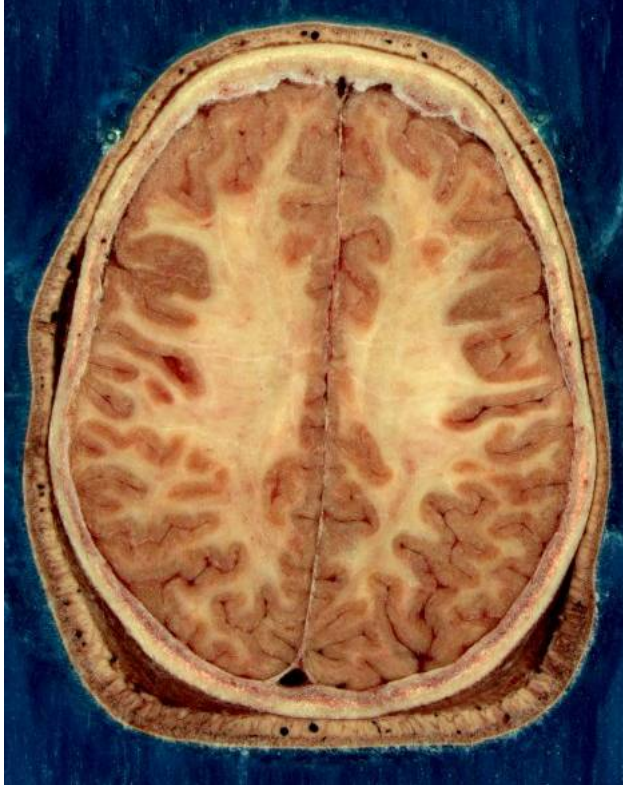


Jules Joseph Dejerine (*Anatomie des centres nerveux* (Paris, 1890-1901): Atlas of Neuroanatomy based on myelin stained preparation

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MRI of White Matter

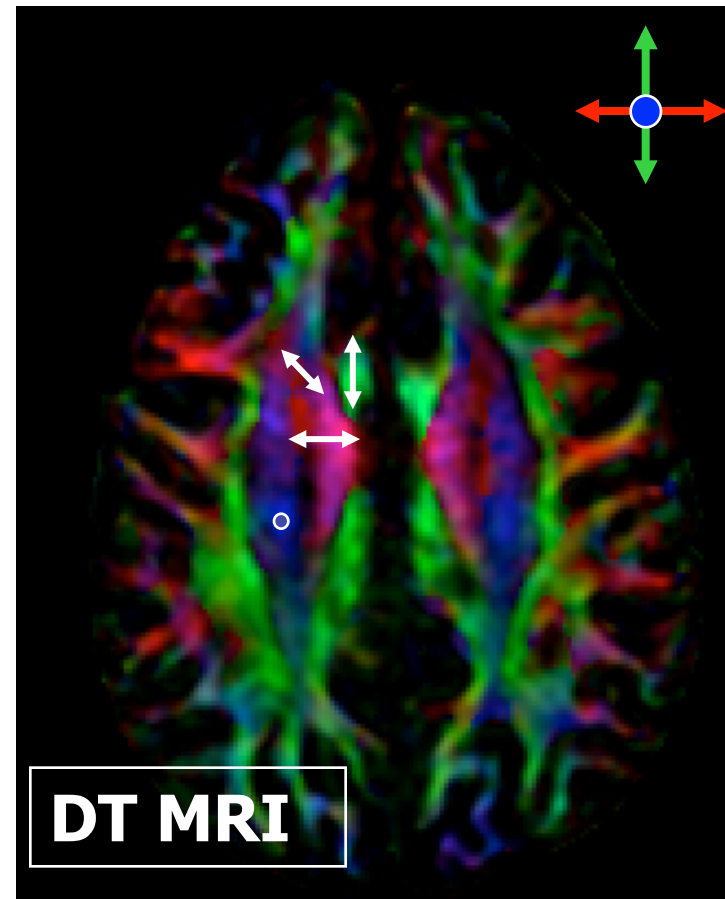
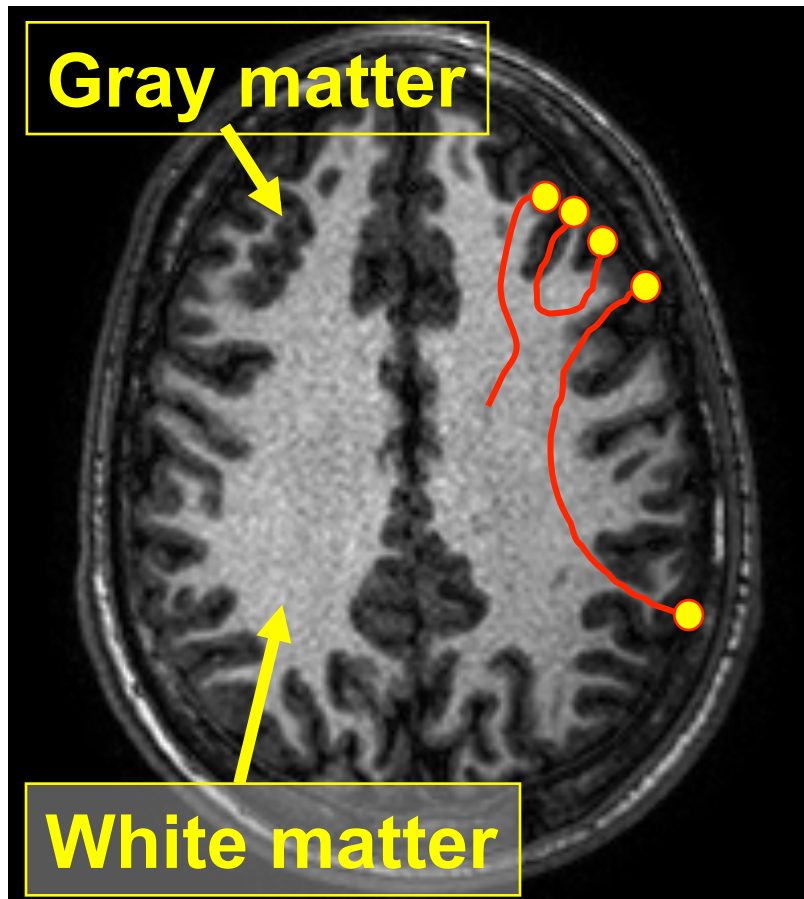


White matter tracts appear homogeneous on T1, T2 or Flair images

DT-MRI Tractography. S.Pujol.
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Diffusion Tensor Imaging (DT MRI) reveals White Matter Structure

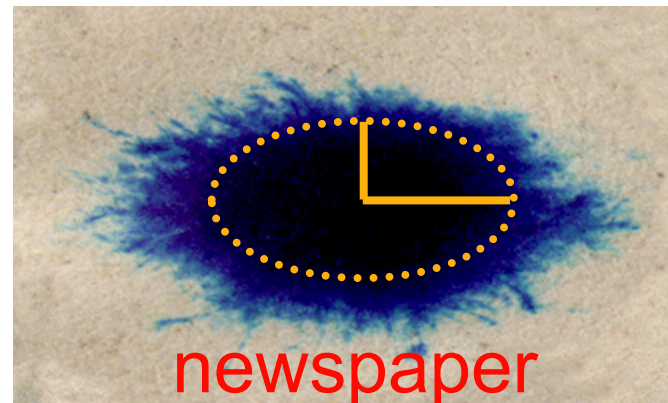
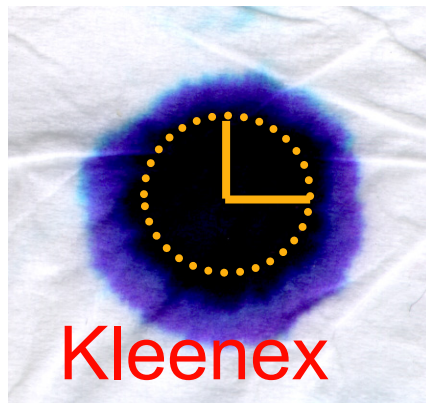


Courtesy of Susumu Mori, JHU



Diffusion in Biological Tissue

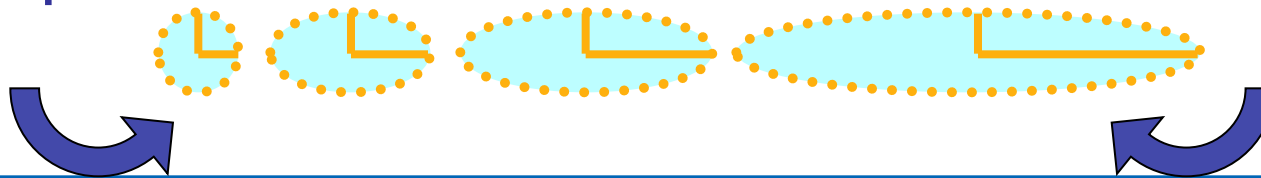
- Motion of water through tissue
- Sometimes faster in some directions than others



- Anisotropy: diffusion rate depends on direction

isotropic

anisotropic

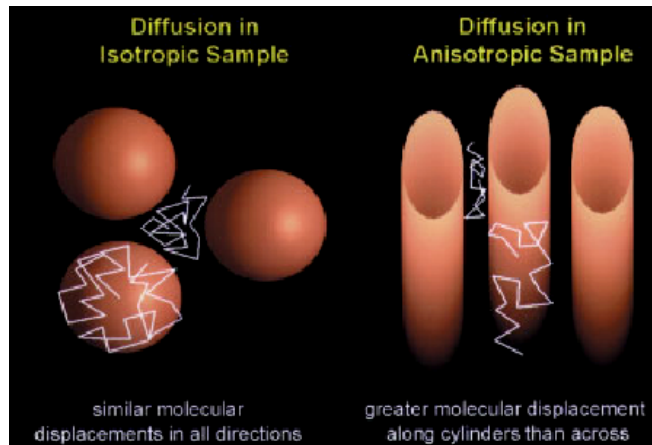


G. Kindlmann



Diffusion in White Matter

- Diffusion of water molecules



From Beaulieu[02]

- Reflects the underlying structure of the tissues
 - Faster diffusion along fibers than perpendicular to them
 - Water diffusion anisotropy used to track fibers, estimate white matter integrity
- Tensor model [Basser]
 - Determine the whole tensor to estimate diffusion anisotropy



The Physics of Diffusion

- Density of substance changes (evolves) over time according to a differential equation (PDE)

$$\frac{\partial \mu}{\partial t} = \nabla \cdot D \nabla \mu$$

Change in
density

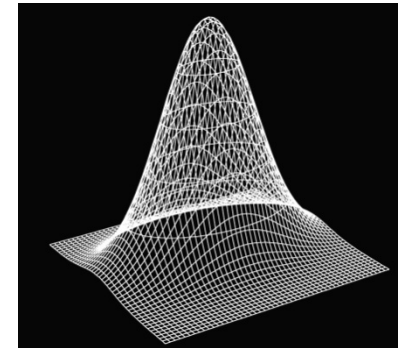
Diffusion – matrix,
tensor
(2x2 or 3x3)

Derivatives
(gradients) in
space



Solutions of the Diffusion Equation

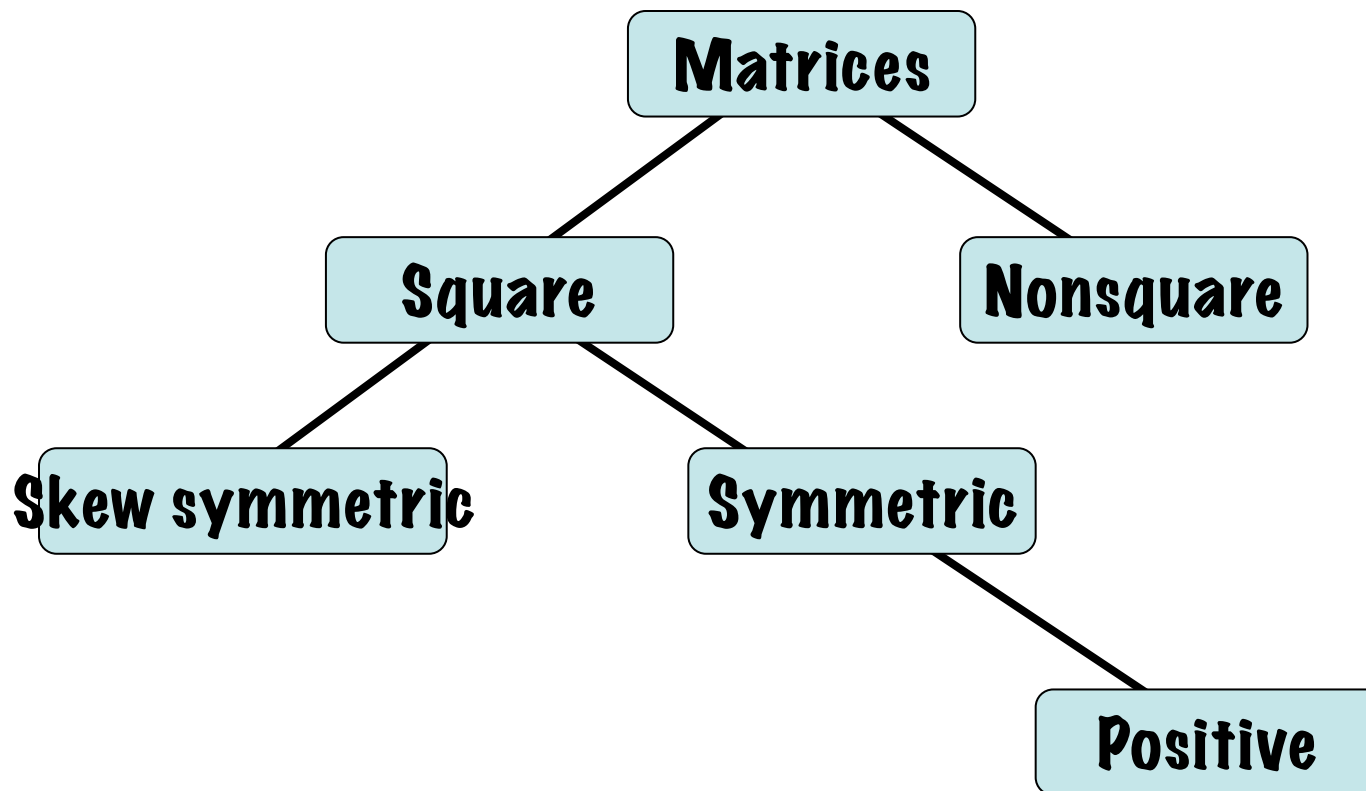
- Simple assumptions
 - Small dot of a substance (point)
 - D constant everywhere in space
- Solution is a multivariate Gaussian
 - Normal distribution
 - “ D ” plays the role of the covariance matrix
- This relationship is not a coincidence
 - Probabilistic models of diffusion (random walk)





D Is A Special Kind of Matrix

- The universe of matrices

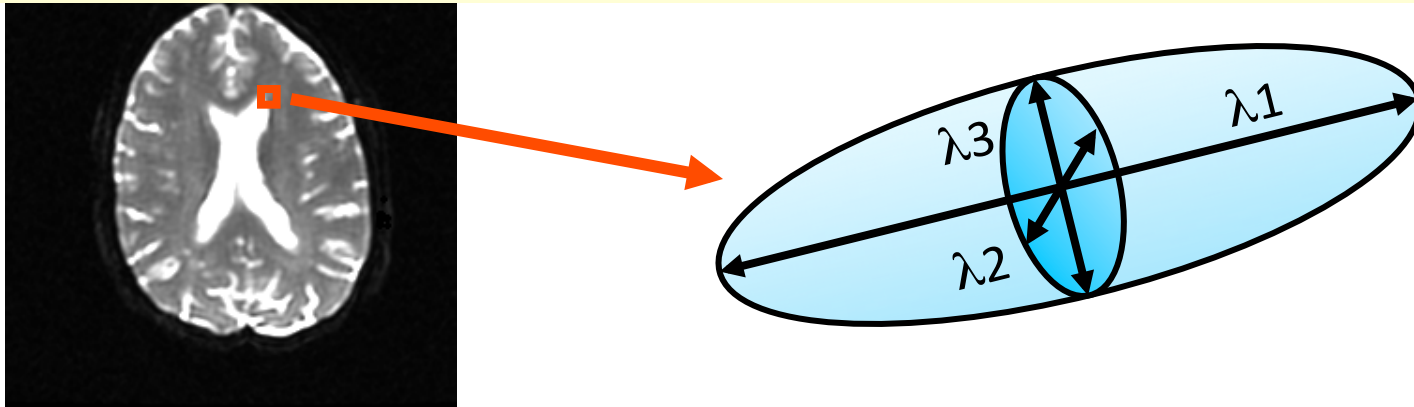


D is a “square, symmetric, positive-definite matrix” (SPD)



Physical Interpretation

The diffusion tensor \underline{D} in the voxel (I,J,K) can be visualized as an ellipsoid, with the eigenvectors indicating the directions of the principal axes, and the square root of the eigenvalues defining the ellipsoidal radii.



DT-MRI Tractography. S.Pujol.
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Properties of SPD

- Bilinear forms and quadratics

$$(x \ y \ z) \begin{pmatrix} D_{11} & D_{12} & D_{13} \\ D_{12} & D_{22} & D_{23} \\ D_{13} & D_{23} & D_{33} \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = k$$

$$(D_{11})x^2 + (2D_{21})xy + (2D_{31})xz + (D_{22})y^2 + (2D_{23})yz + (D_{33})z^2 = k$$

Quadratic equation – implicit equation for ellipse (ellipsoid in 3D)

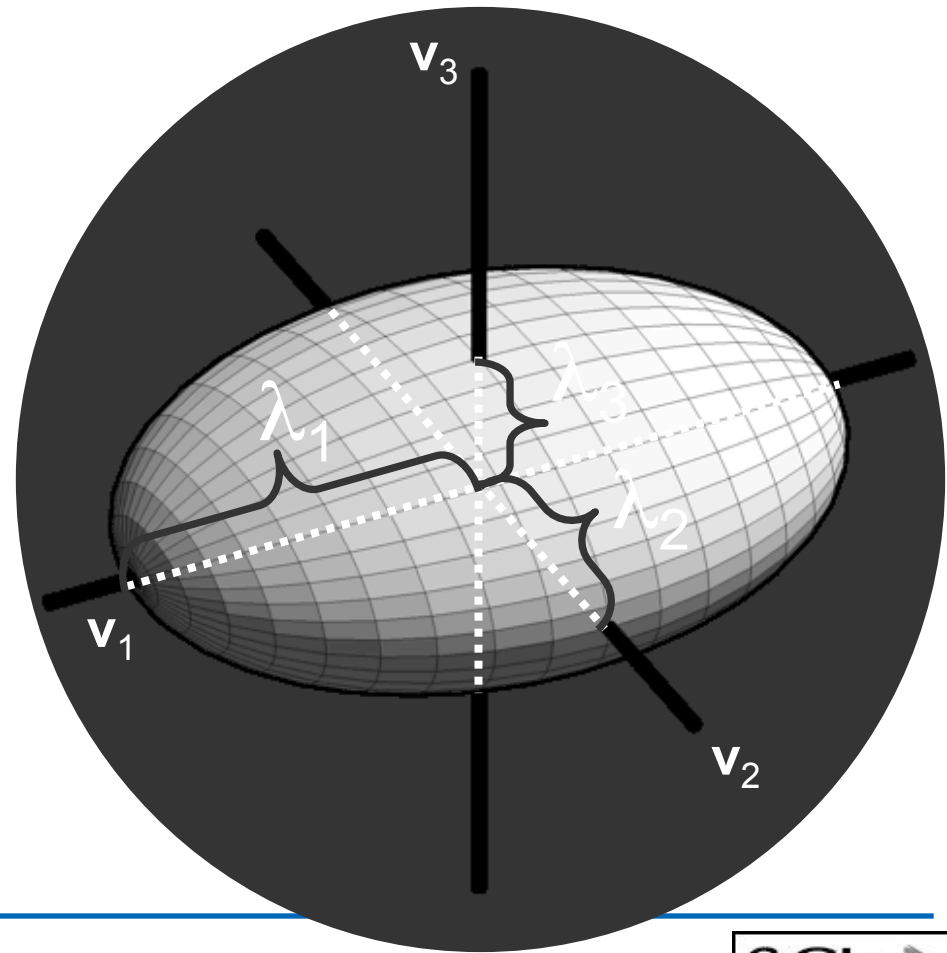
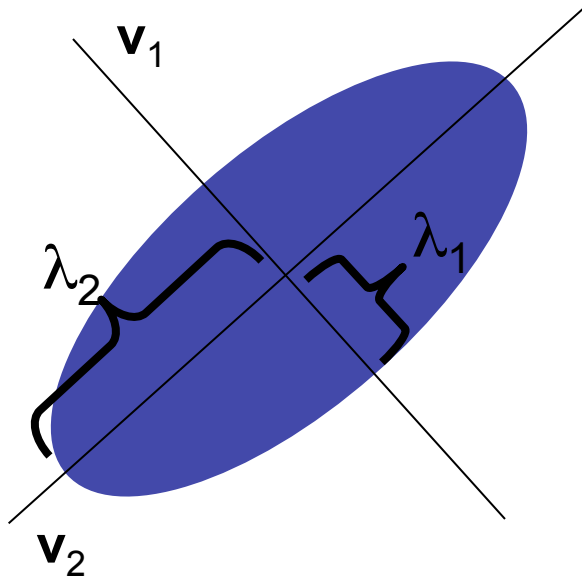
- Eigen Decomposition

$$D = R\Lambda R^{-1} = \begin{bmatrix} | & | & | \\ v_1 & v_2 & v_3 \\ | & | & | \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 & 0 \\ 0 & \lambda_2 & 0 \\ 0 & 0 & \lambda_3 \end{bmatrix} \begin{bmatrix} - & v_1 & - \\ - & v_2 & - \\ - & v_3 & - \end{bmatrix}$$

- Lambda – shape information, independent of orientation
- R – orientation, independent of shape
- Lambda's > 0



Eigen Directions and Values (Principle Directions)





Tensors From Diffusion-Weighted Images

- Big assumption
 - At the scale of DW-MRI measurements
 - Diffusion of water in tissue is approximated by Gaussian
 - Solution to heat equation with constant diffusion tensor
- **Stejskal-Tanner equation**
 - Relationship between the DW images and D

$$S_k = S_0 e^{-bg_k^T D g_k}$$

S_k kth DW Image

S_0 Base image

g_k Gradient direction

Physical constants
Strength of gradient
Duration of gradient pulse
Read-out time



Tensors From Diffusion-Weighted Images

- **Stejskal-Tanner equation**
 - Relationship between the DW images and D

$$S_k = S_0 e^{-b g_k^T D g_k}$$

k^{th} DW Image Base image Gradient direction

Physical constants
Strength of gradient
Duration of gradient pulse
Read-out time



Tensors From Diffusion-Weighted Images

- Solving S-T for D

- Take log of both sides

$$g_k^T D g_k = \frac{\log S_0 - \log S_k}{b}$$

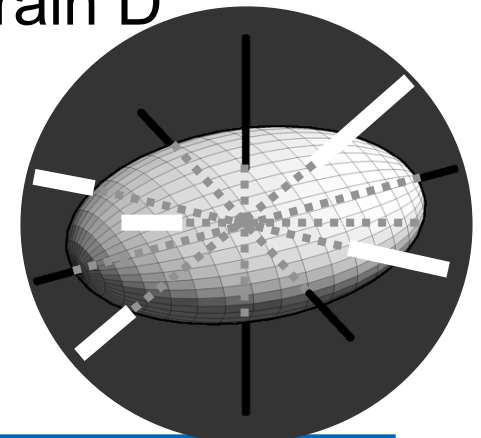
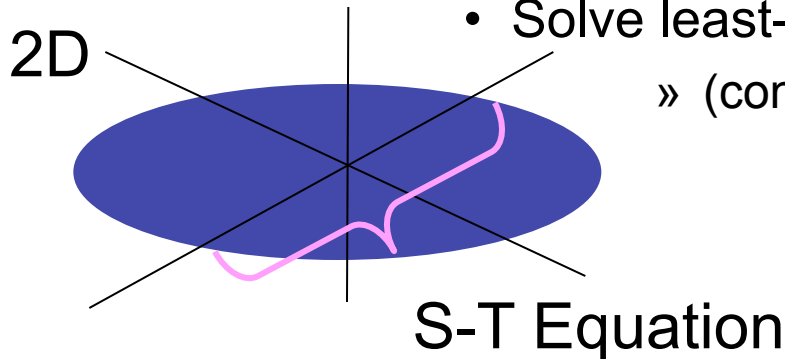
- Linear system for elements of D

- Six gradient directions (3 in 2D) uniquely specify D

- More gradient directions overconstrain D

- Solve least-squares

- » (constrain lambda>0)

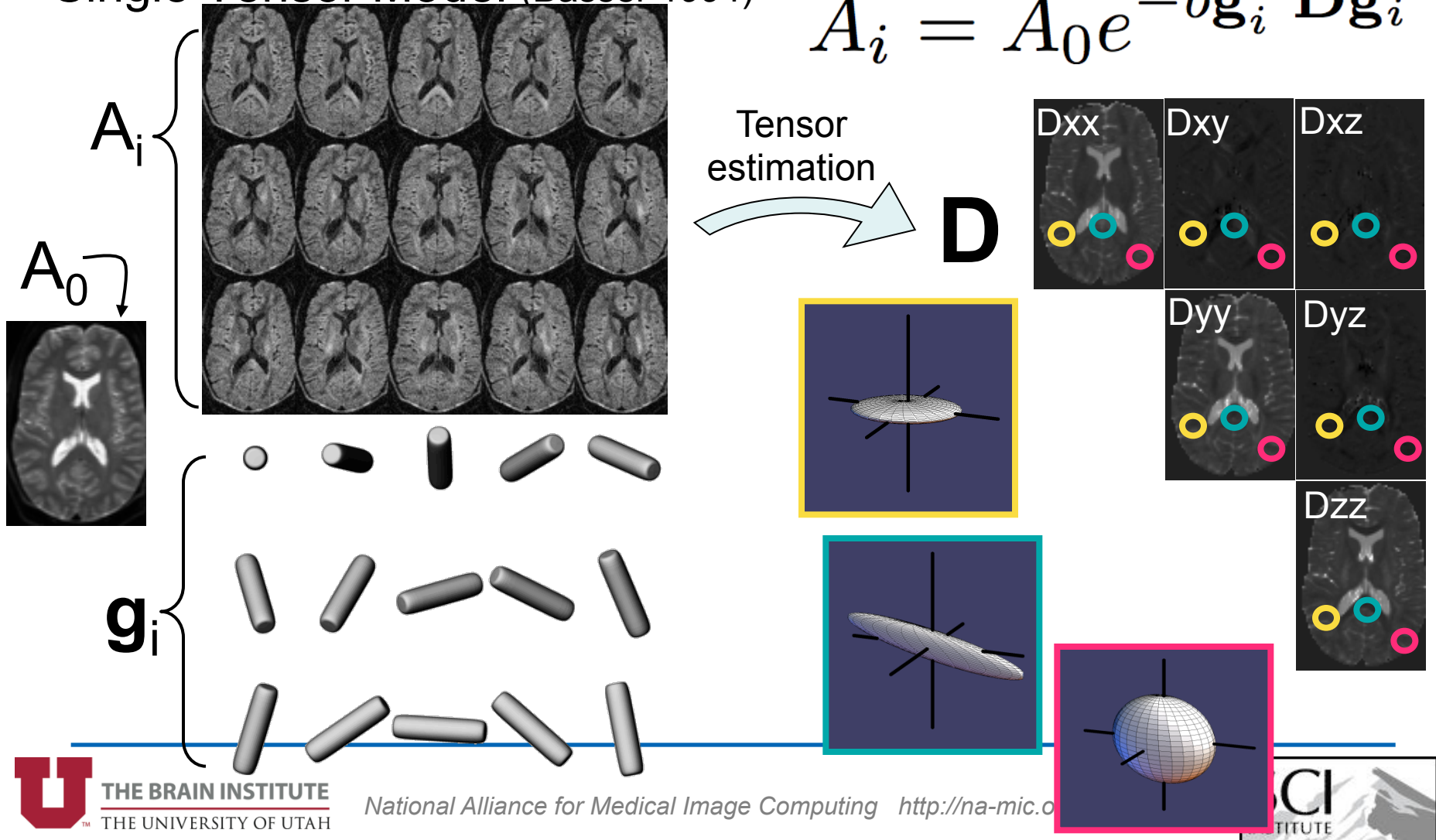




DWI summary: Model

Single Tensor Model (Basser 1994)

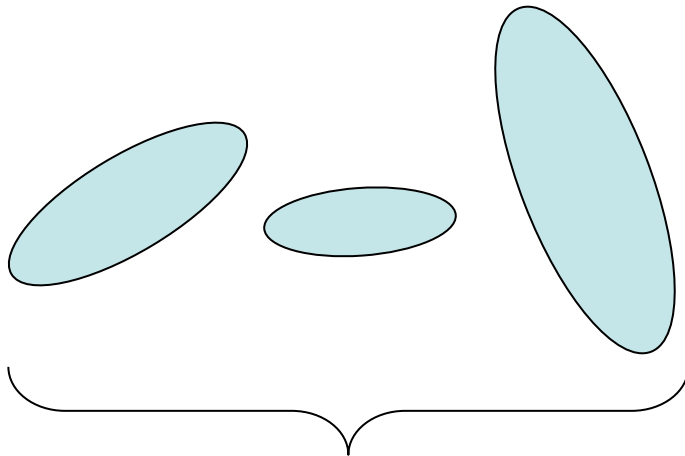
$$A_i = A_0 e^{-b g_i^T D g_i}$$



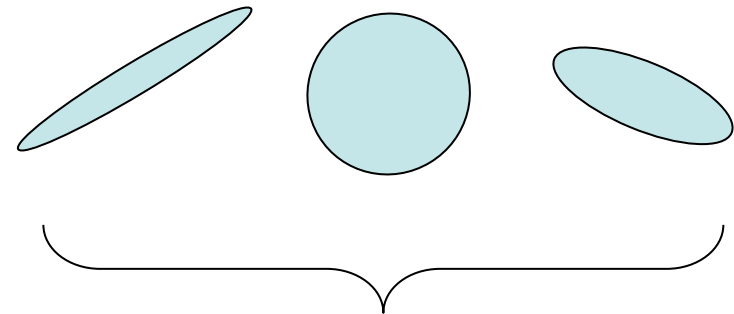


Shape Measures on Tensors

- Represent or visualization shape
- Quantify meaningful aspect of shape
- Shape vs size



Different sizes/orientations



Different shapes



Measuring the “Size” of a Tensor

- Length – $(\lambda_1 + \lambda_2 + \lambda_3)/3$
– $(\lambda_1^2 + \lambda_2^2 + \lambda_3^2)^{1/2}$
- Area – $(\lambda_1 \lambda_2 + \lambda_1 \lambda_3 + \lambda_2 \lambda_3)$
- Volume – $(\lambda_1 \lambda_2 \lambda_3)$

Sometimes used.

Also called:

- “Root sum of squares”
- “Diffusion norm”
- “Frobenius norm”

Generally used.

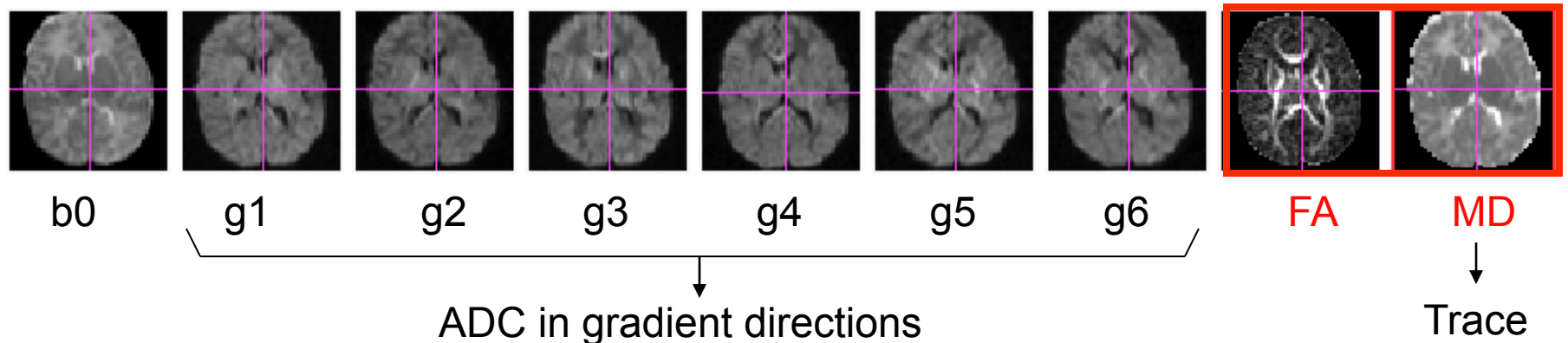
Also called:

- “Mean diffusivity” <MD>
- “Trace”



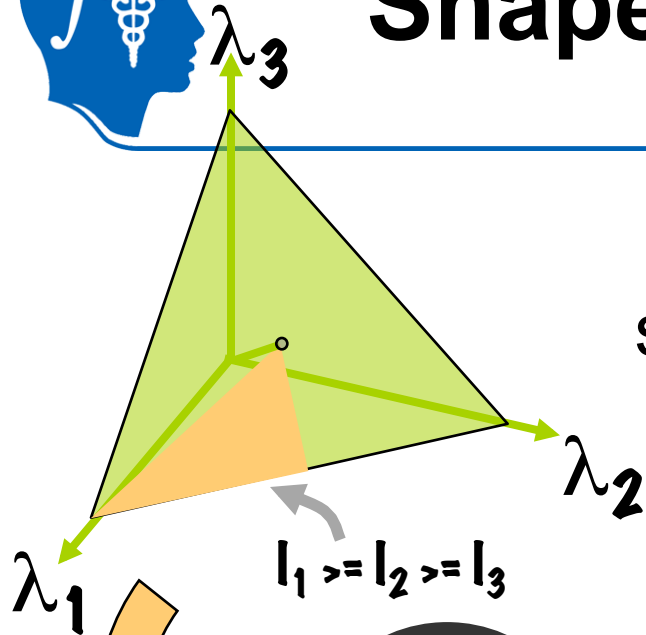
ADC versus Mean Diffusivity

- Apparent diffusion coefficient (ADC) measures diffusivity in a specific direction.
- Mean diffusivity ($\langle MD \rangle$) is the trace of the diffusion tensor.
- Terms often not properly used, papers often cite ADC but actually mean $\langle MD \rangle$

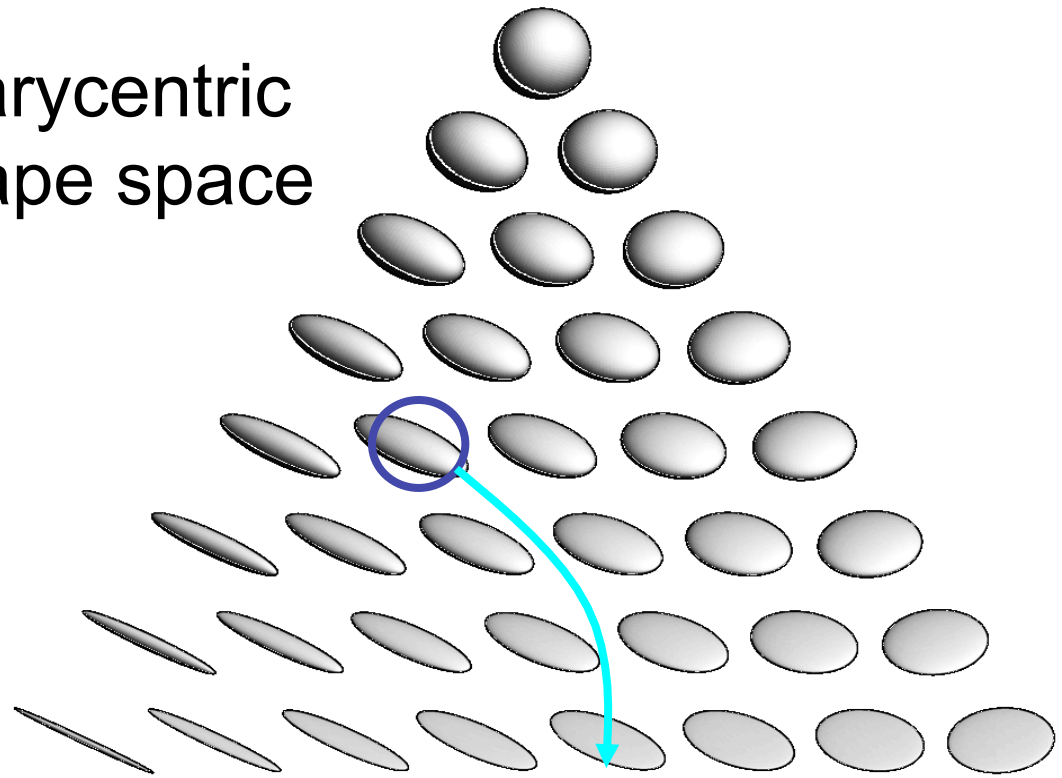




Shape Other Than Size



Barycentric
shape space



(C_S, C_L, C_P)

Westin, 1997

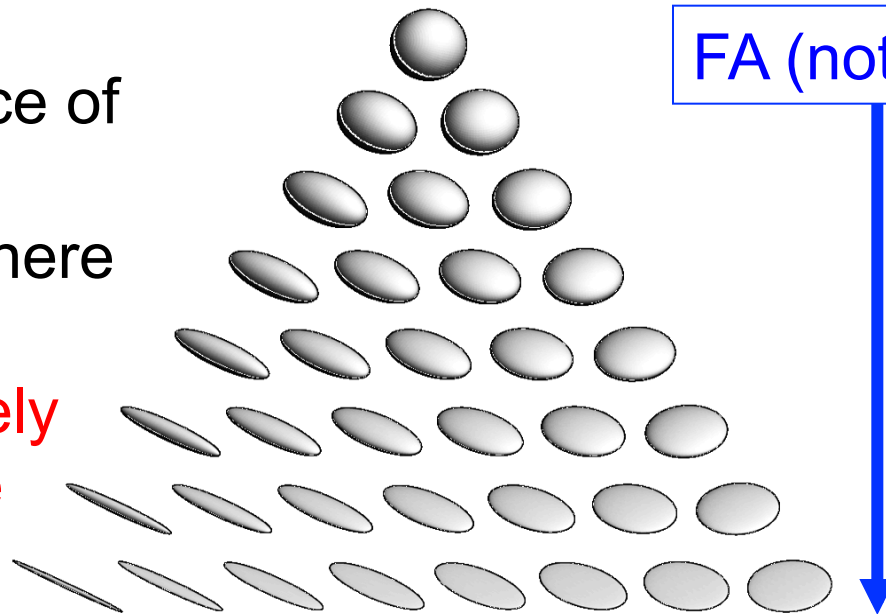


Reducing Shape to One Number Fractional Anisotropy

$$FA = \frac{\sqrt{(\lambda_1 - \lambda_2)^2 + (\lambda_1 - \lambda_3)^2 + (\lambda_2 - \lambda_3)^2}}{\sqrt{2}\sqrt{\lambda_1^2 + \lambda_2^2 + \lambda_3^2}}$$

Properties:

- Normalized variance of eigenvalues
- Difference from sphere
- Invariant to size
- **FA does not uniquely characterize shape**

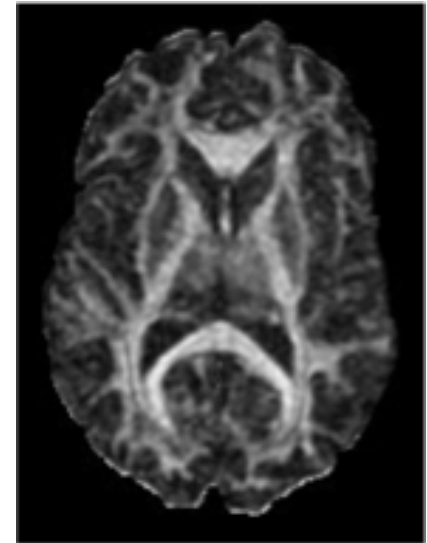


FA (not quite)



FA as an Indicator for White Matter

- Visualization – ignore tissue that is not WM
- Registration – Align WM bundles
- Tractography – terminate tracts as they exit WM
- Analysis
 - Axon density/degeneration
 - Myelin
- Big question
 - What physiological/anatomical property does FA measure?

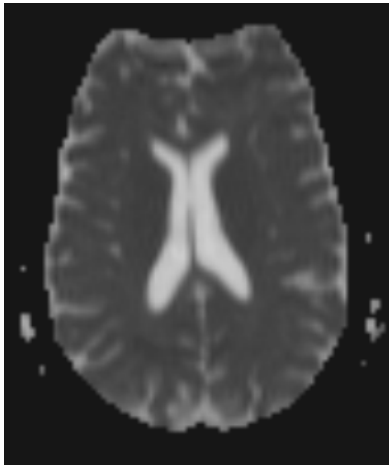




Tensor size (MD) and shape (FA)

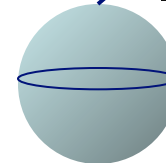
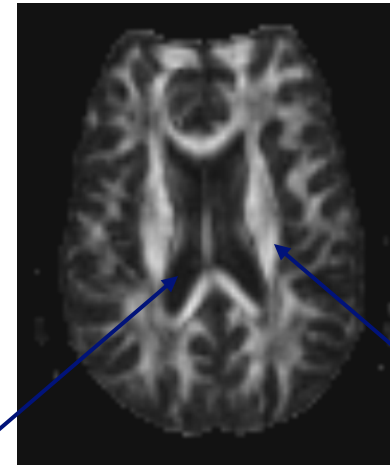
- Mean diffusivity (MD)

$$MD = \frac{\lambda_1 + \lambda_2 + \lambda_3}{3}$$



- Fractional anisotropy (FA)

$$FA = \frac{1}{\sqrt{2}} \frac{\sqrt{(\lambda_1 - \lambda_2)^2 + (\lambda_2 - \lambda_3)^2 + (\lambda_1 - \lambda_3)^2}}{\sqrt{\lambda_1^2 + \lambda_2^2 + \lambda_3^2}}$$



Isotropic
diffusion



Highly
directional
diffusion

White
matter

Cerebrospinal
fluid





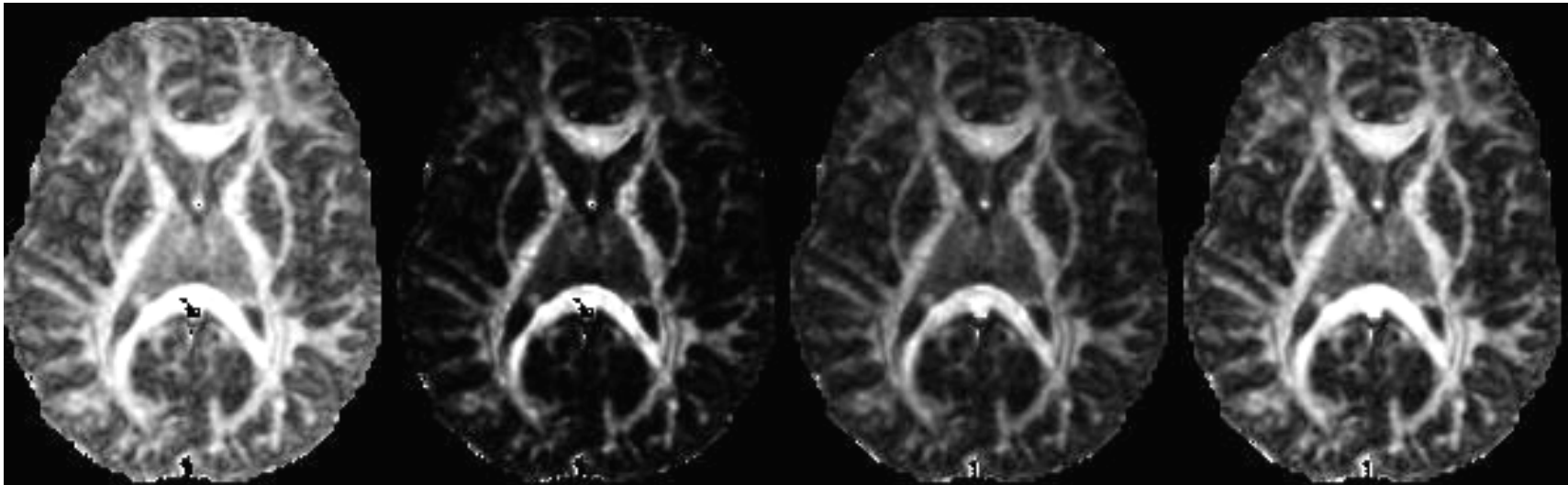
Various Measures of Anisotropy

A_1

VF

RA

FA



A. Alexander



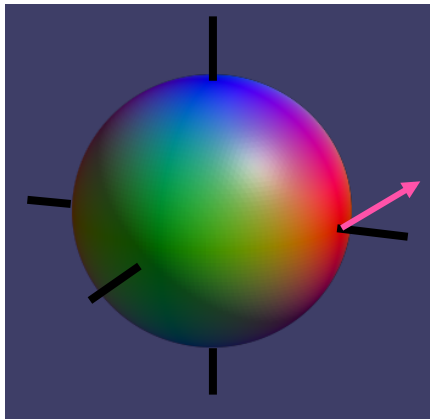
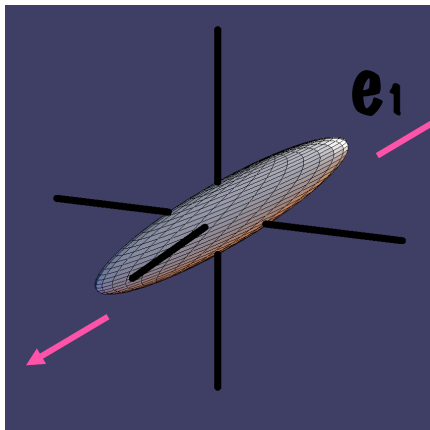
Visualizing Tensors: Direction and Shape

- Color mapping
- Glyphs

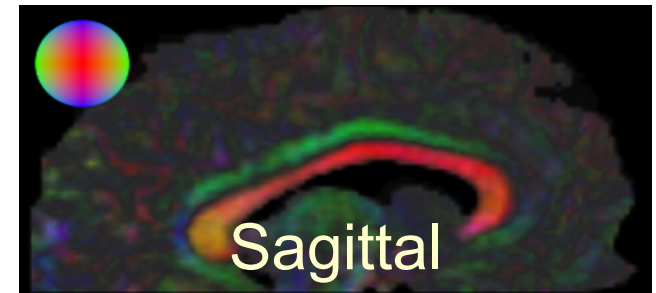
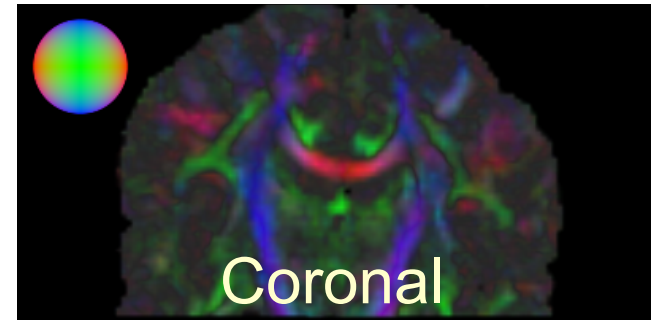
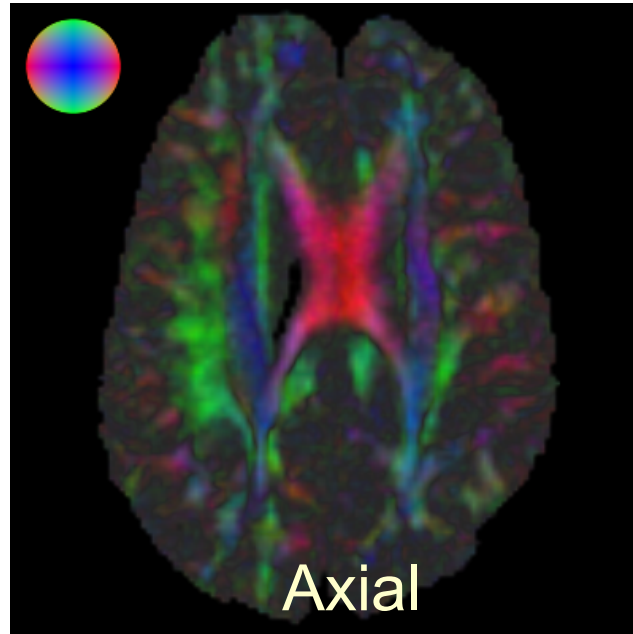




Coloring by Principal Diffusion Direction



- Principal eigenvector, linear anisotropy determine color



$$R = | \mathbf{e}_1 \cdot \mathbf{x} |$$

$$G = | \mathbf{e}_1 \cdot \mathbf{y} |$$

$$B = | \mathbf{e}_1 \cdot \mathbf{z} |$$

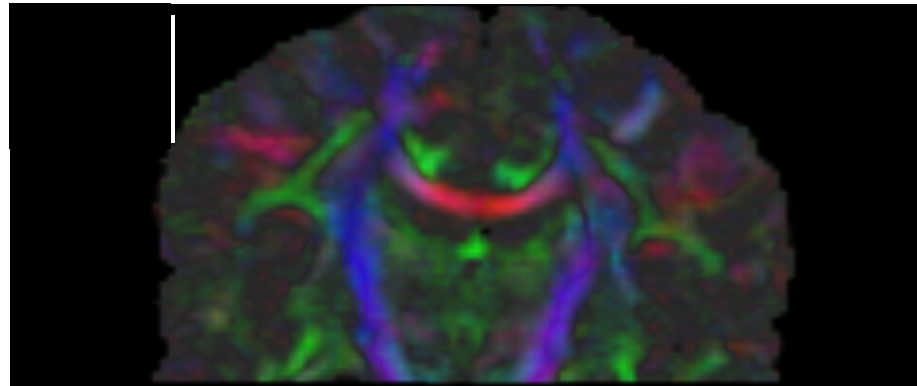
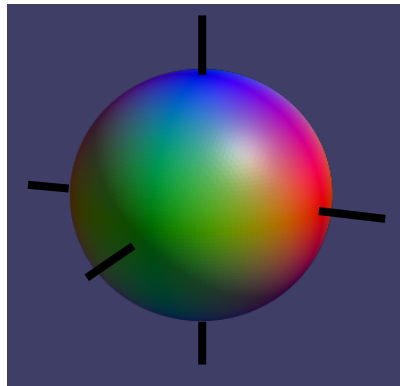
Pierpaoli, 1997

Slide G. Kindlmann



Issues With Coloring by Direction

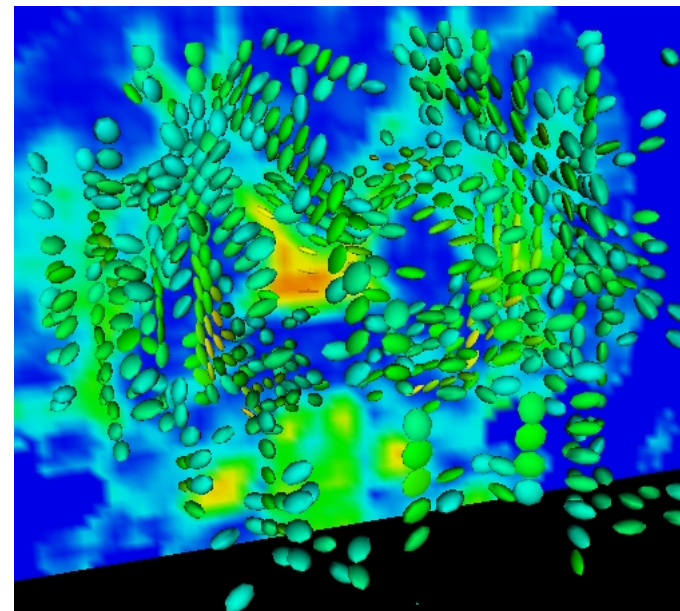
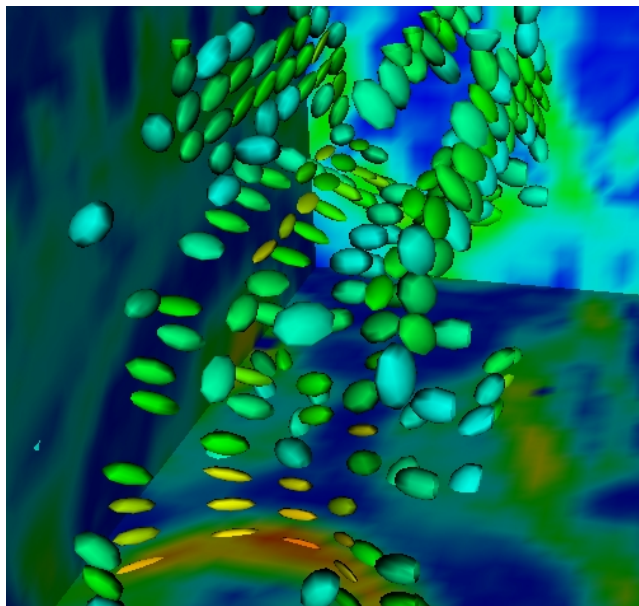
- Set transparency according to FA (highlight-tracts)
- Coordinate system dependent
- Primary colors dominate
 - Perception: saturated colors tend to look more intense
 - Which direction is “cyan”?
 - Coloring is not unique



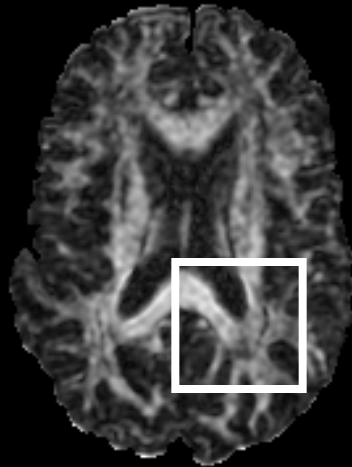


Visualization with Glyphs

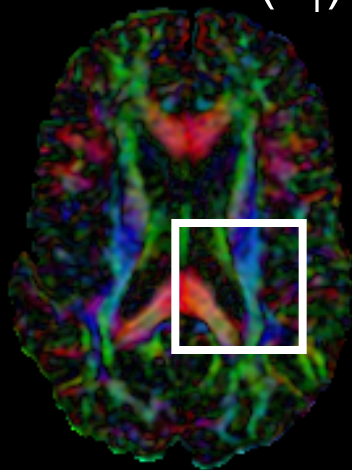
- Density and placement based on FA or detected features
- Place ellipsoids on regular grid



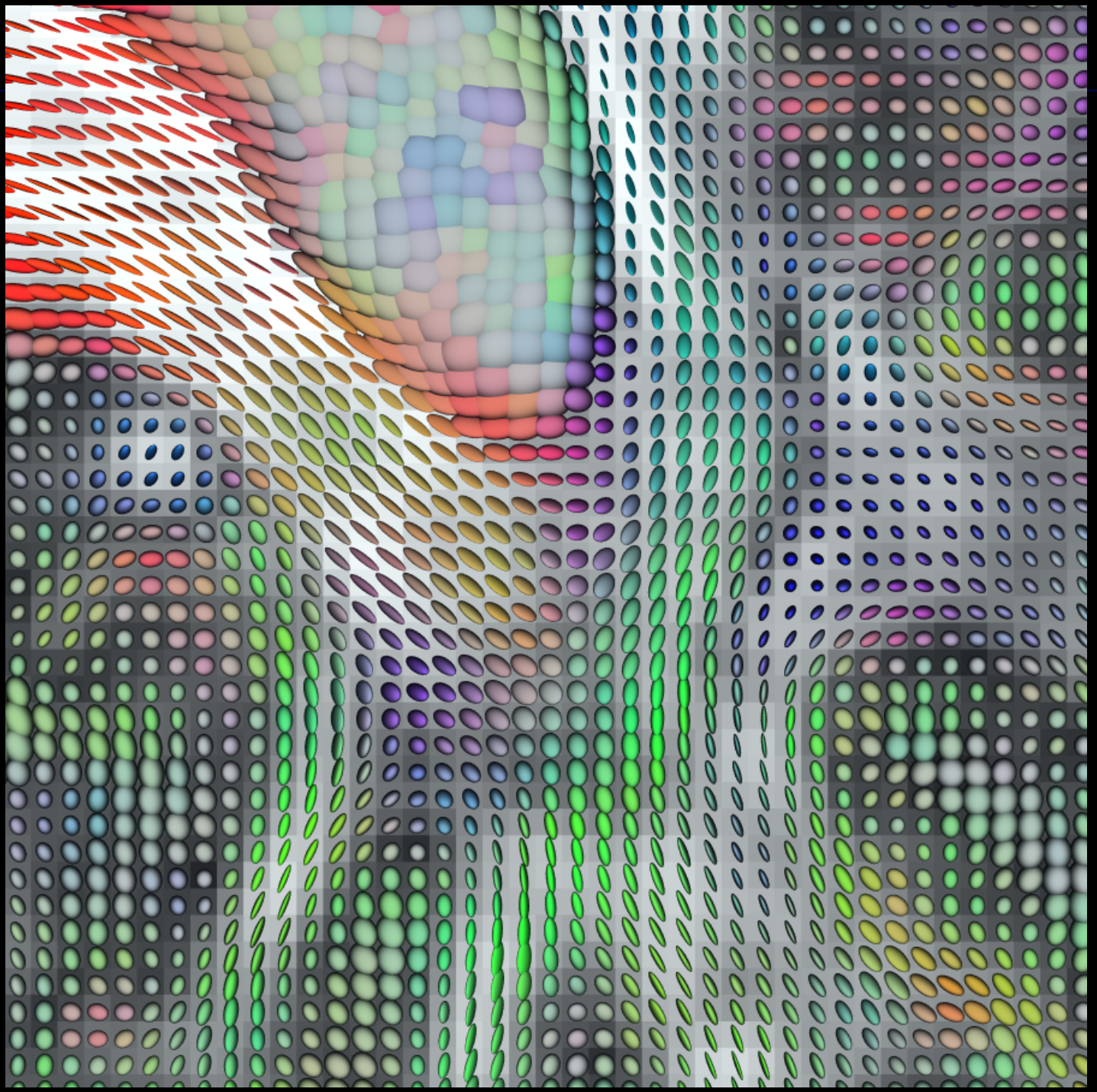
Backdrop: FA



Color: RGB(\mathbf{e}_1)



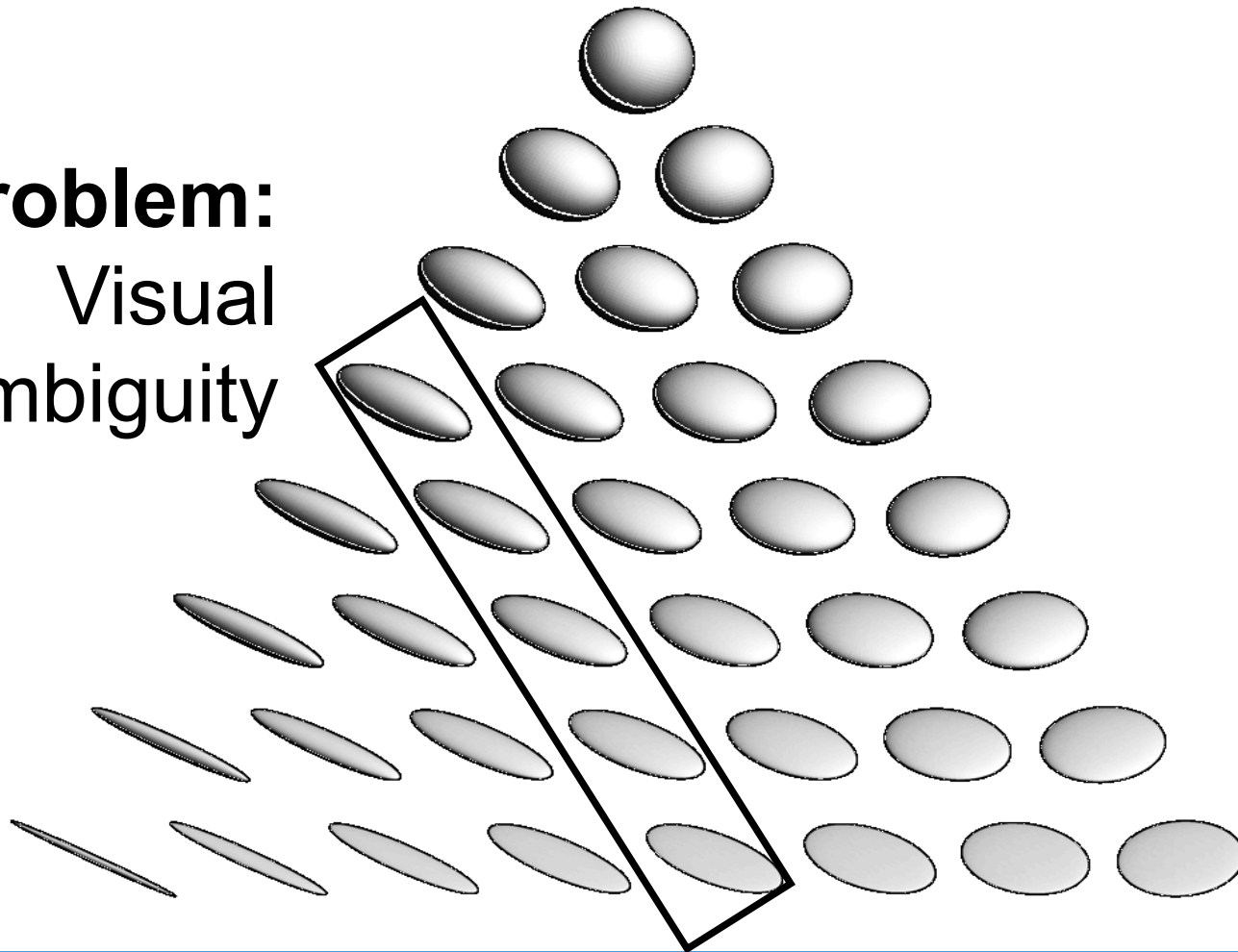
G. Kindlmann





Glyphs: ellipsoids

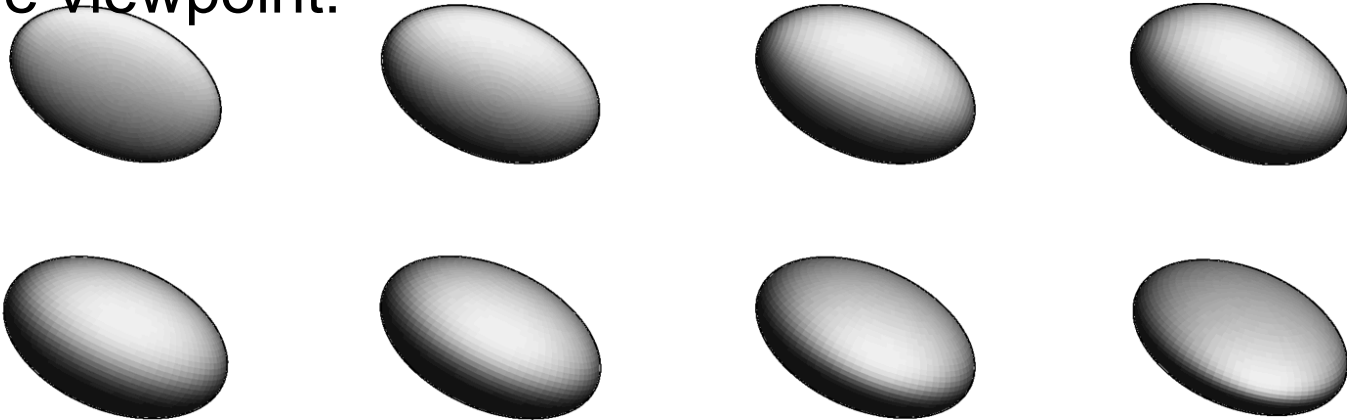
Problem:
Visual
ambiguity



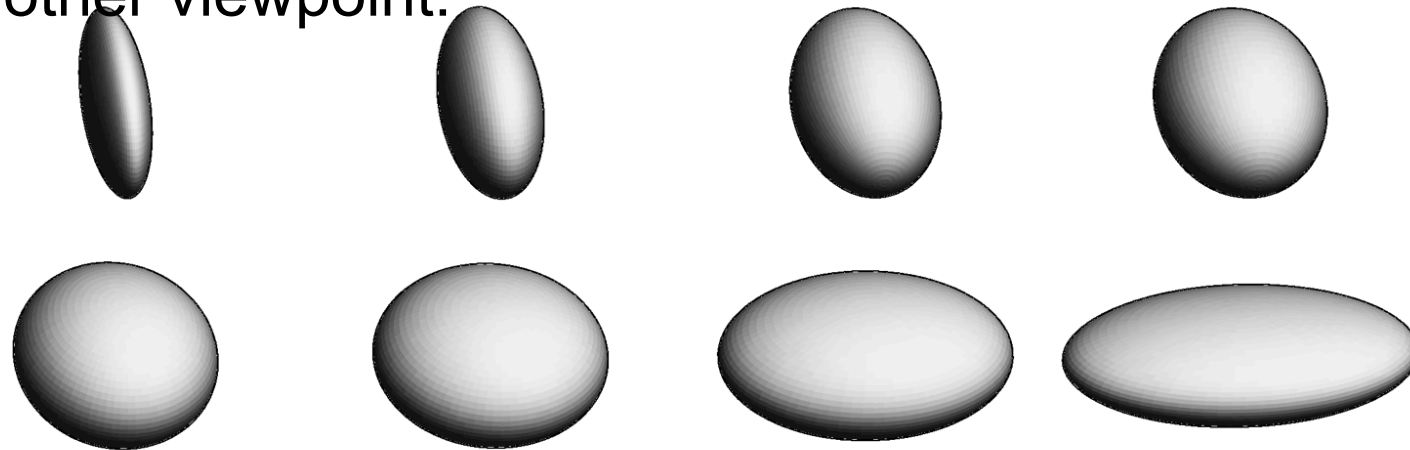


Worst case scenario: ellipsoids

one viewpoint:



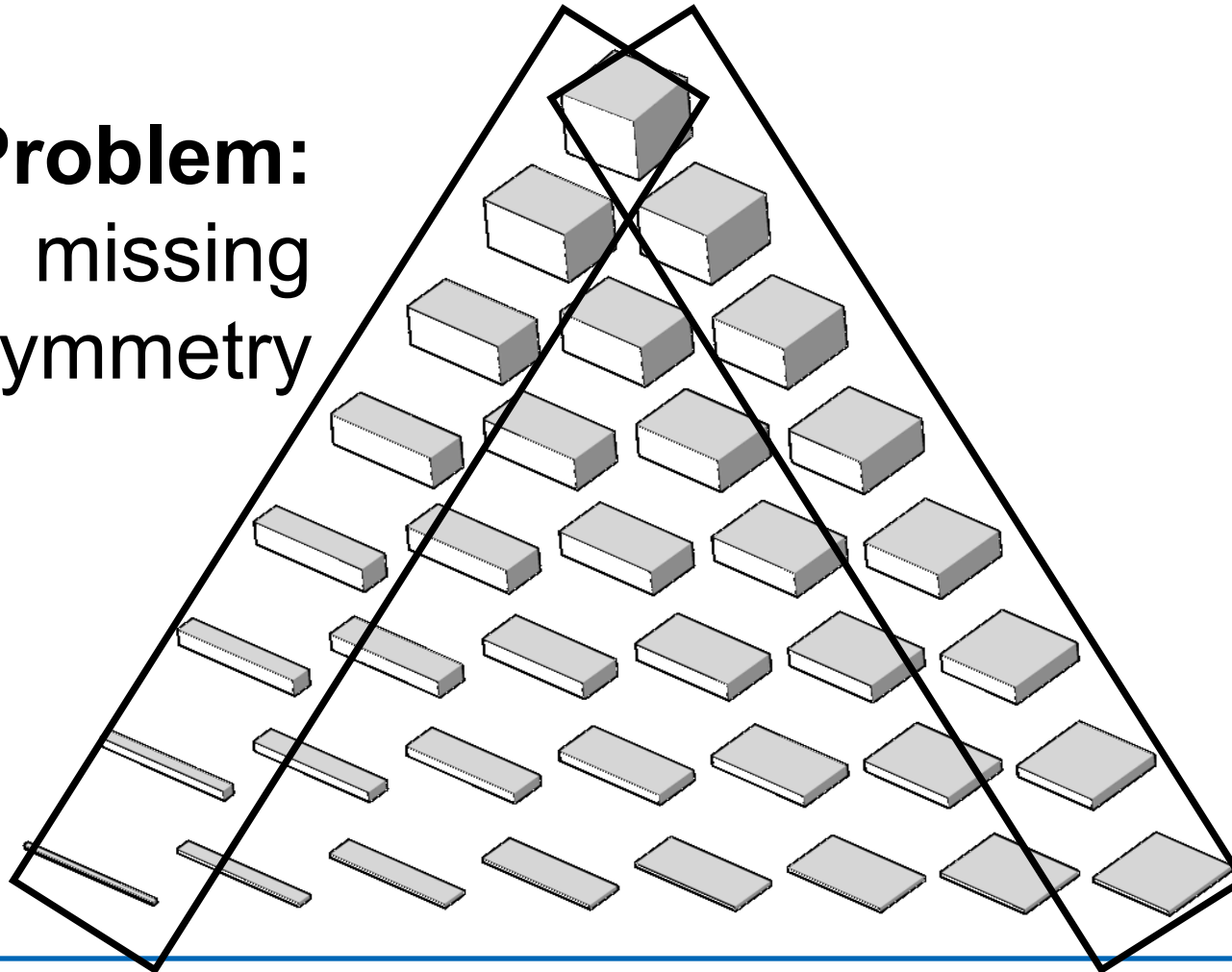
another viewpoint:





Glyphs: cuboids

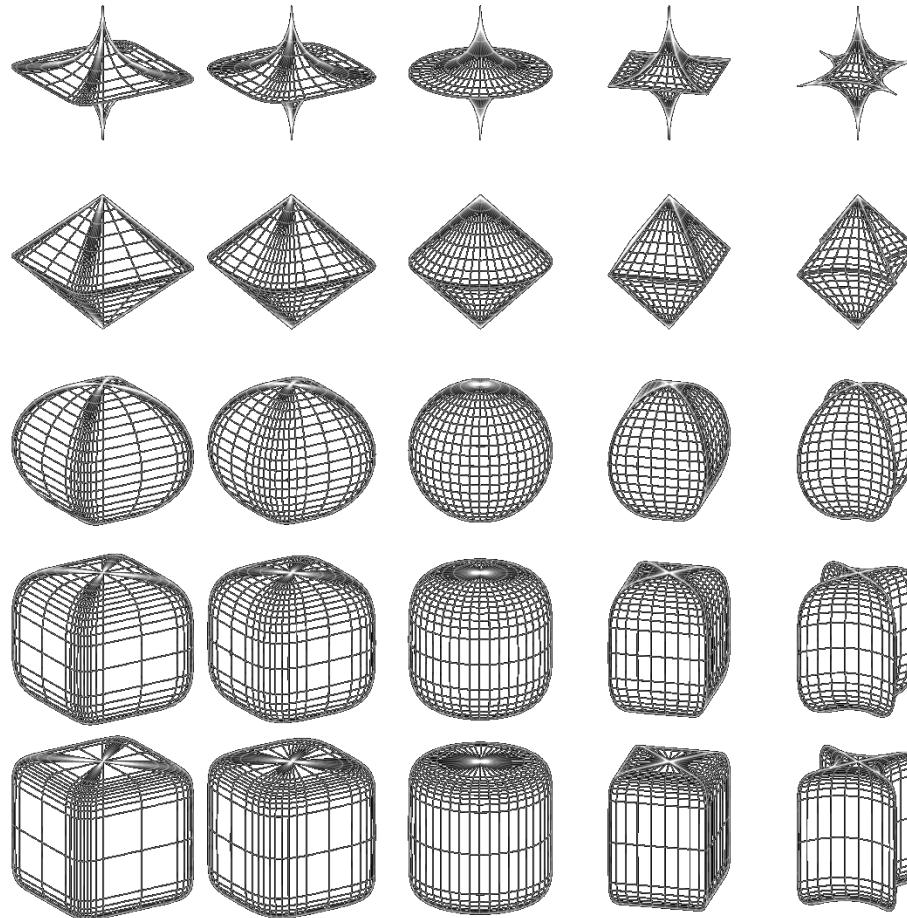
Problem:
missing
symmetry





Superquadrics

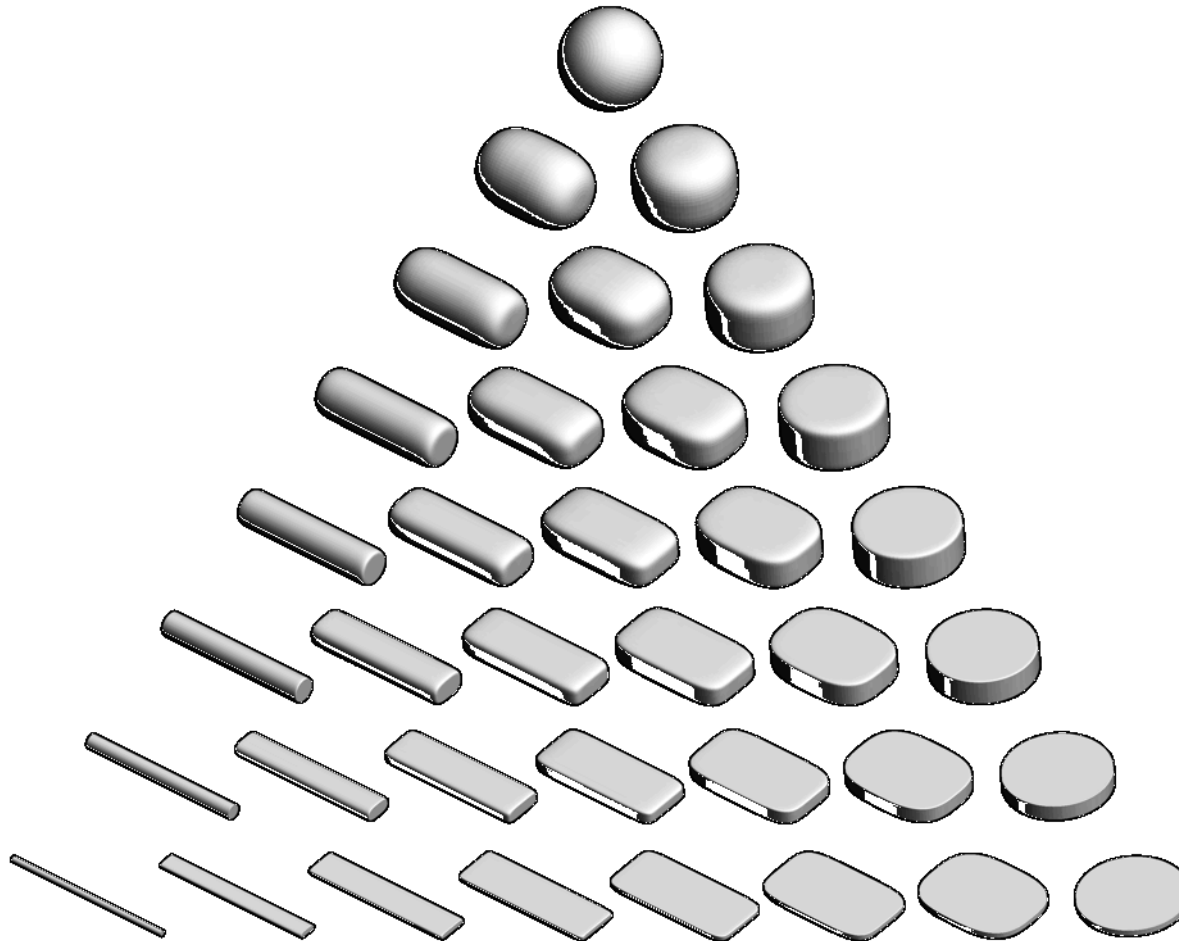
Barr 1981





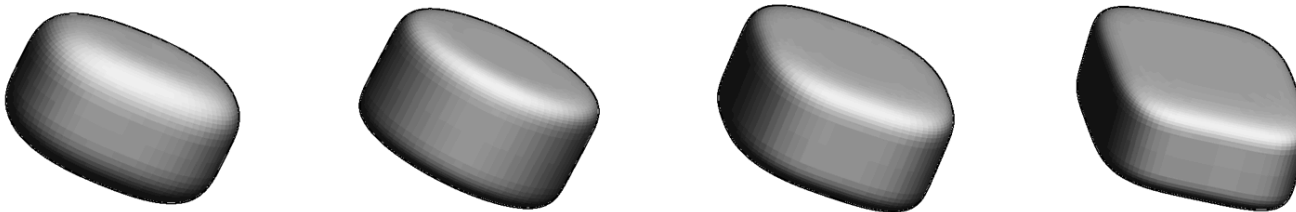
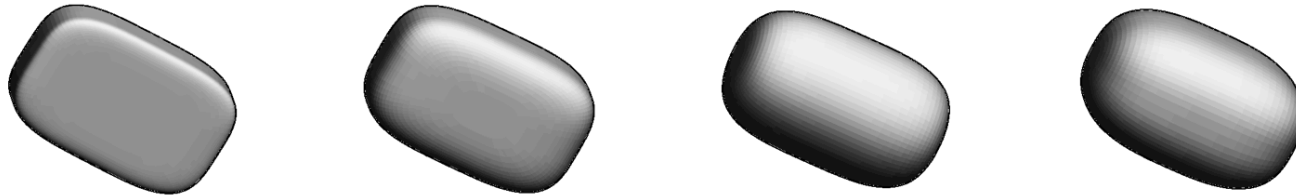
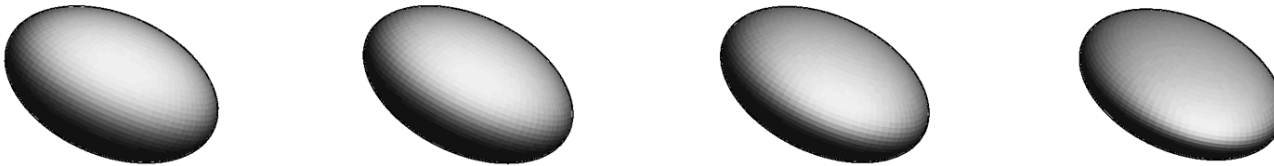
Superquadric Glyphs for Visualizing DTI

Kindlmann 2004

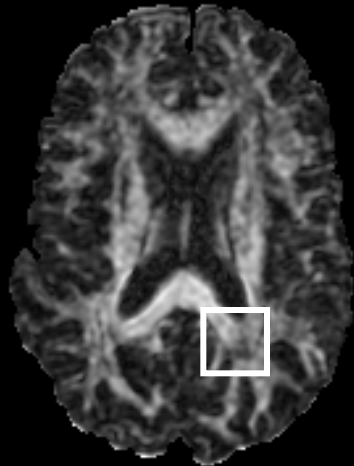




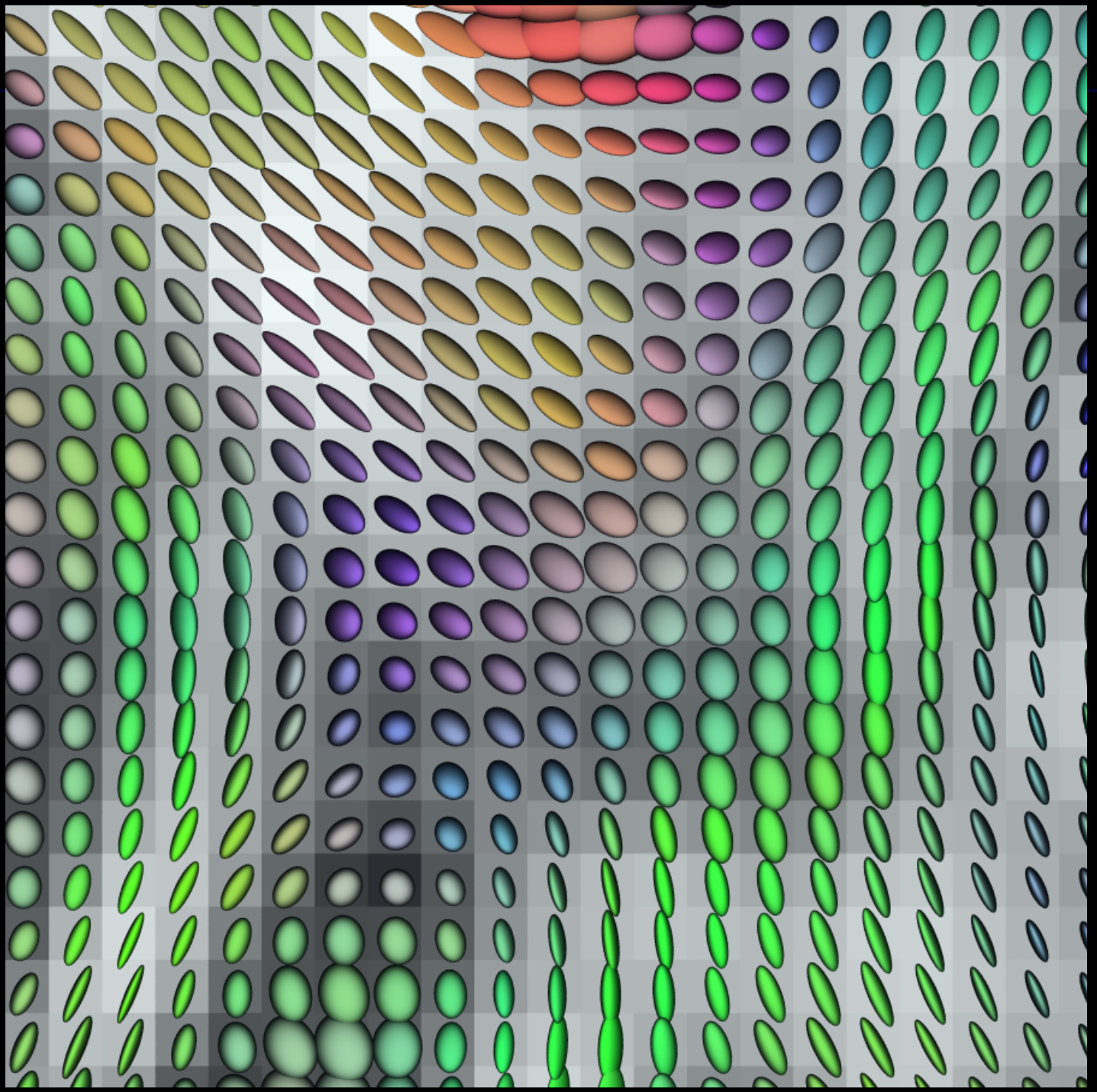
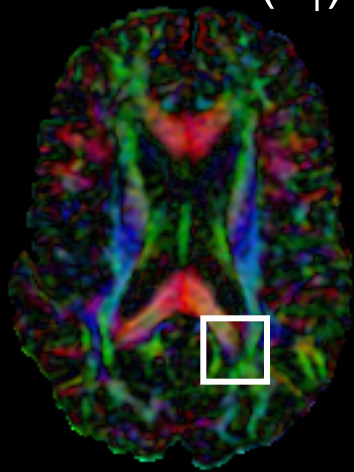
Worst case scenario, revisited



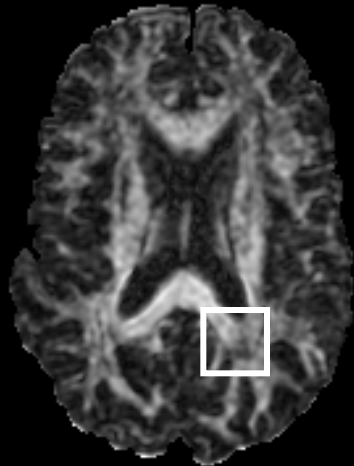
Backdrop: FA



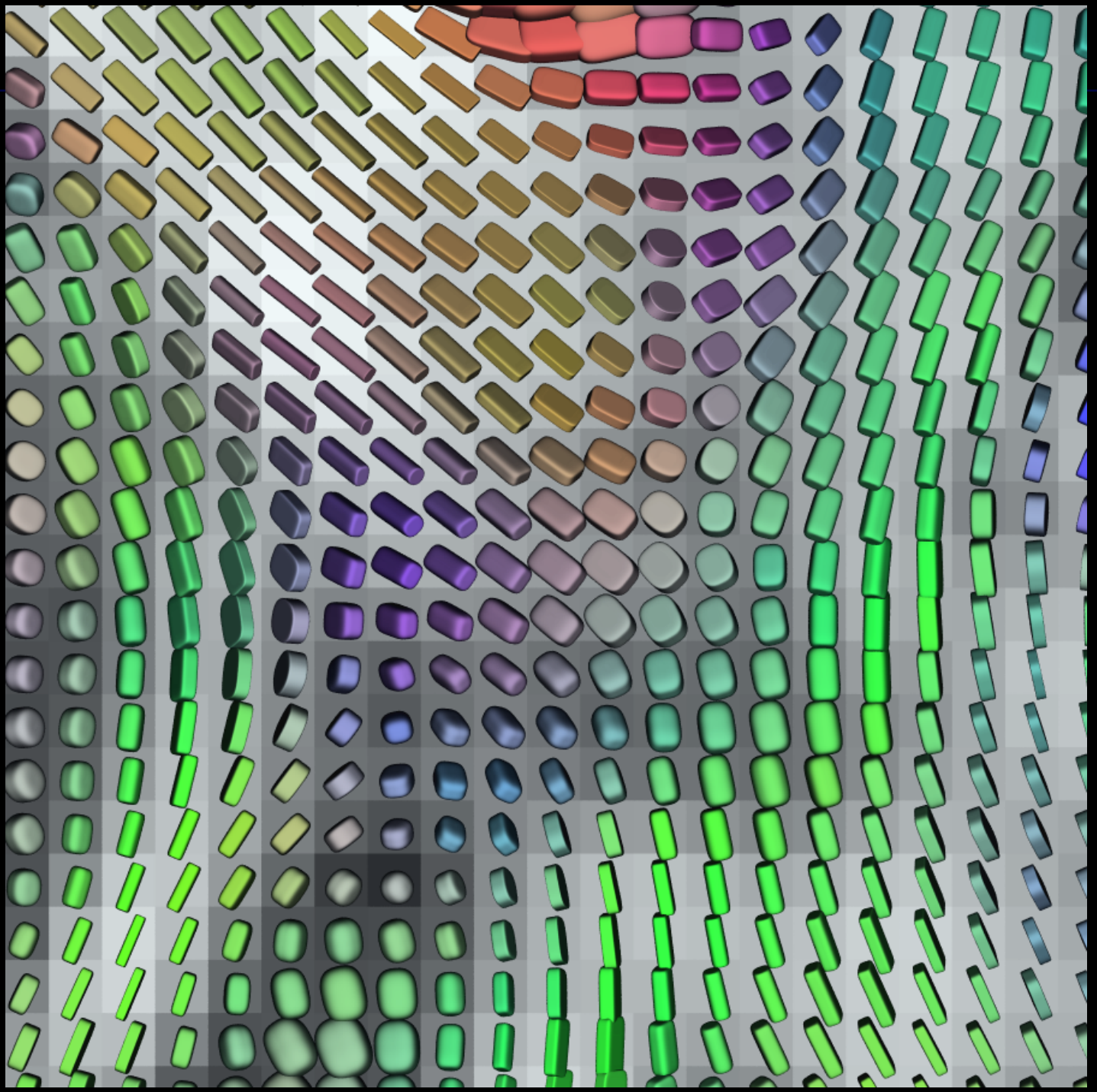
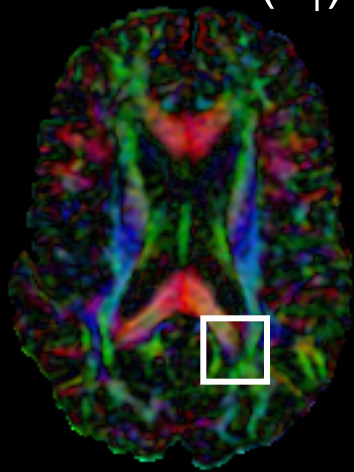
Color: RGB(\mathbf{e}_1)

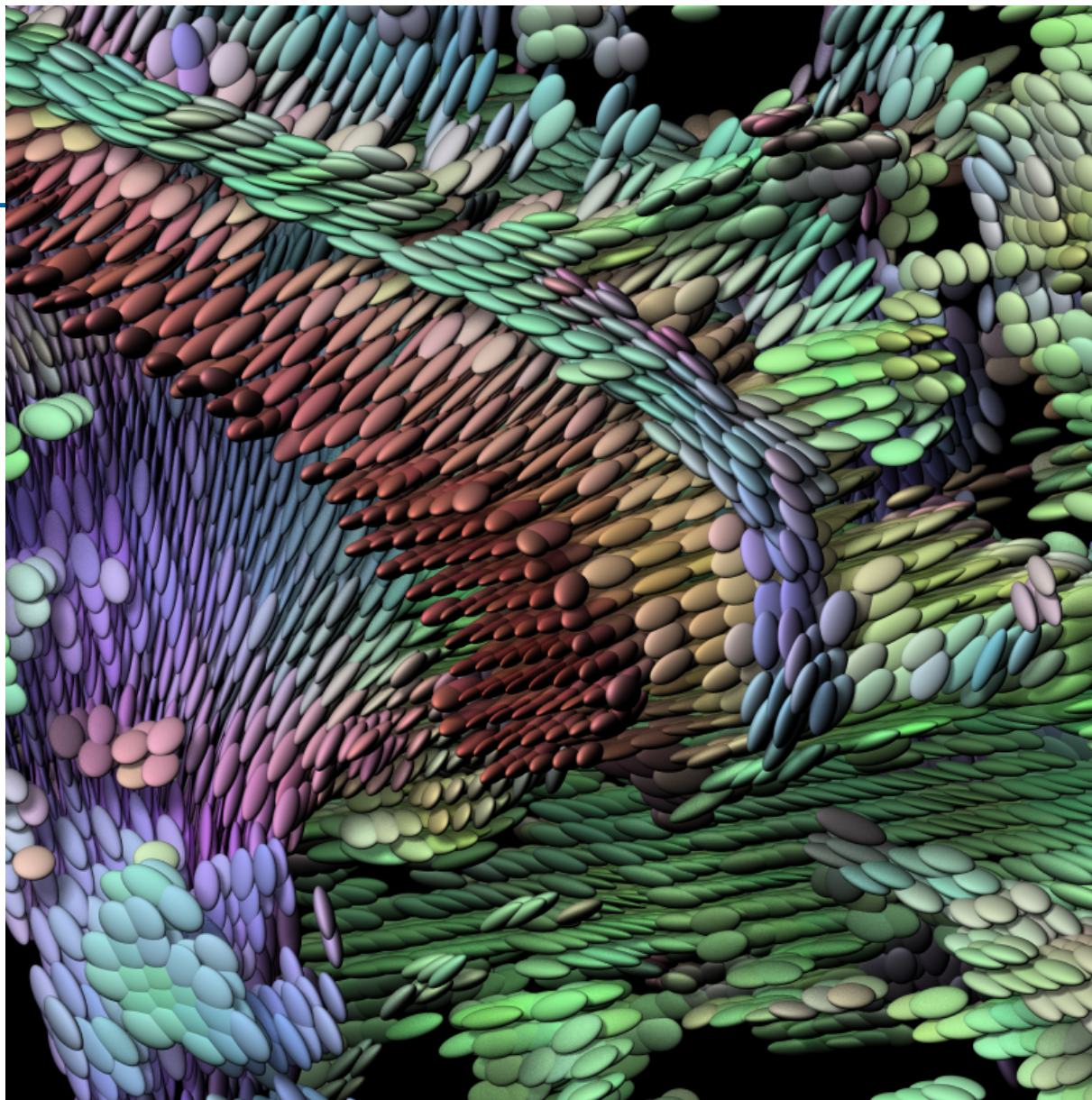


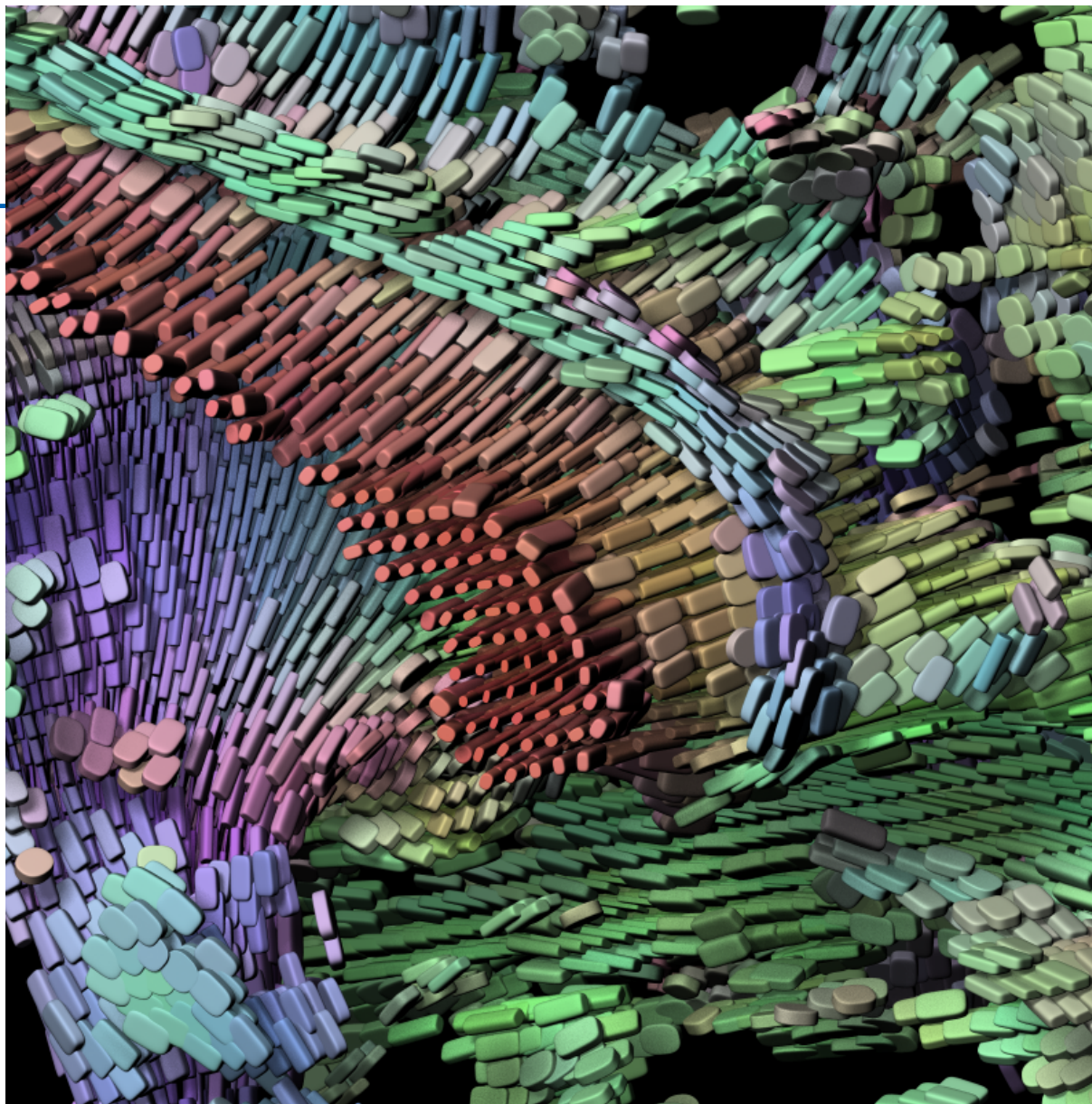
Backdrop: FA



Color: RGB(\mathbf{e}_1)



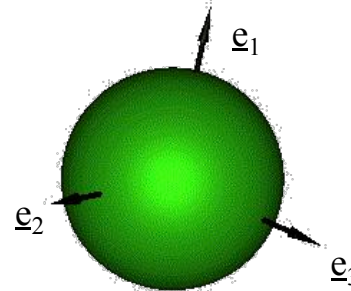
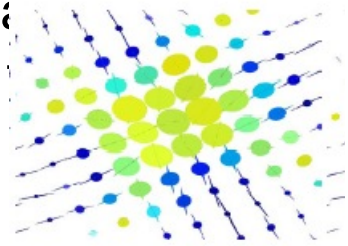




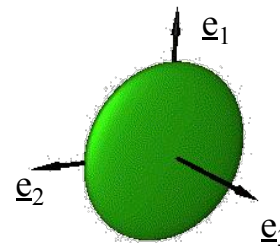


Why do we care?

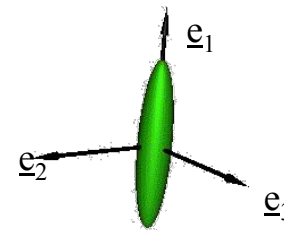
- Free diffusion (ventricles) shown as spheres.
- Intersecting tracts can't be properly modeled by a single tensor: Simplified disks in rank-1 tensors.
- Large tracts can be locally modeled by single tensors.



$\lambda_1 \approx \lambda_2 \approx \lambda_3$ - Isotropic
Prevalent in CSF and gray matter regions of the brain.



$\lambda_1 \approx \lambda_2 \gg \lambda_3$ - Oblate
Arise in white matter regions.



$\lambda_1 \gg \lambda_2 \approx \lambda_3$ - Prolate
Prevalent in white matter regions.



Shape Characterization: Westin

$$c_l = \frac{\lambda_1 - \lambda_2}{\lambda_1}$$

$$c_p = \frac{\lambda_2 - \lambda_3}{\lambda_1}$$

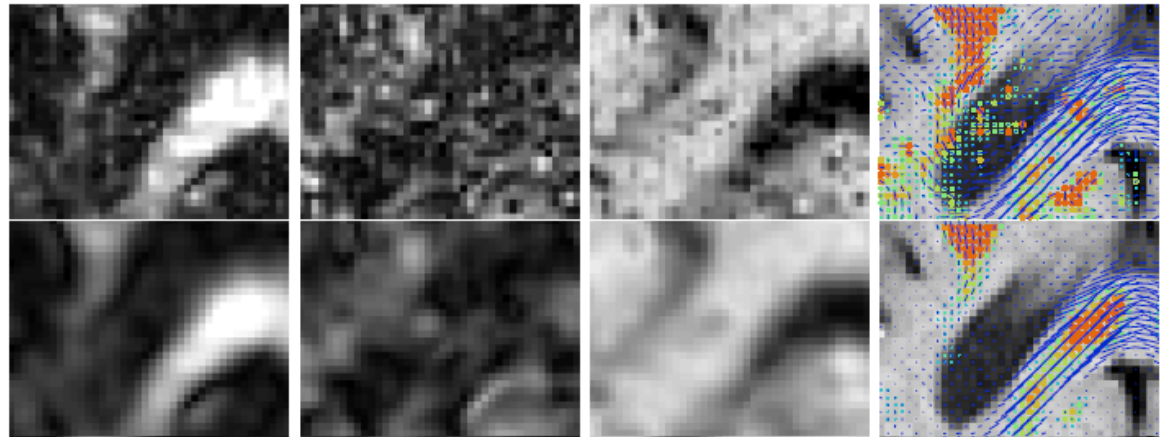
$$c_s = \frac{\lambda_3}{\lambda_1}$$

linear

planar

spherical

tensor map

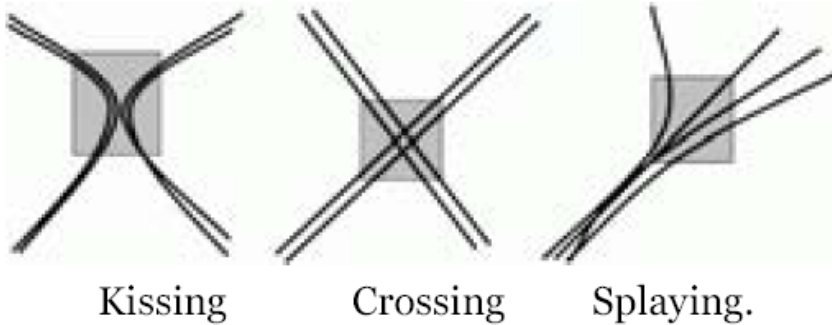


$$c_l + c_p + c_s = 1$$

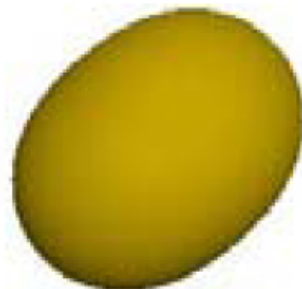
Westin et al., MICCAI' 99



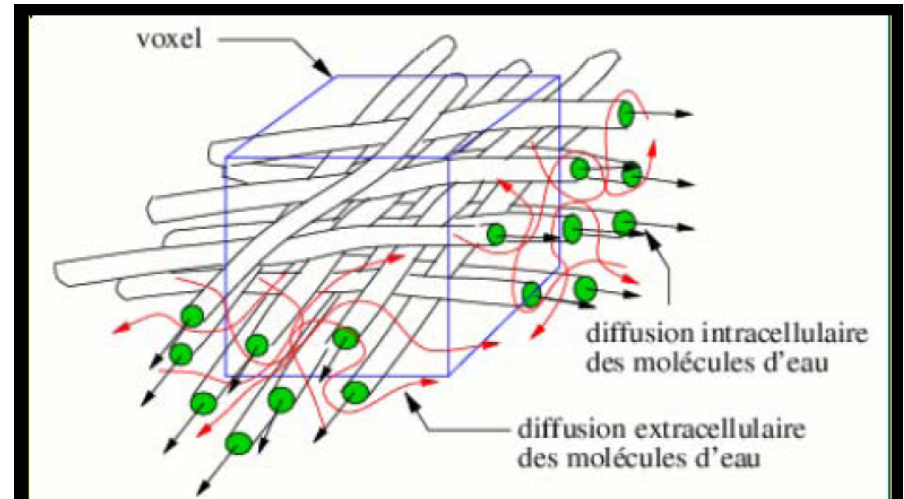
Limitations of the Diffusion Tensor Model



Diffusivity in a fiber crossing



2nd-order tensor approximation

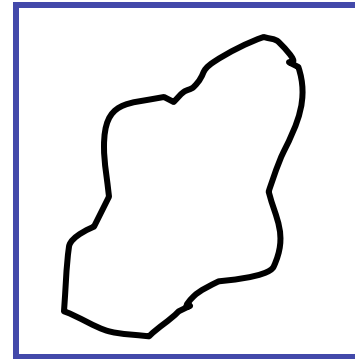
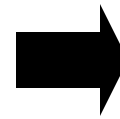
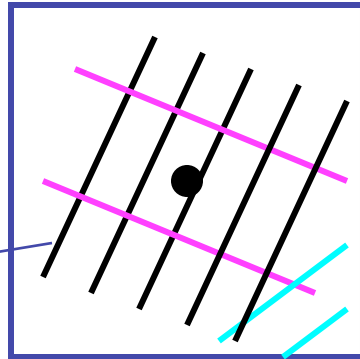
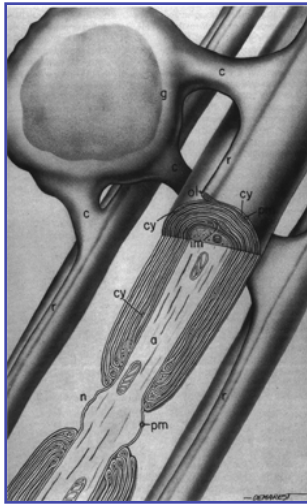


DTI fails when fiber bundles crosses within the same voxel
Non-Gaussian diffusion process - Image from [Poupon-PhD:99]

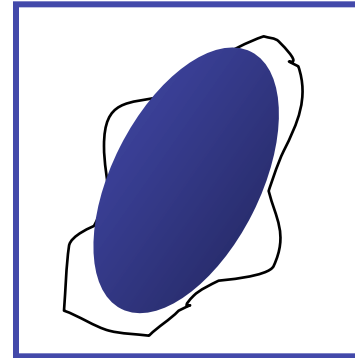
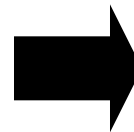
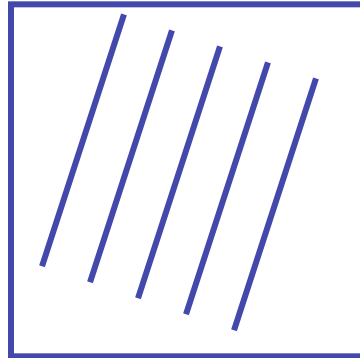
Courtesy B. Vemuri, MICCAI 2008 workshop



Simplification and assumption



Orientalional Diffusion Fct



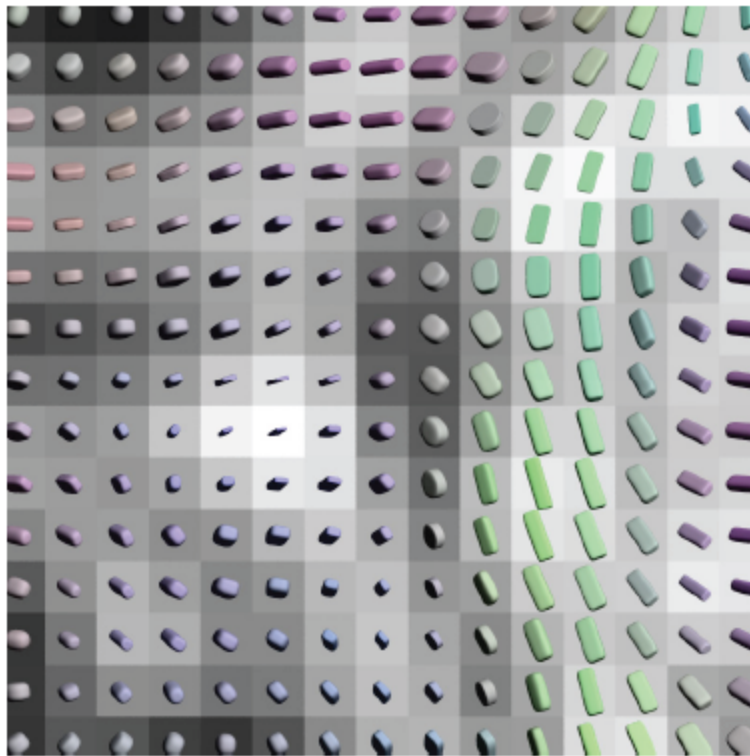
Diffusion ellipsoid

Courtesy of Susumu Mori, JHU

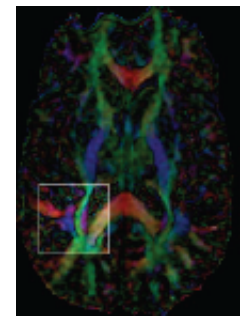
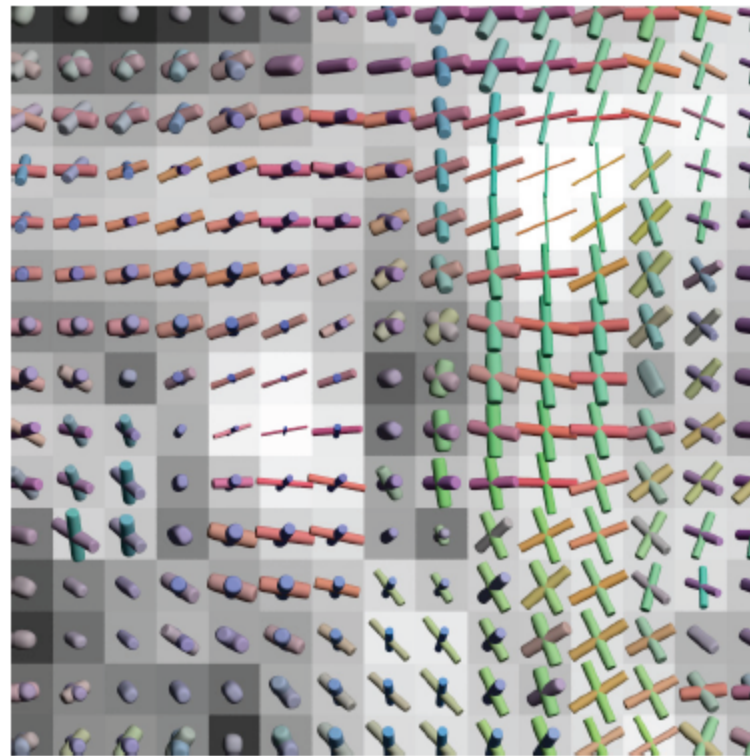


Two Tensor Model (C-F Westin, S Peled, G Kindlmann)

DTI: Single tensor model



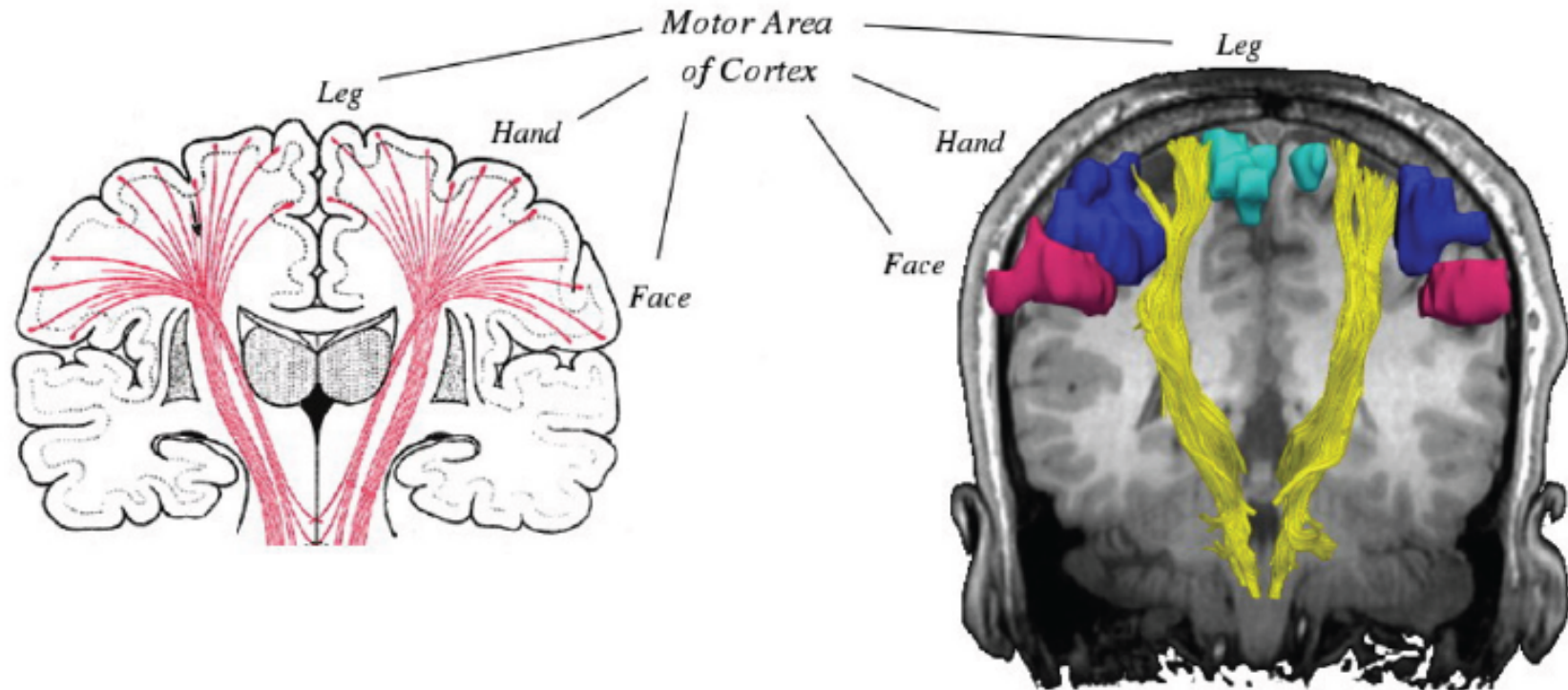
Two-tensor model



Courtesy Carl-Fredrik Westin, MICCAI 2008 workshop



Tractography Corticospinal Tract

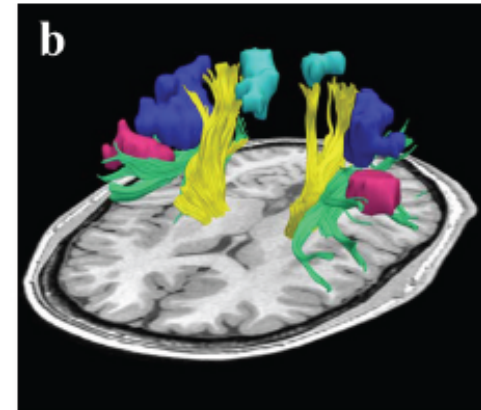
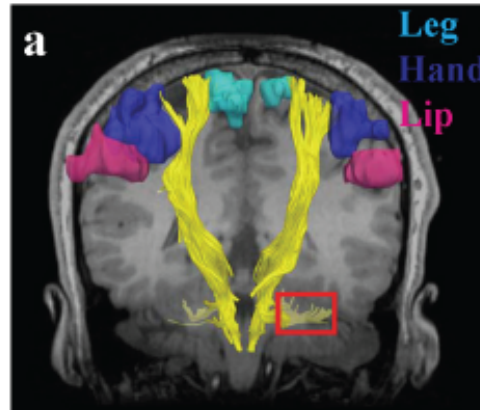


Provided by L O'Donnell

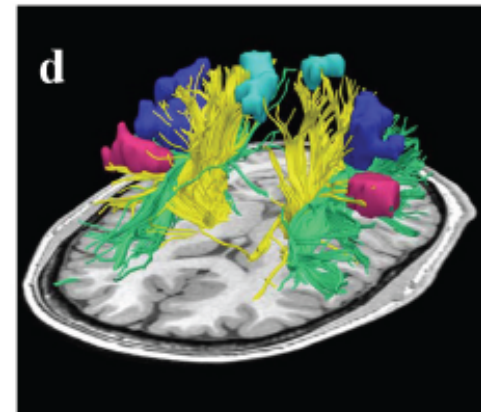
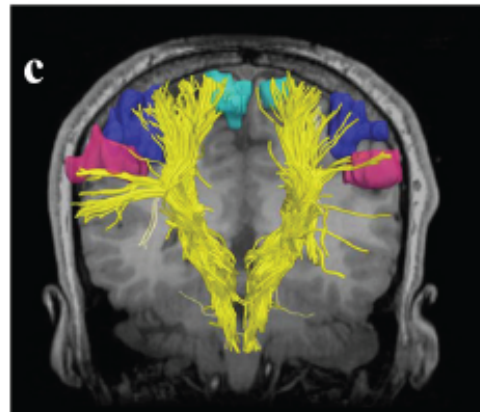


Results Two-Tensor Tractography

Single tensor model



Two-tensor model



A Qazi, A Radmanesh, L O'Donnell, G Kindlmann, S Peled, S Whalen, C-F Westin, A J Golby. Resolving crossings in the corticospinal tract by two-tensor streamline tractography: method and clinical assessment using fMRI. NeuroImage 2008



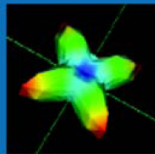
Orientation Distribution Function ODF

ODF and FRT allows to effectively recover the fibers direction

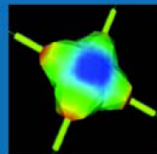
1. Apparent Diffusion Coefficient (ADC)
2. Orientation Distribution Function (ODF)



Fiber distribution

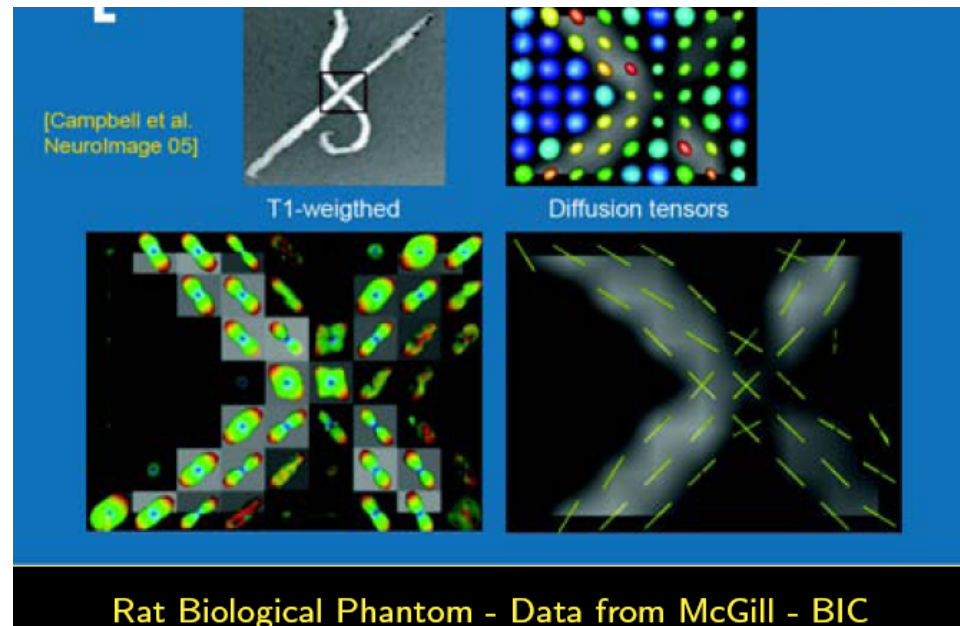


ADC profile



Diffusion ODF

Descoteaux/Angelino/Fitzgibbons/Deriché in *Magnetic Resonance in Medicine*, 2006 and 2007

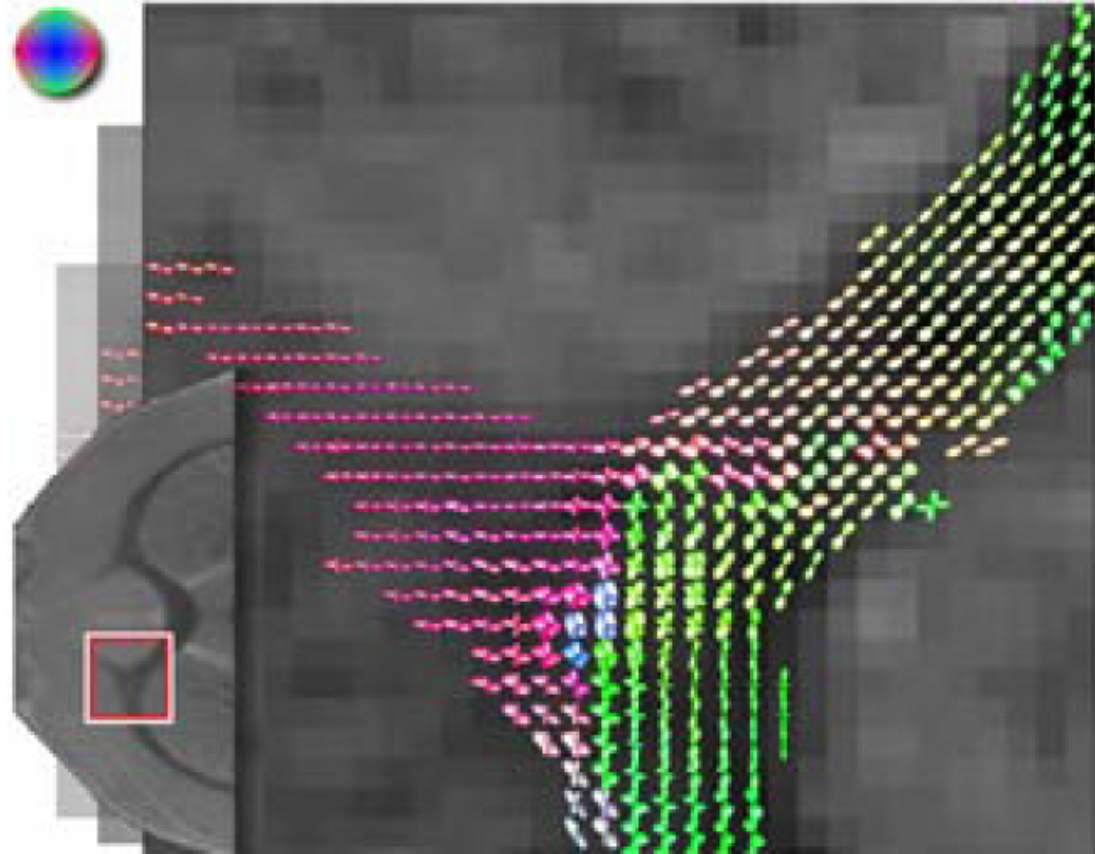


Courtesy Rachid Deriché, MICCAI 2008 workshop



Higher Order Tensor can capture fiber crossing geometry

- Excised full rat brain
- S_0 + HARDI (32 dir., B-value=1250 s/mm²)
- Data provided by Drs Carney and Mareci



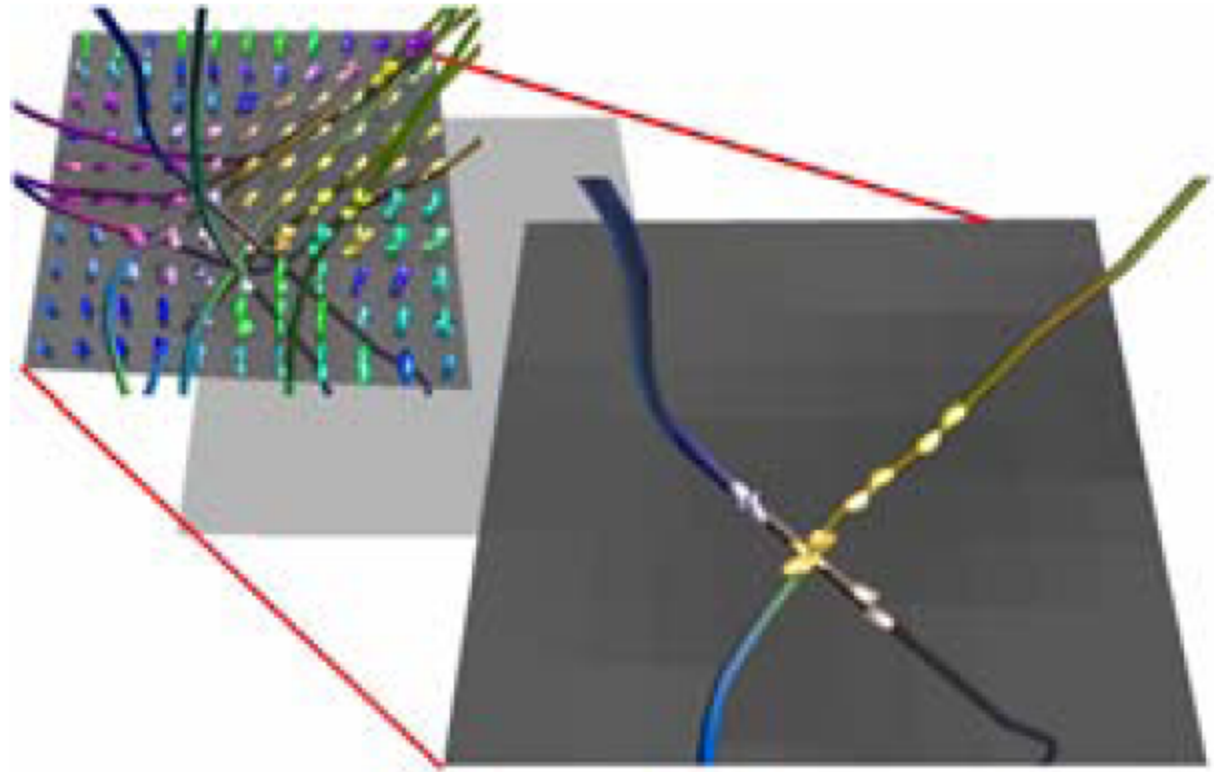
Junction of CC and singulum

Courtesy Baba Vemuri,
MICCAI 2008 workshop



Higher Order Tensor can capture fiber crossing geometry

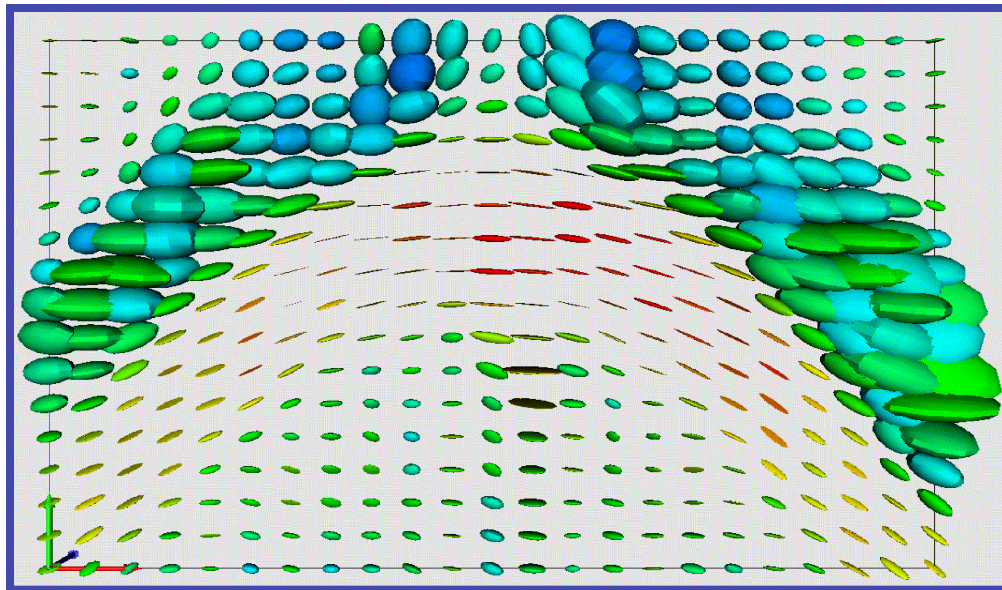
- Excised full rat brain
- S_0 + HARDI (32 dir., B-value=1250 s/mm²)
- Data provided by Drs Carney and Mareci



Courtesy Baba Vemuri,
MICCAI 2008 workshop

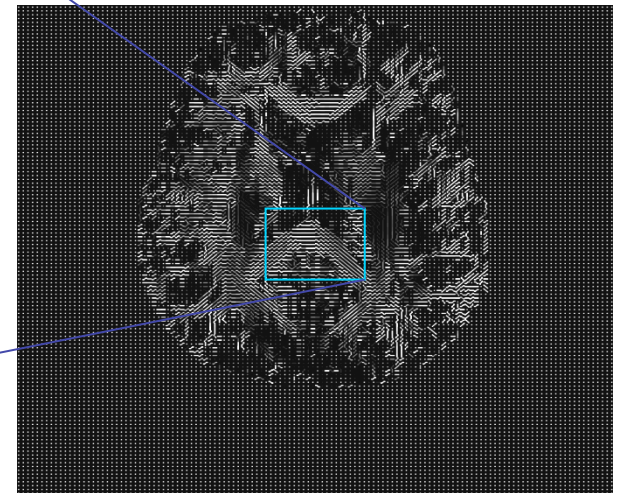


Spatial Transformations of Diffusion Tensors



Warmer colors indicate higher anisotropy

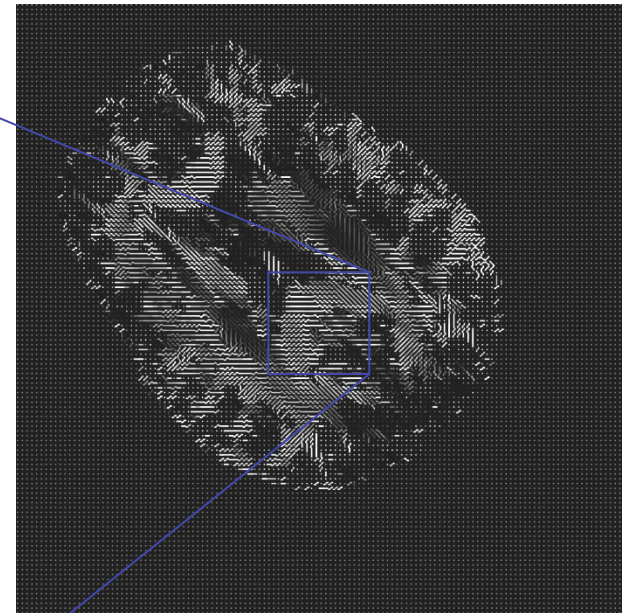
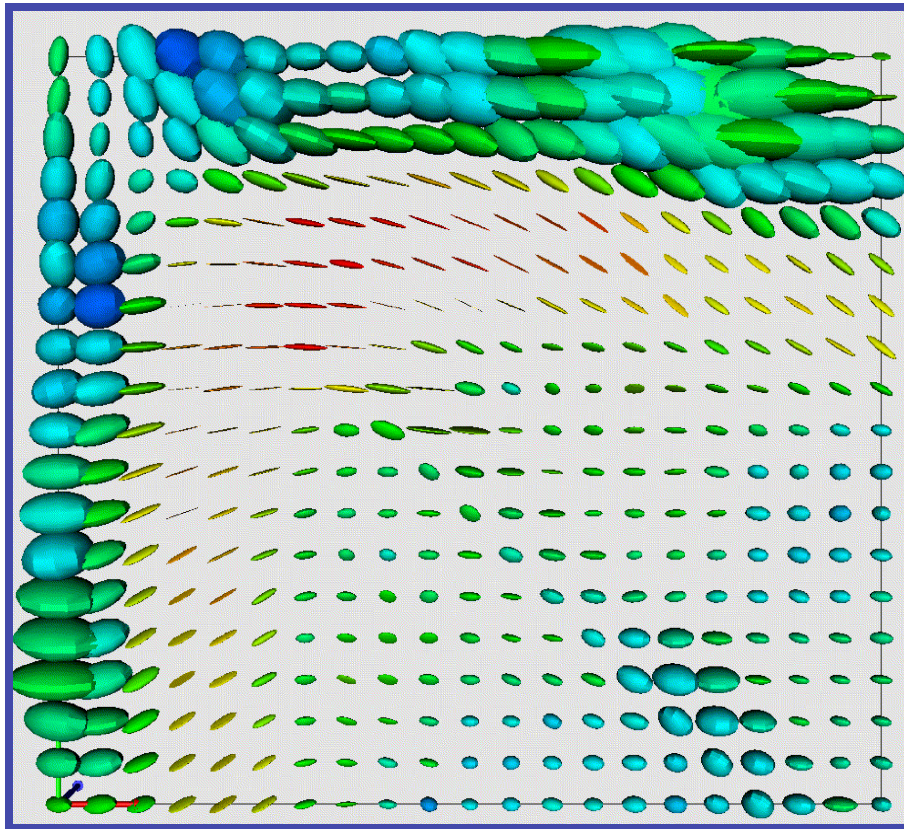
Principal diffusion directions in anisotropic regions of a DT-MR image slice



James Gee, Department of Radiology
University of Pennsylvania



Rotation without DT Reorientation

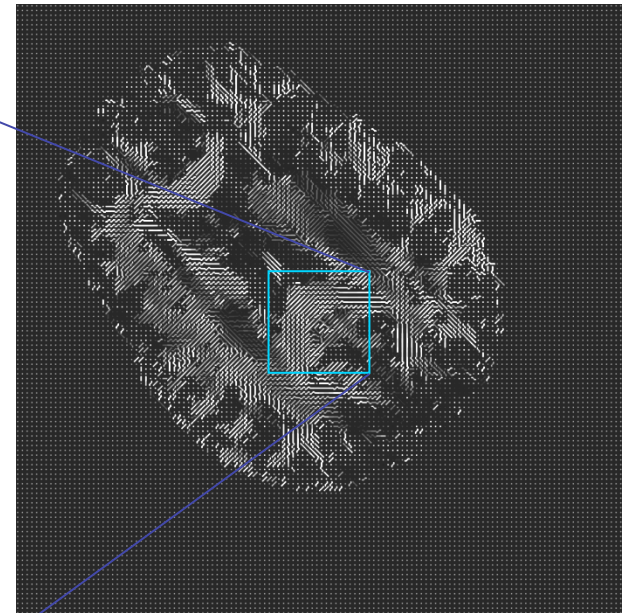
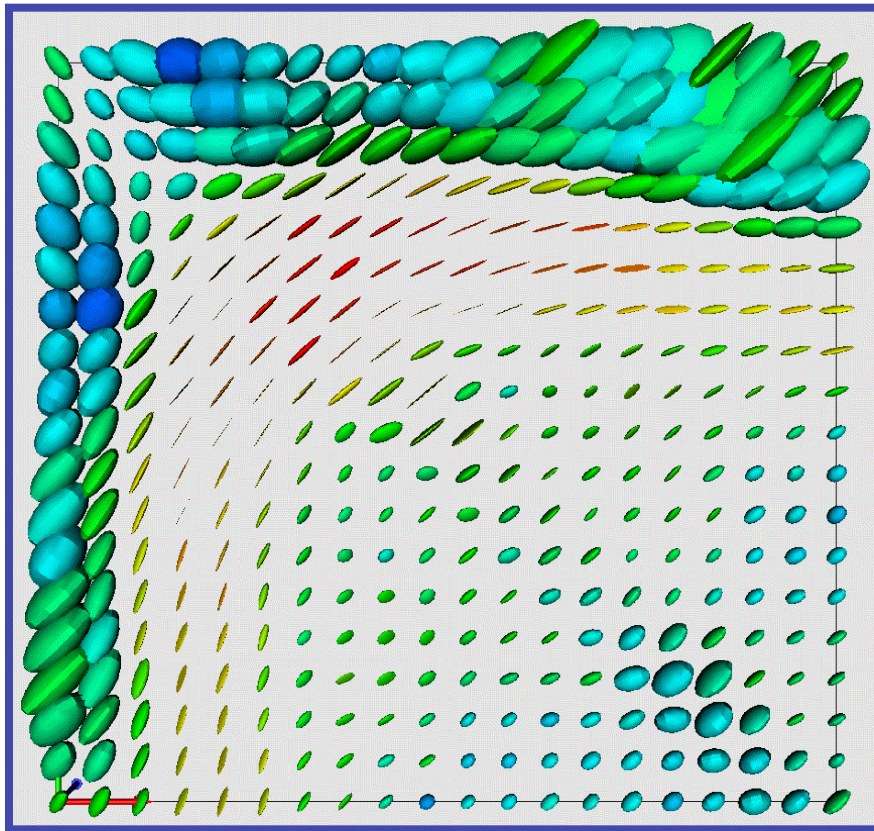


- Directional structure is lost.
- DTs orientations are no longer consistent with the anatomical structure of the image.

James Gee, Department of Radiology
University of Pennsylvania



Rotation with DT Reorientation



- $D \rightarrow R \cdot D \cdot R^T$.
- Directional structure preserved.
- DTs orientations remain consistent with the anatomy.

James Gee, Department of Radiology
University of Pennsylvania



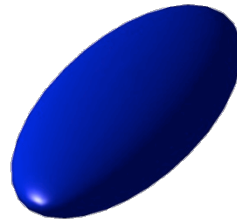
Affine Tensor Transformations

(Alexander et al, MICCAI 1999)

Original
Tensor

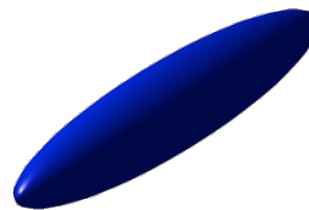


Transformed
Tensor



$$D \rightarrow F \cdot D \cdot F^T$$

- We wish to **preserve the shape** of the DTs.
- But we must reorient them appropriately.
- Require R that reflects reorientation due to F .



$$D \rightarrow R \cdot D \cdot R^T$$

- For an affine transformation, $D \rightarrow F \cdot D \cdot F^T$?
- **No...**

Finite Strain Estimation

- Decompose F into:
 - Rigid rotation, R , and
 - Deformation, U :
$$F = R \cdot U$$
$$R = F \cdot (F^T \cdot F)^{-1/2}$$
- Then reorient D using R :
$$D' = R \cdot D \cdot R^T$$

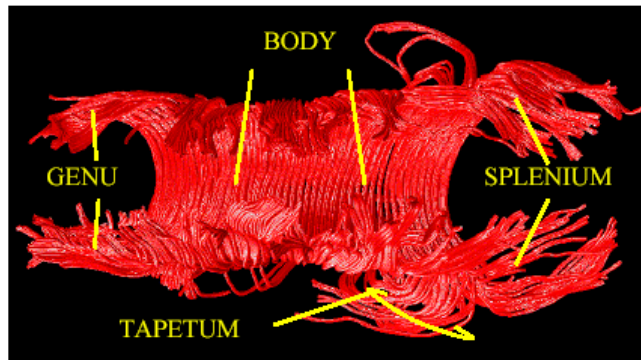
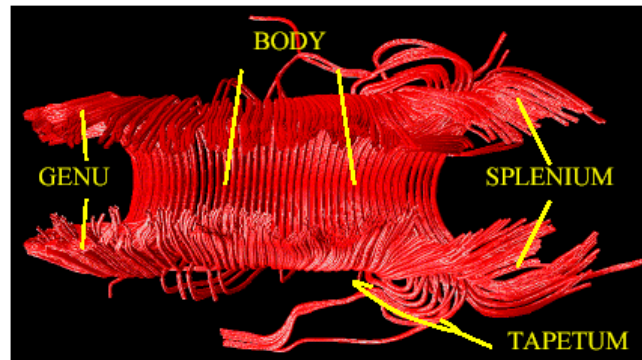
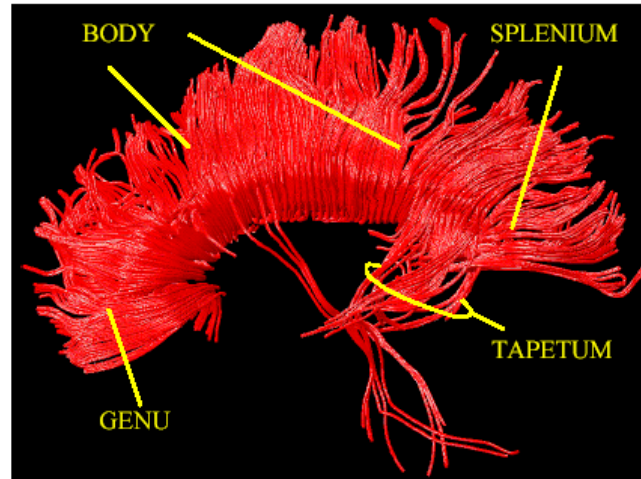
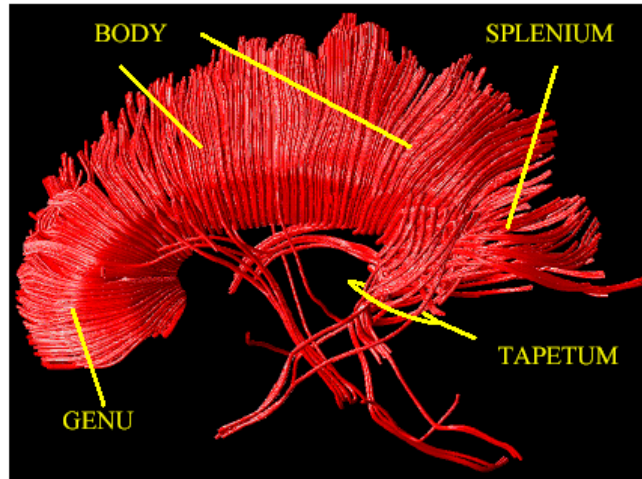


Mean Callosal Fiber Map

Diffusion Tensor Images Averaged over Ten Subjects

AVERAGE BRAIN

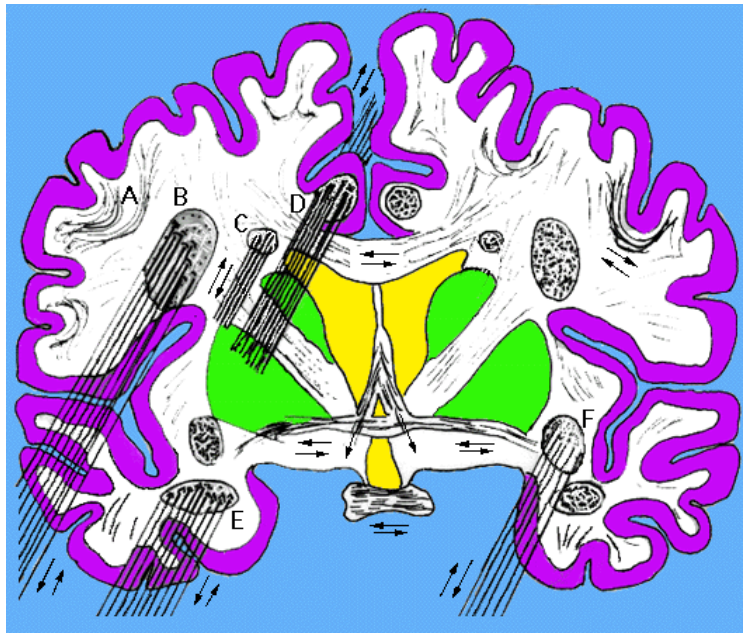
SINGLE BRAIN



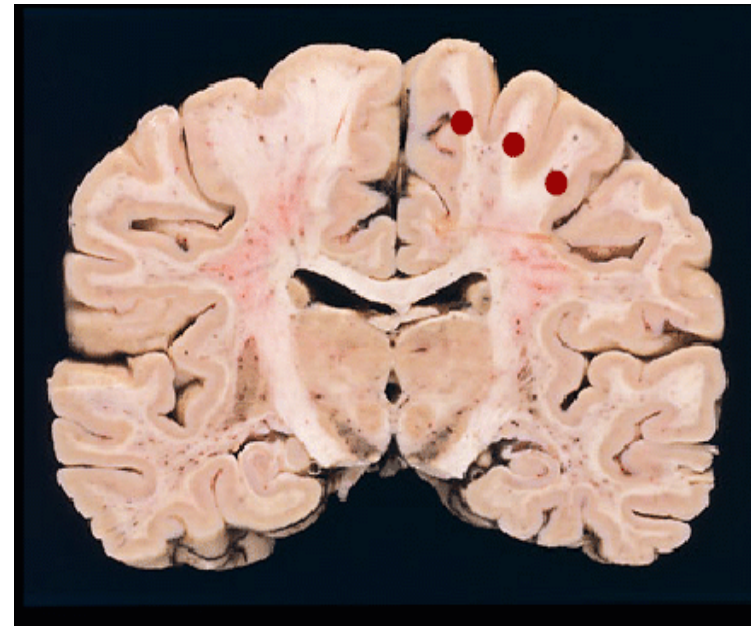
Jones et al, 2002



Dream: Connectivity?



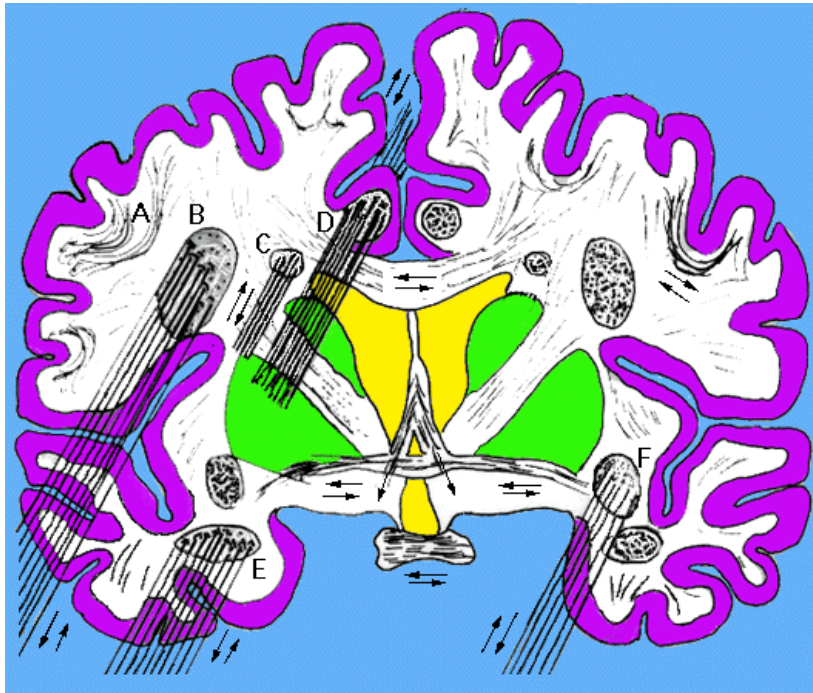
Forebrain Fiber Bundles: General idea of where various fiber bundles are and regions they interconnect or project to.



Hulotte, Duke University: Staining to get axonal projections.



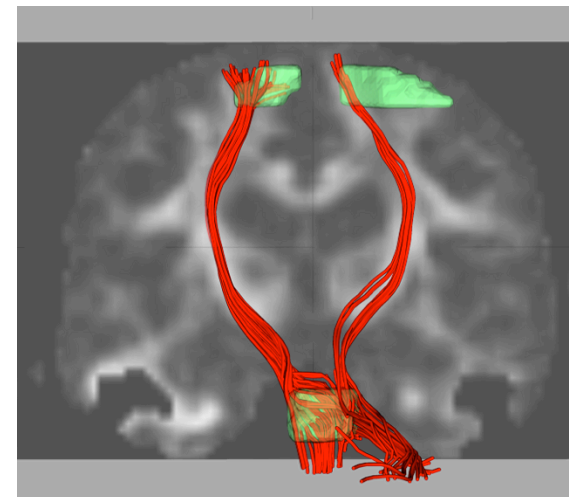
Dream: Connectivity?



Forebrain Fiber Bundles: General idea of where various fiber bundles are and regions they interconnect or project to.



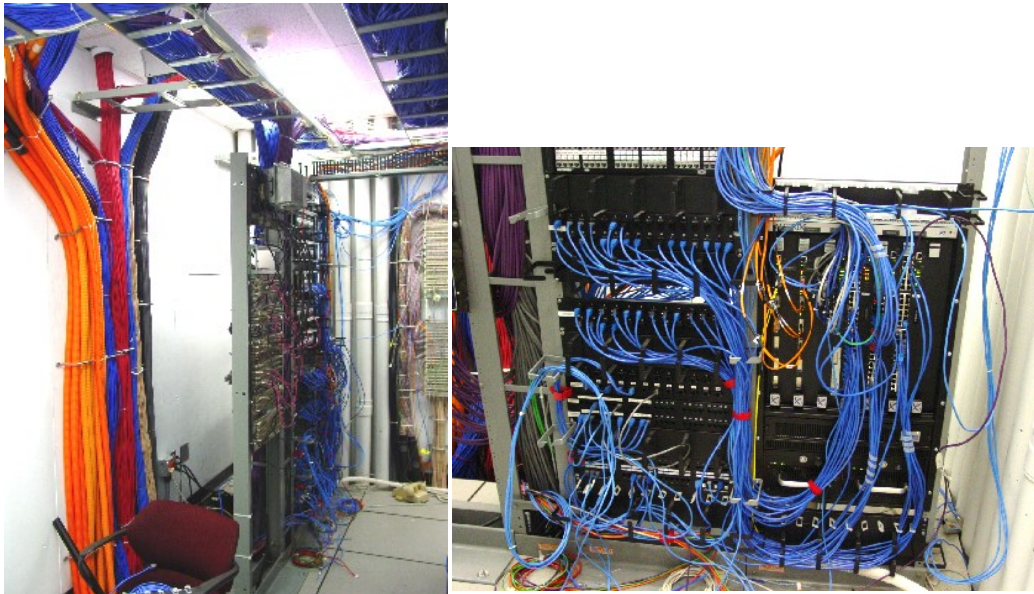
Source: Duke NeuroAnatomy Web Resources (Ch. Hulette)



Tractography: Coronal view

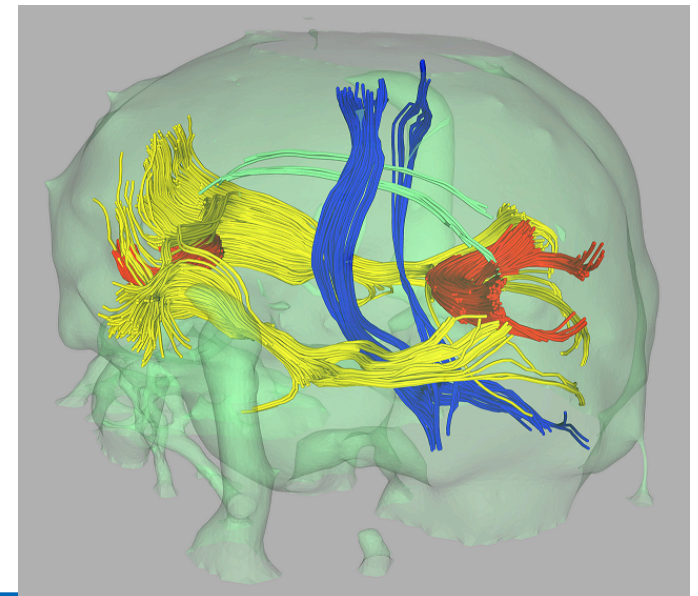


Networking and Brain Connectivity



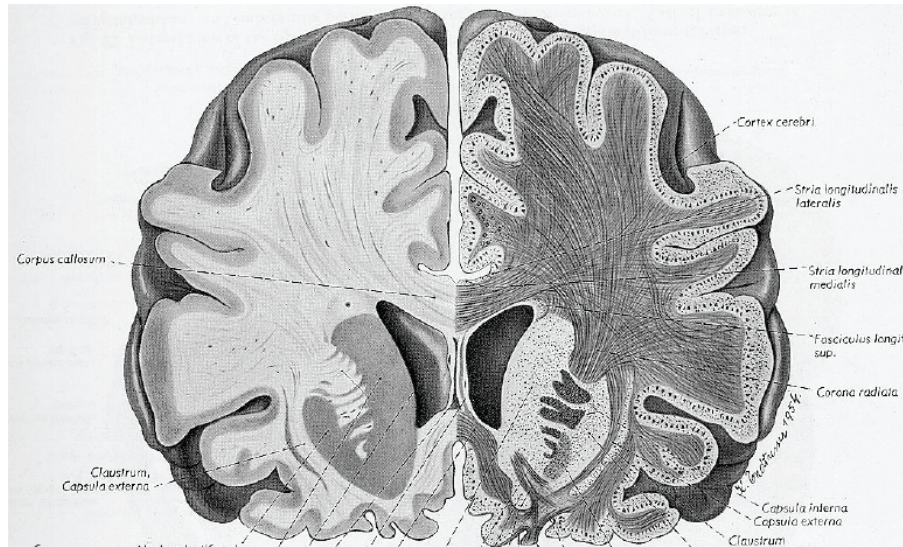
**UNC Computer Science:
Network wire cabinets**

**Major Fiber
Tracts extracted
from DT MRI**

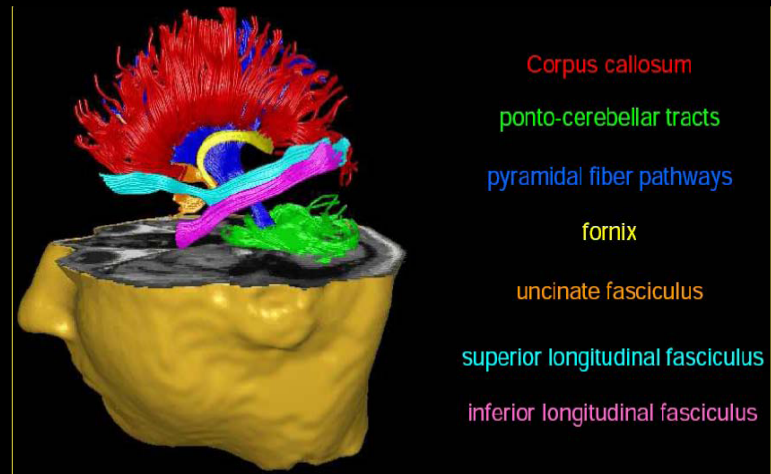




White Matter Tracts



WM Fiber Structures of the Human Brain



WM Fibers structures : Image from [Alexander Leemans - PhD:06]

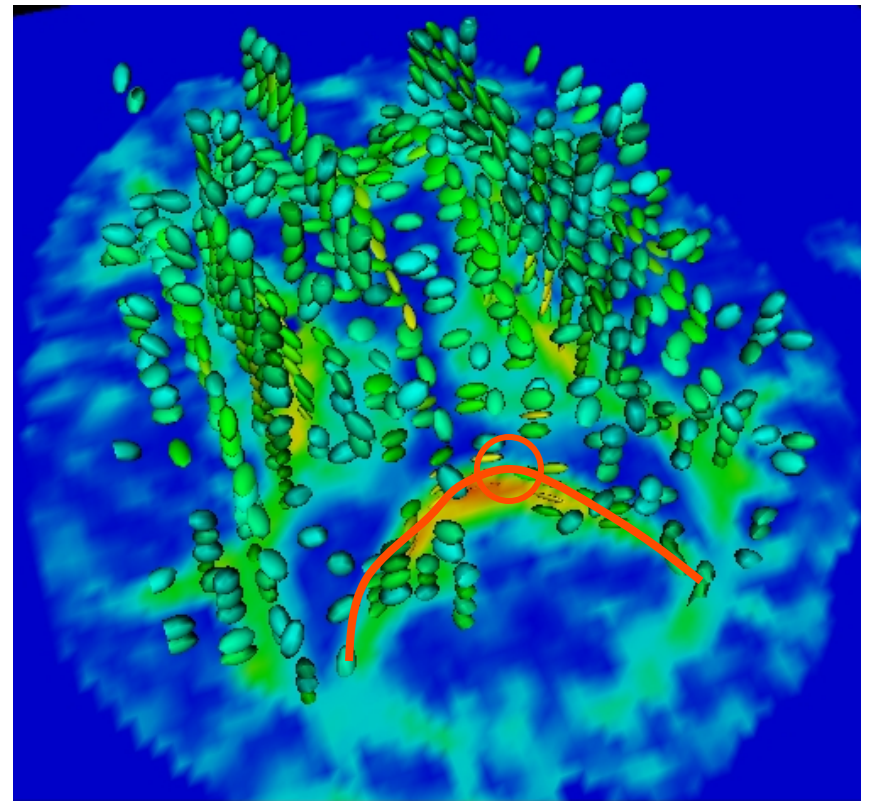
- In tractography fibers are traced, with the aim to visualize white matter tracts.
- The word “tractography” is not related to “tracking”, but to “tract”.
- White matter tract, white matter fasciculus

Courtesy Carl-Fredrik Westin, MICCAI 2008 workshop



From Tensors to Connectivity?

- Study diffusivity in 3D tensor field
- Propagate principal diffusion direction originating at user-selected seed point
- Display paths as streamlines
- Measurement of FA and MD along path





DTI Tractography

Seed point(s)

Move marker in discrete steps and find next direction

Direction of principle eigen value



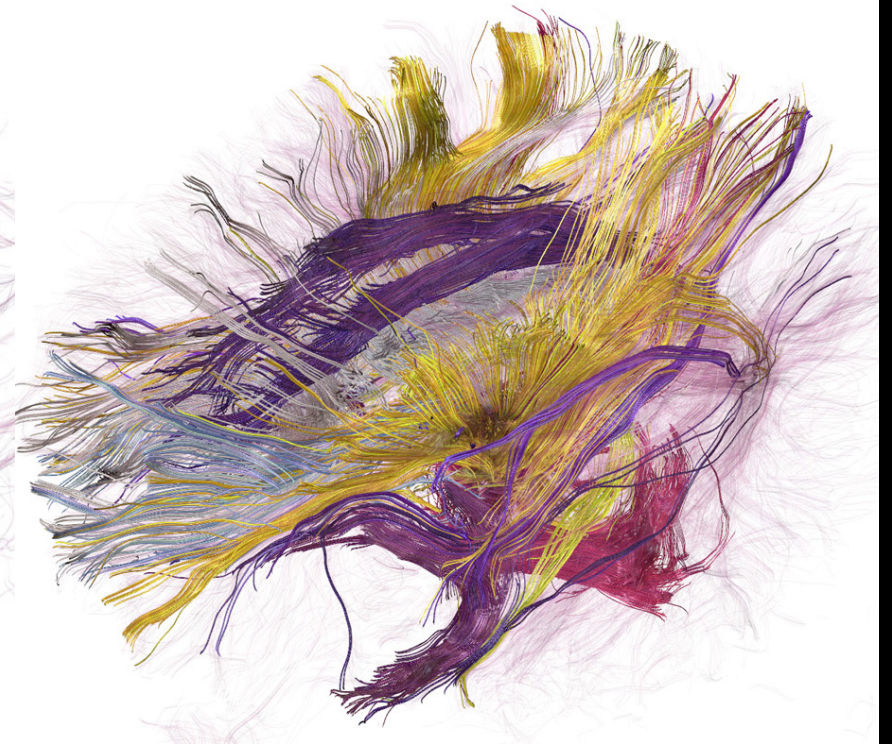


Going Beyond Voxels: Tractography

- Method for visualization/analysis
- Integrate vector field associated with grid of principle directions
- Requires
 - Seed point(s)
 - Stopping criteria
 - FA too low
 - Directions not aligned (curvature too high)
 - Neighborhood coherence
 - Leave region of interest/volume
- Many methods have been published during the past decade (Basser, Mori, Westin, Vermuri, Kindlmann, Lenglet, etc.)



Tractography



J. Fallon



White Matter Fiber Tract Atlases

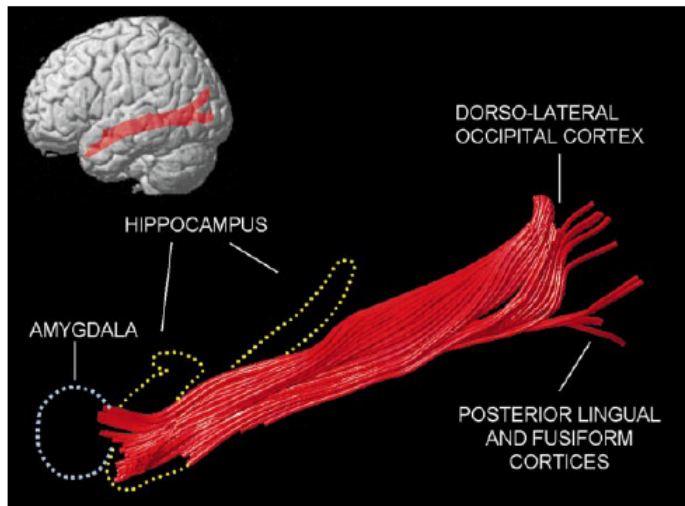


Fig. 7 Reconstruction of the ILF in the average DT-MRI data set. The long fibres originate from extrastriate areas of the occipital lobe and terminate in lateral temporal cortex and medial temporal cortex in the region of the amygdala and parahippocampal gyrus.

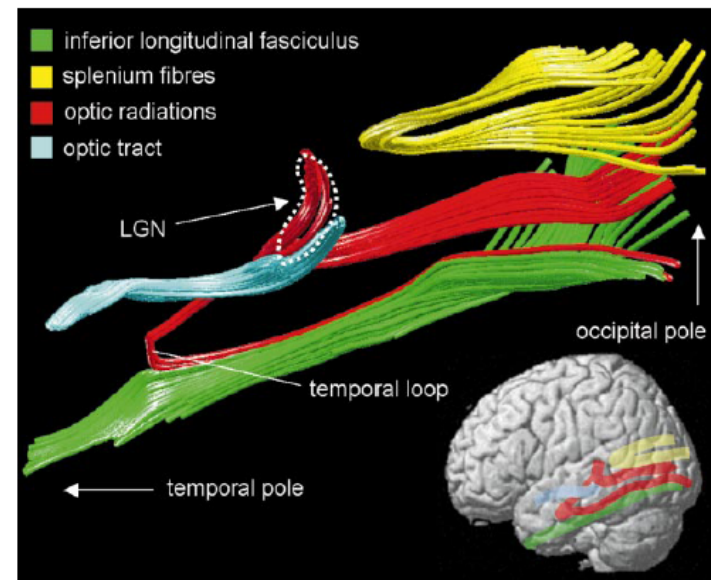


Fig. 2 Virtual *in vivo* dissection of the ILF and visual pathway of the right hemisphere (medial view) in the average brain data set. Splenial fibres connecting medial occipital regions are also shown. See text for explanation.

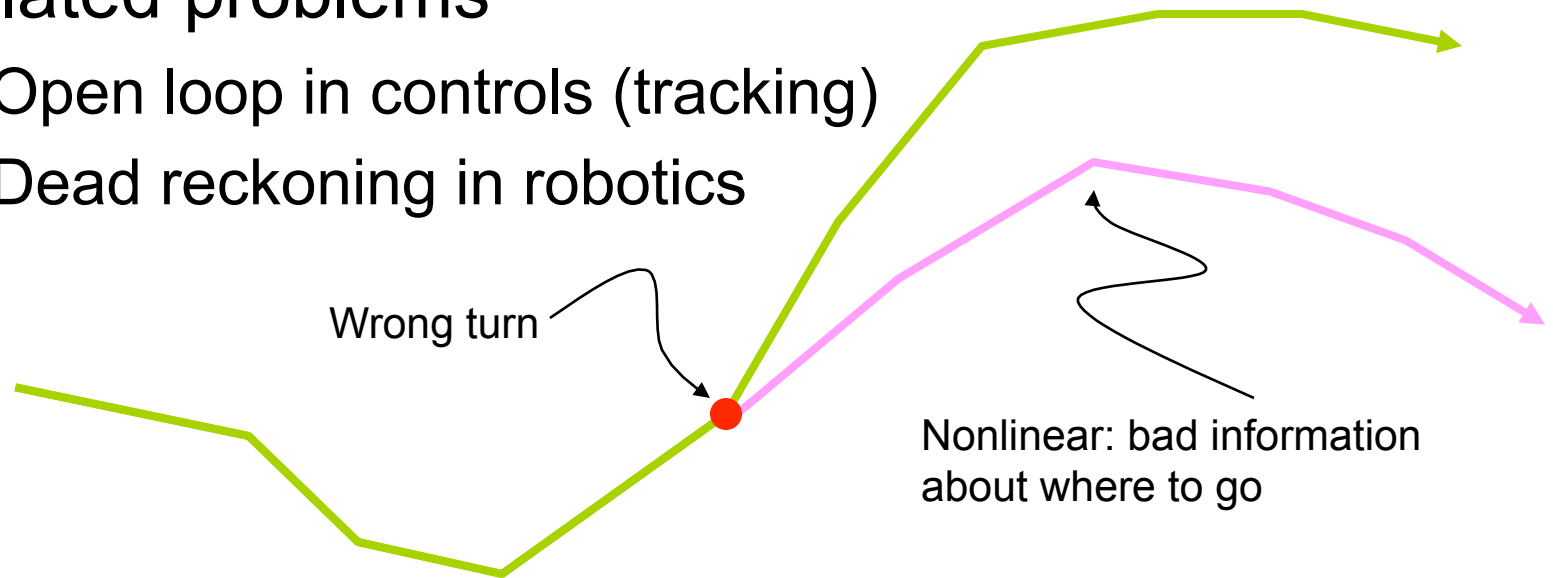
Catani et al., Occipito-temporal connections in the human brain, Brain 2003



The Problem with Tractography

How Can It Work?

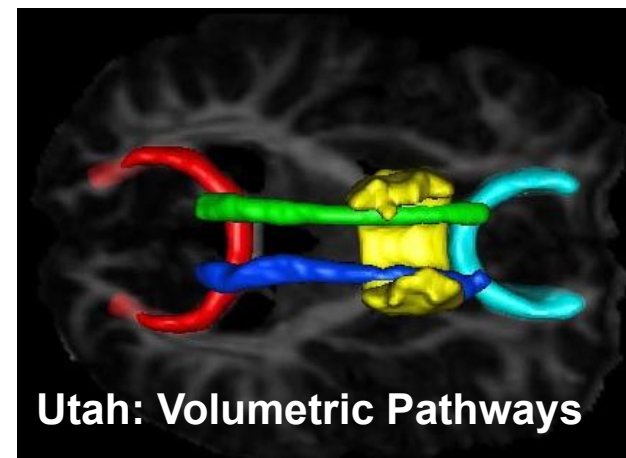
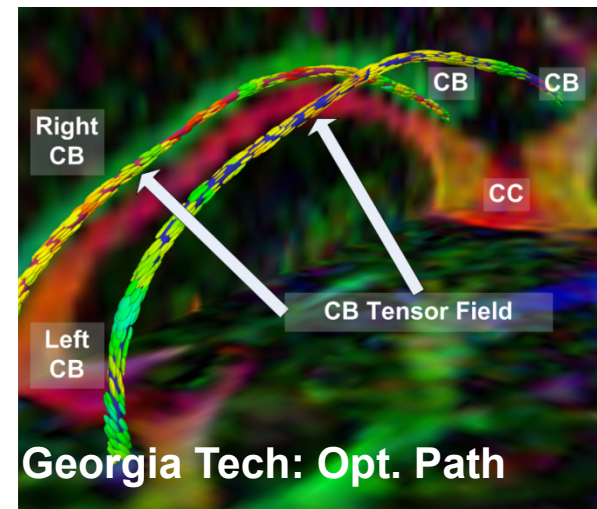
- Integrals of uncertain quantities are prone to error
 - Problem can be aggravated by nonlinearities
- Related problems
 - Open loop in controls (tracking)
 - Dead reckoning in robotics





Alternative methods for tractography

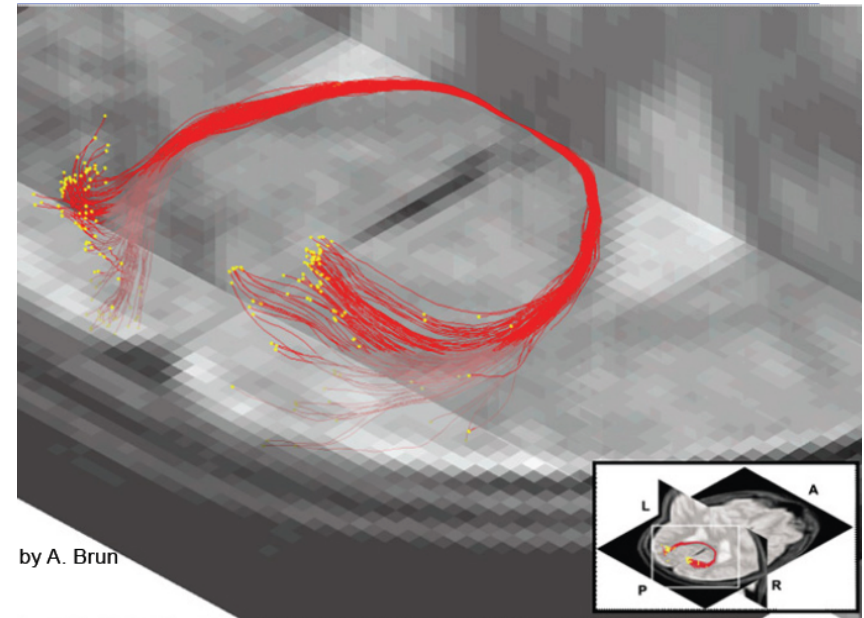
- Tracking in tensor field
- Keep history along track: e.g. Kalman filtering
- Probabilistic tractography
- Optimal path analysis
- Fiber tract by volumetric diffusion
-
- Variety of methods developed by NAMIC developers





Stochastic Tractography

- Lazar, Alexander, **White Matter Tractography using Random Vector (RAVE) Perturbation**, ISMRM 2002
- D. Tuch, Diffusion MRI of complex tissue structure, Ph.D. dissertation, Harvard-MIT, 2002
- Brun, Westin, **Regularized Stochastic White Matter Tractography Using Diffusion Tensor MRI: Monte Carlo, Sequential Importance Sampling and Resampling**. MICCAI 2002.
- Zhang, Hancock, Goodlett and Gerig, **Probabilistic White Matter Fiber Tracking using, Particle Filtering and von Mises-Fisher Sampling**, Med Image Anal. 2009 Feb; 13(1):5-18



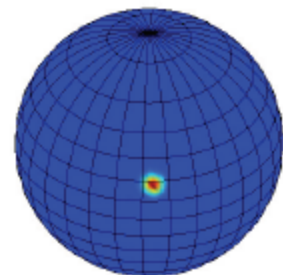
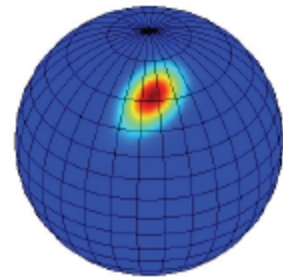
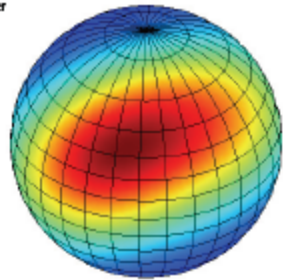
Courtesy Carl-Fredrik Westin,
MICCAI 2008 workshop



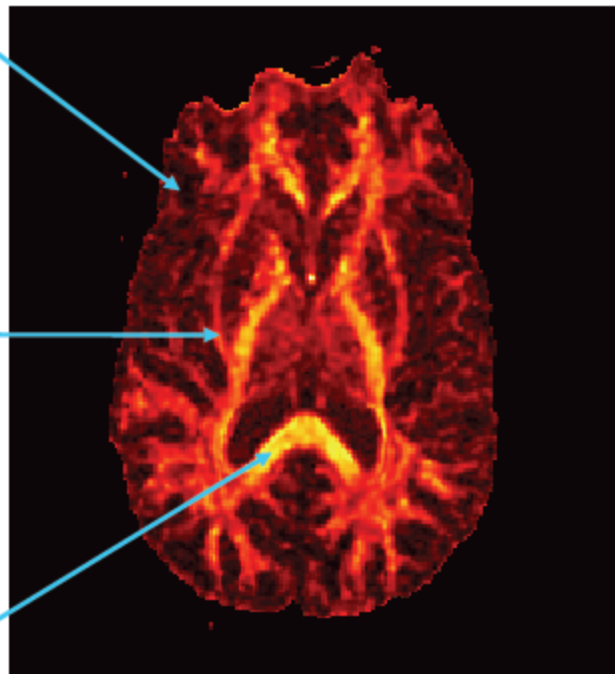
Stochastic Tractography

laboratory of
father

Friman, Westin MICCAI 2005, TMI 2006



Fractional anisotropy



A probability density function of the fiber orientation in each point.

Start point



In every step, draw a step direction from the pdf of the underlying fiber orientation.

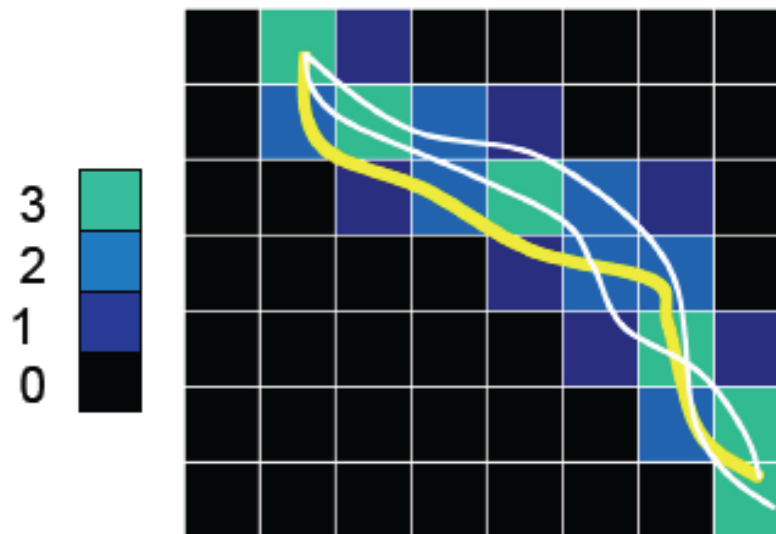
Rickman and Westin, Hospital, Harvard Medical School

Courtesy Carl-Fredrik Westin, MICCAI 2008 workshop



Probability of Connection

Given a large number of fibers, the probability of a connection between two voxels can be estimated

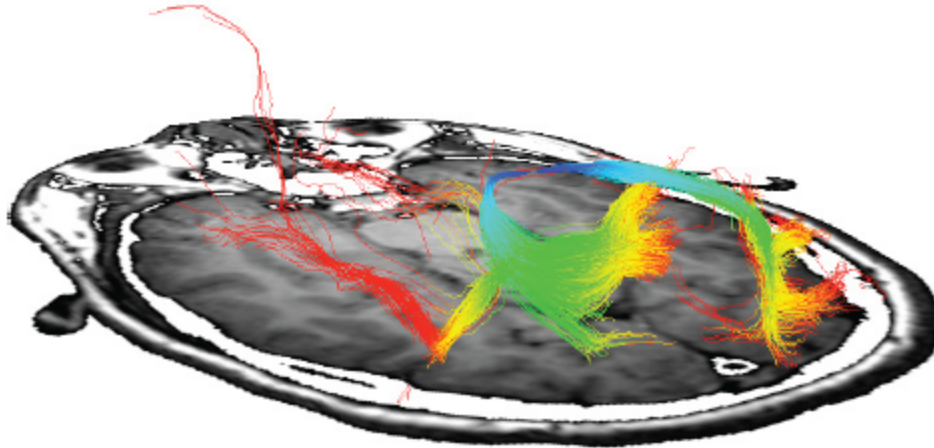


Probability density function: 1) Add the contribution from all paths, and 2) normalize the total sum of all voxels

Courtesy Carl-Fredrik Westin, MICCAI 2008 workshop



Probability of Connection



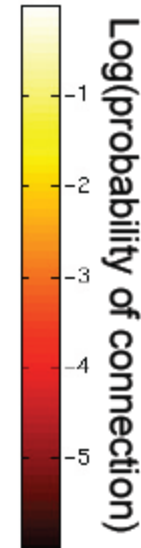
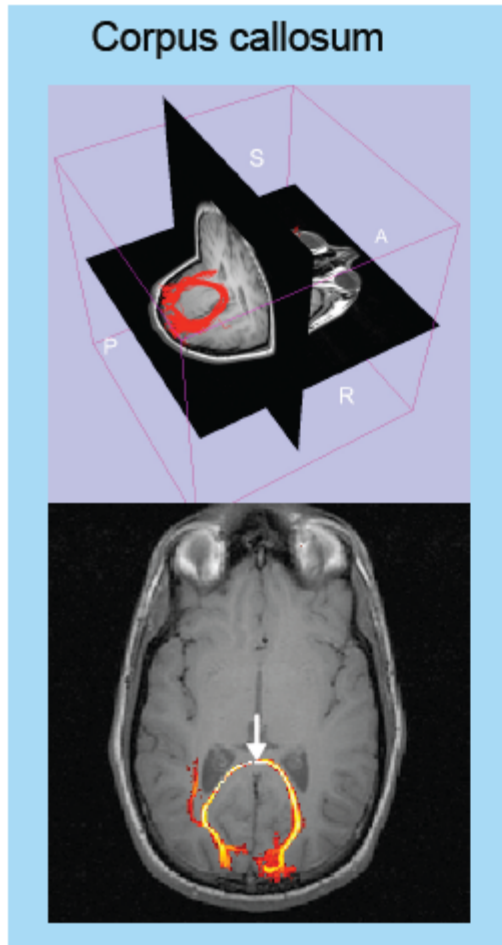
3,000 fiber samples initiated in the splenium of Corpus callosum. The coloring indicates the probability along each path to end up in a specific area.

Work with O. Friman

Courtesy Carl-Fredrik Westin, MICCAI 2008 workshop



Probability of Connection



Courtesy Carl-Fredrik Westin,
MICCAI 2008
workshop

Work with O. Friman

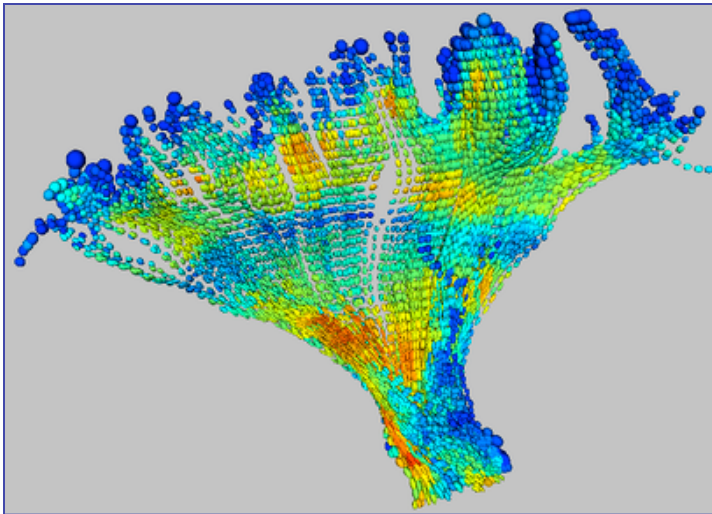


NA-MIC

National Alliance for Medical Image Computing

<http://na-mic.org>

Quantitative Tractography: NAMIC Tool FiberViewer

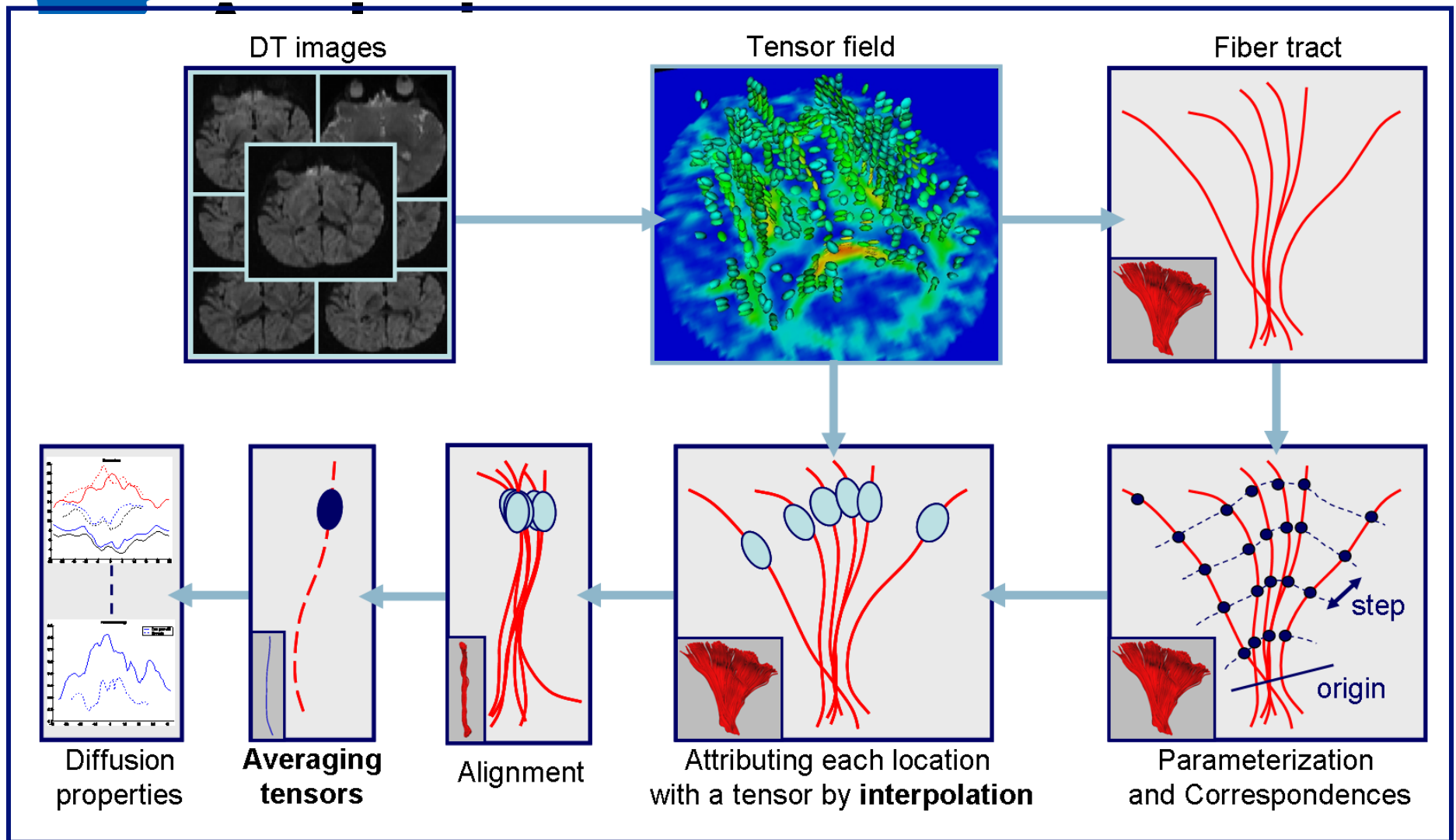


- Tractography results in selected fiber bundles of interest.
- Next step for clinical studies is geometrical and quantitative characterization.

Fiber Tract-Oriented Statistics for Quantitative Diffusion Tensor MRI Analysis, Isabelle Corouge, P.Thomas Fletcher, Sarang Joshi, Sylvain Gouttard, Guido Gerig, *Medical Image Analysis* 10 (2006), 786 - 798

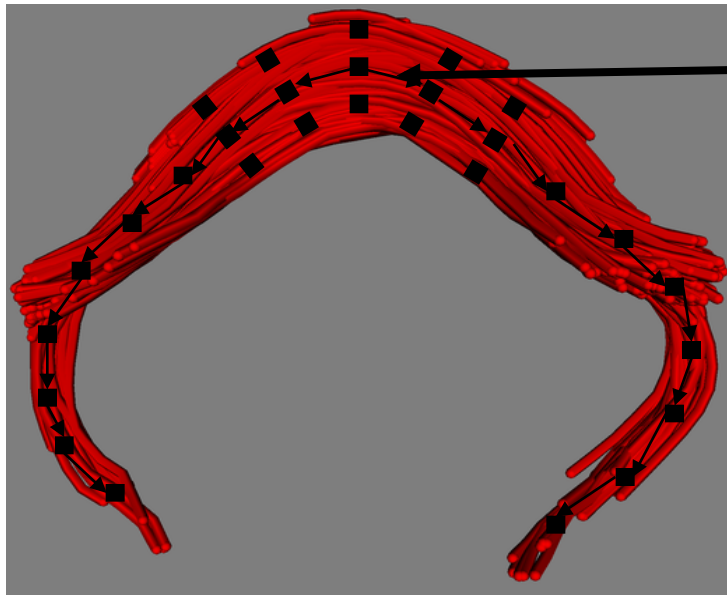


Fiber Tract Modeling and

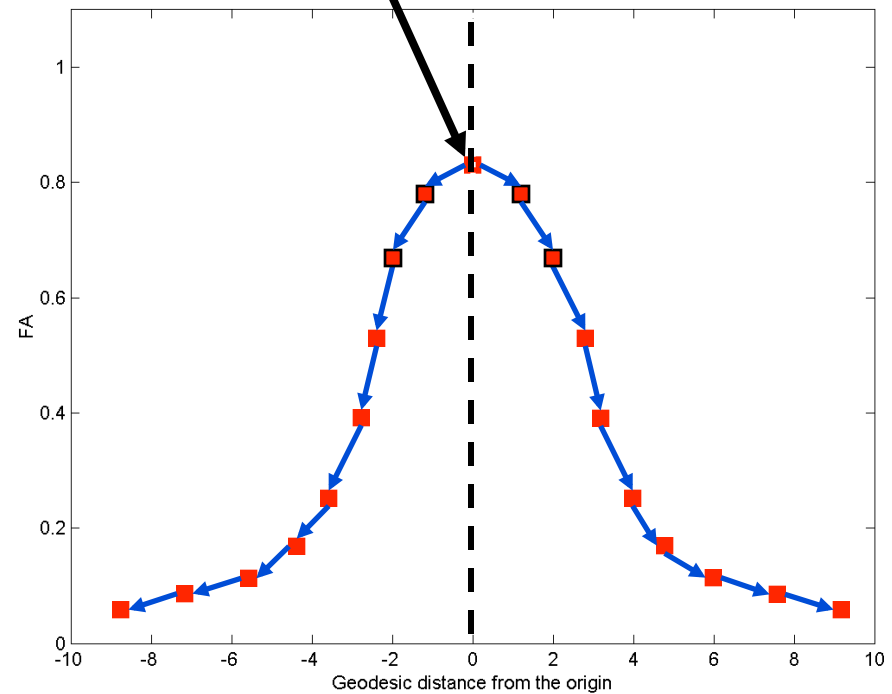
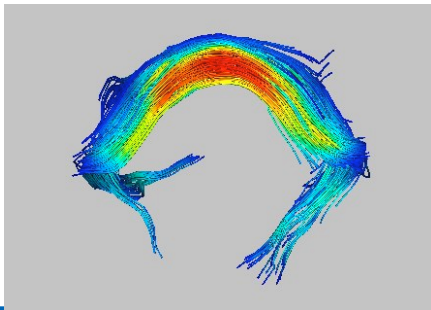




Processing of fiber tracts

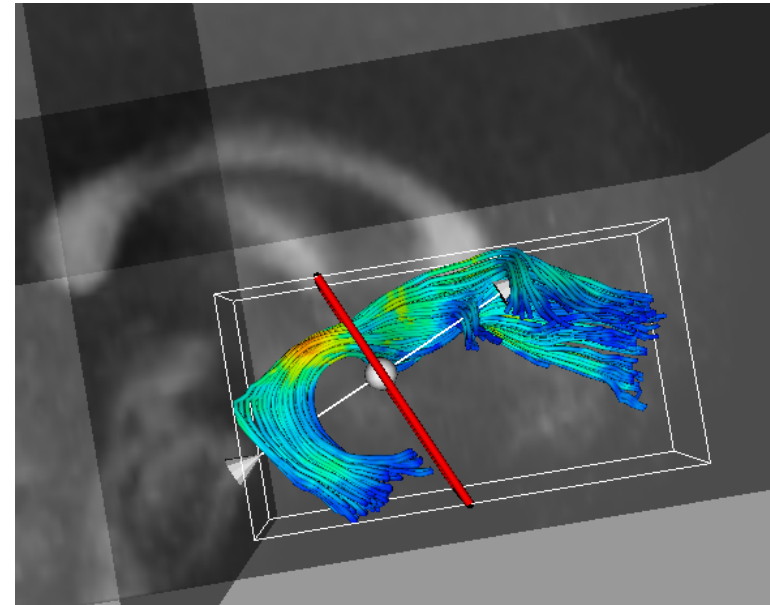
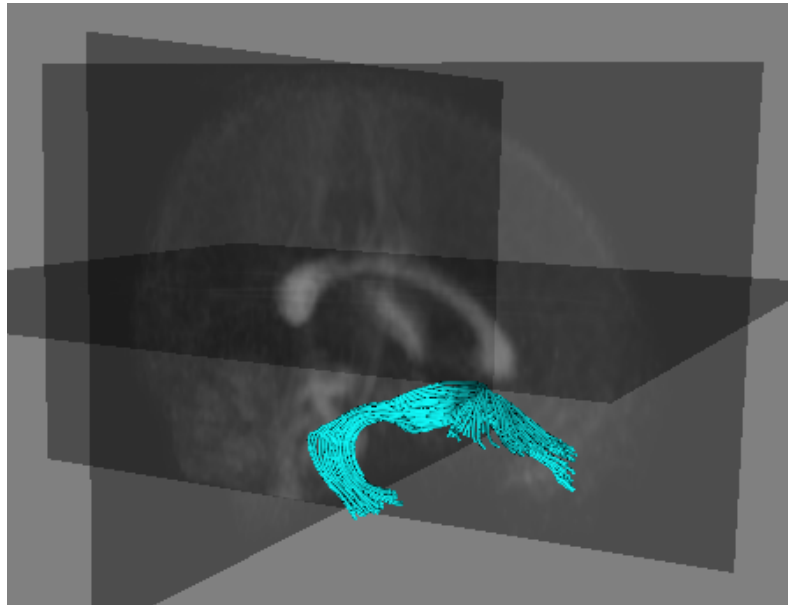


Origin (anatomical landmark)

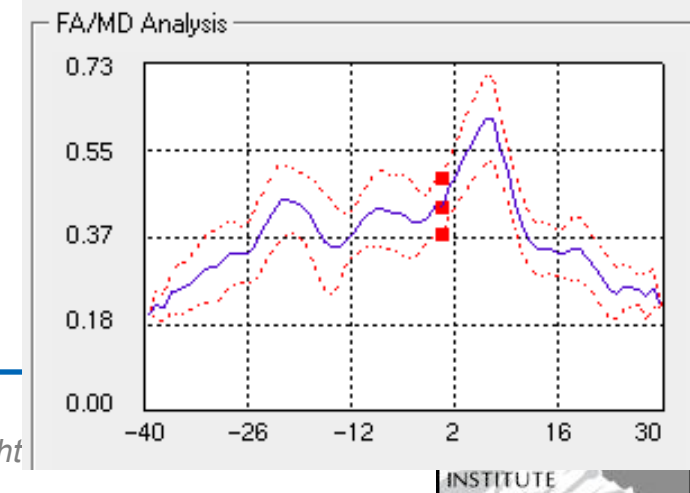




Example Uncinate Fasciculus

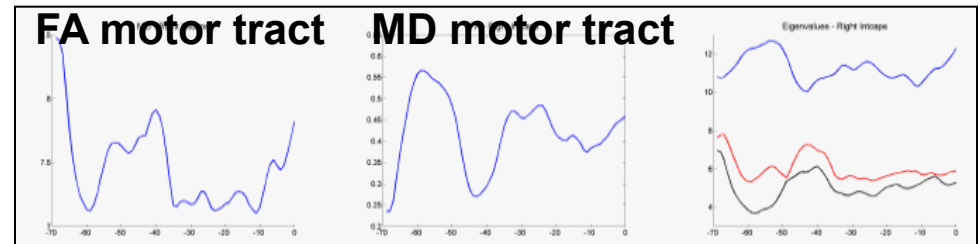
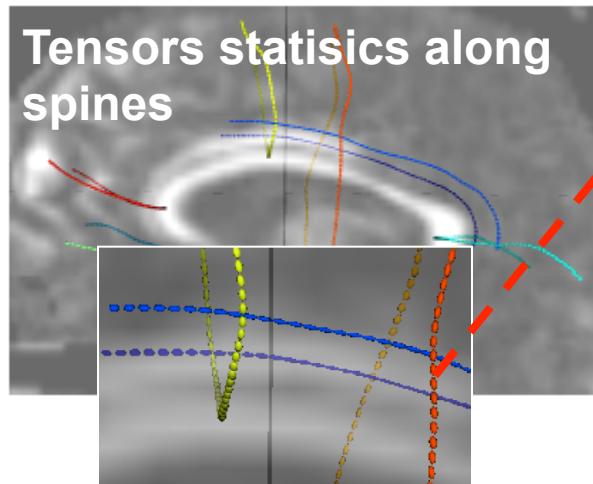
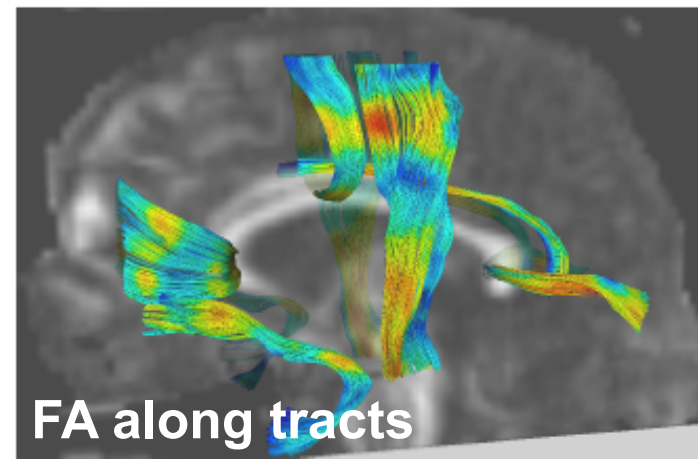
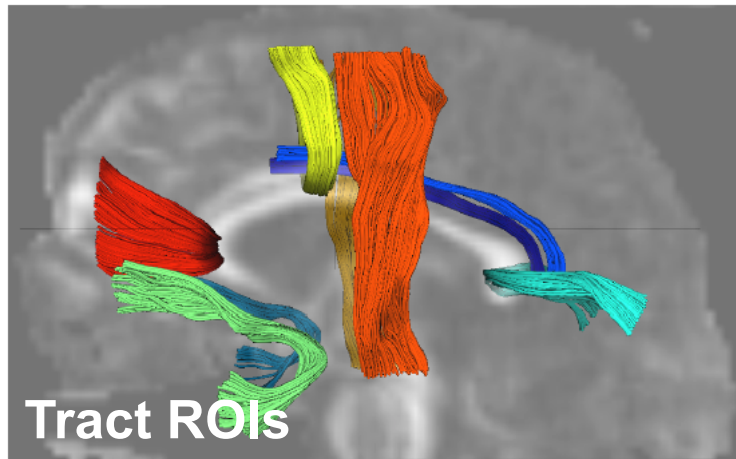


Corouge et al. *Fiber tract-oriented statistics for quantitative diffusion tensor MRI analysis*. Medical Image Analysis 2006.
FiberViewer software - <http://www.ia.unc.edu/dev/>





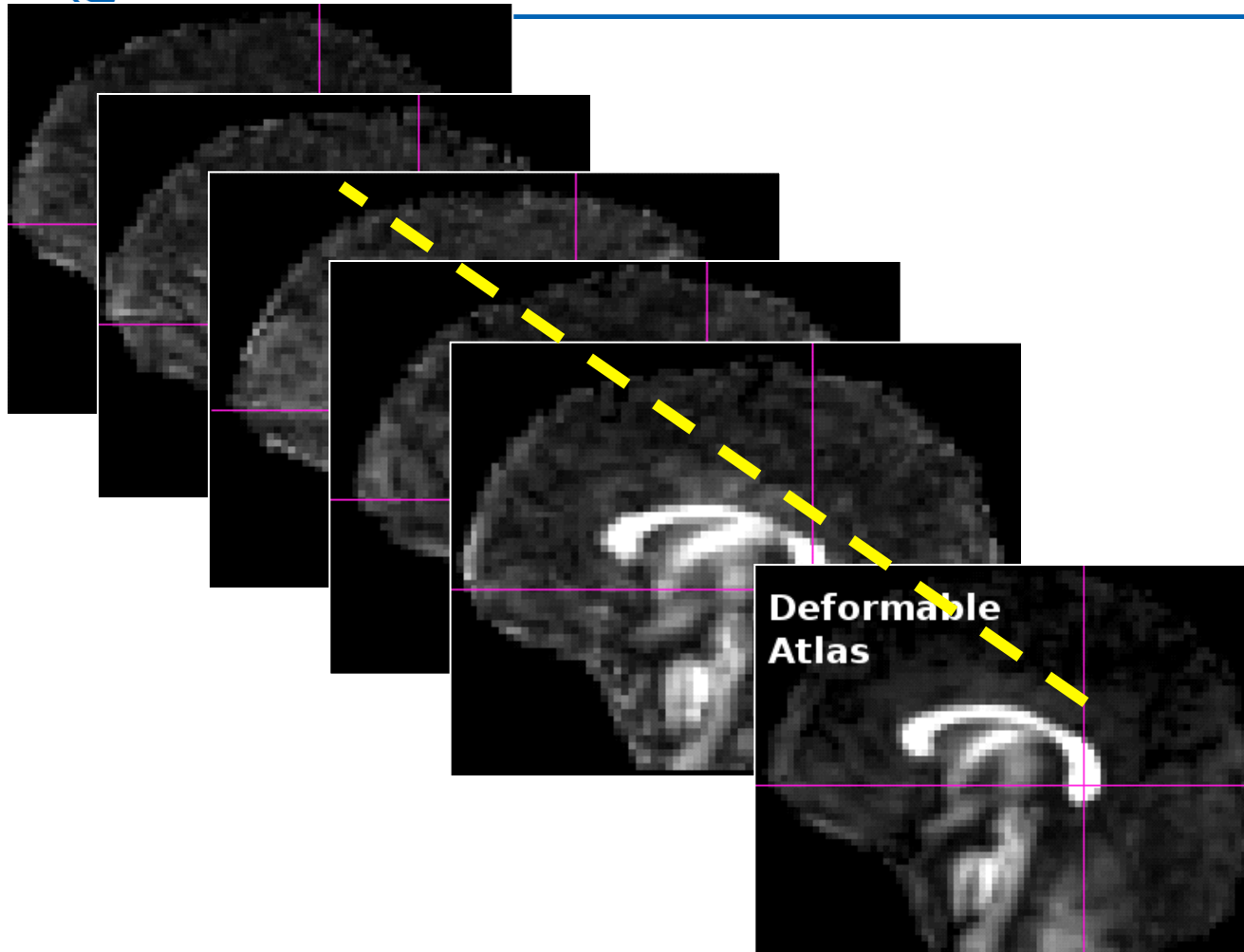
Quantitative Tractography



- Tractography for ROI definition
- Tensor-math. for statistics along tracts

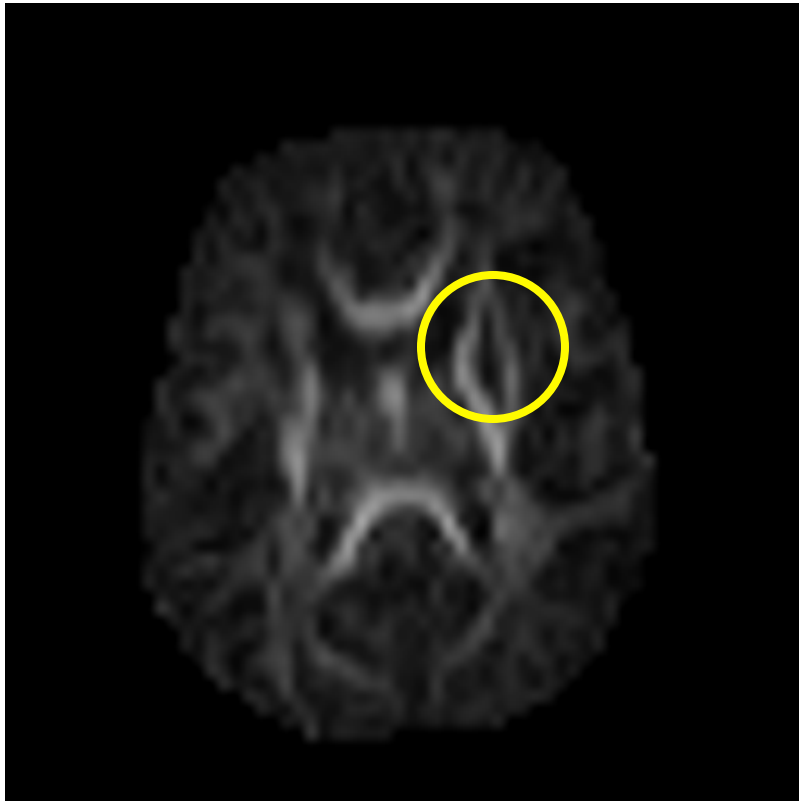


Challenge: Common Coordinate Frame for Population Analysis

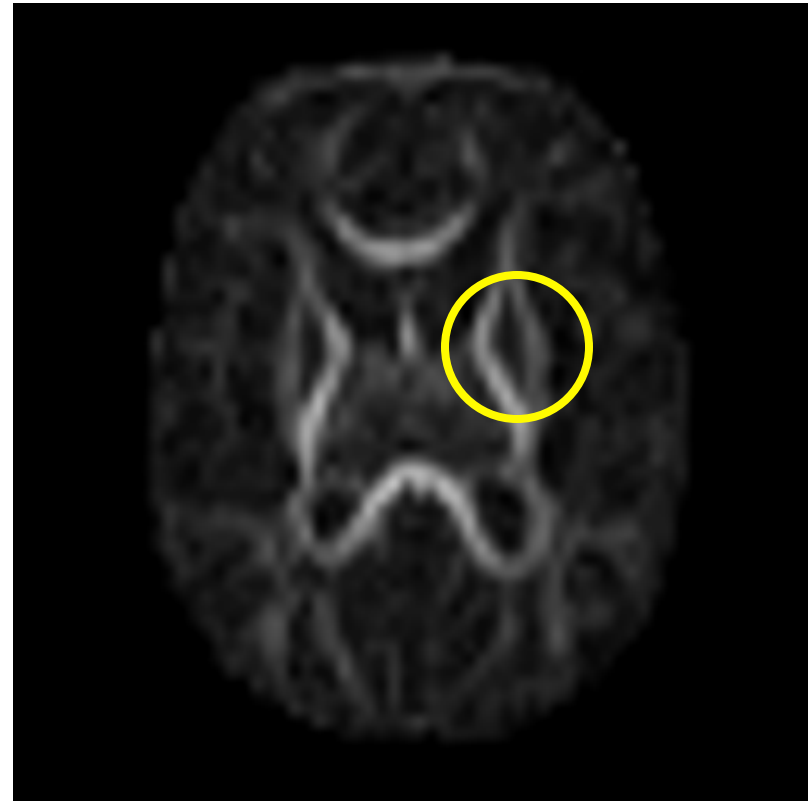




Co-registration of image sets (Neonates)



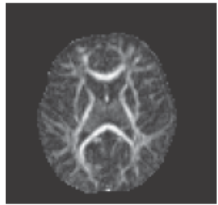
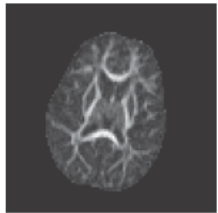
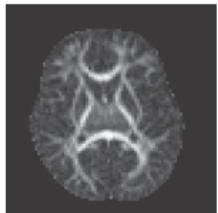
Not registered



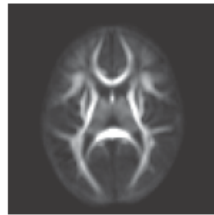
Linear registration (affine)



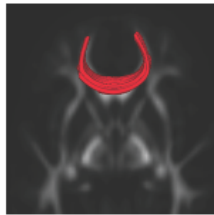
Group statistics of DTI fiber bundles



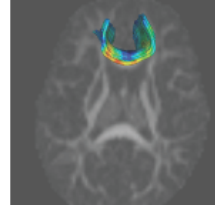
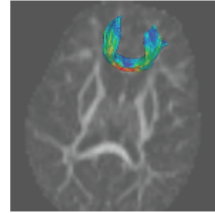
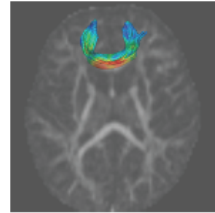
Images



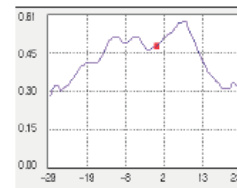
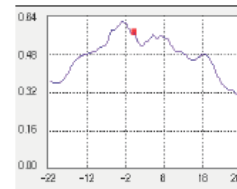
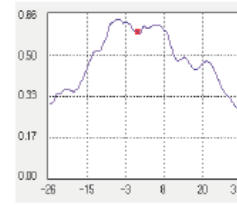
Atlas



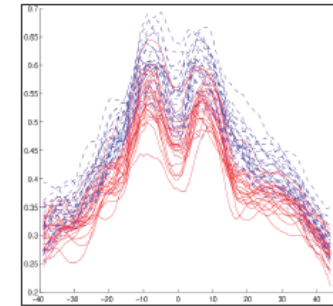
Atlas Tract



Mapped Tracts



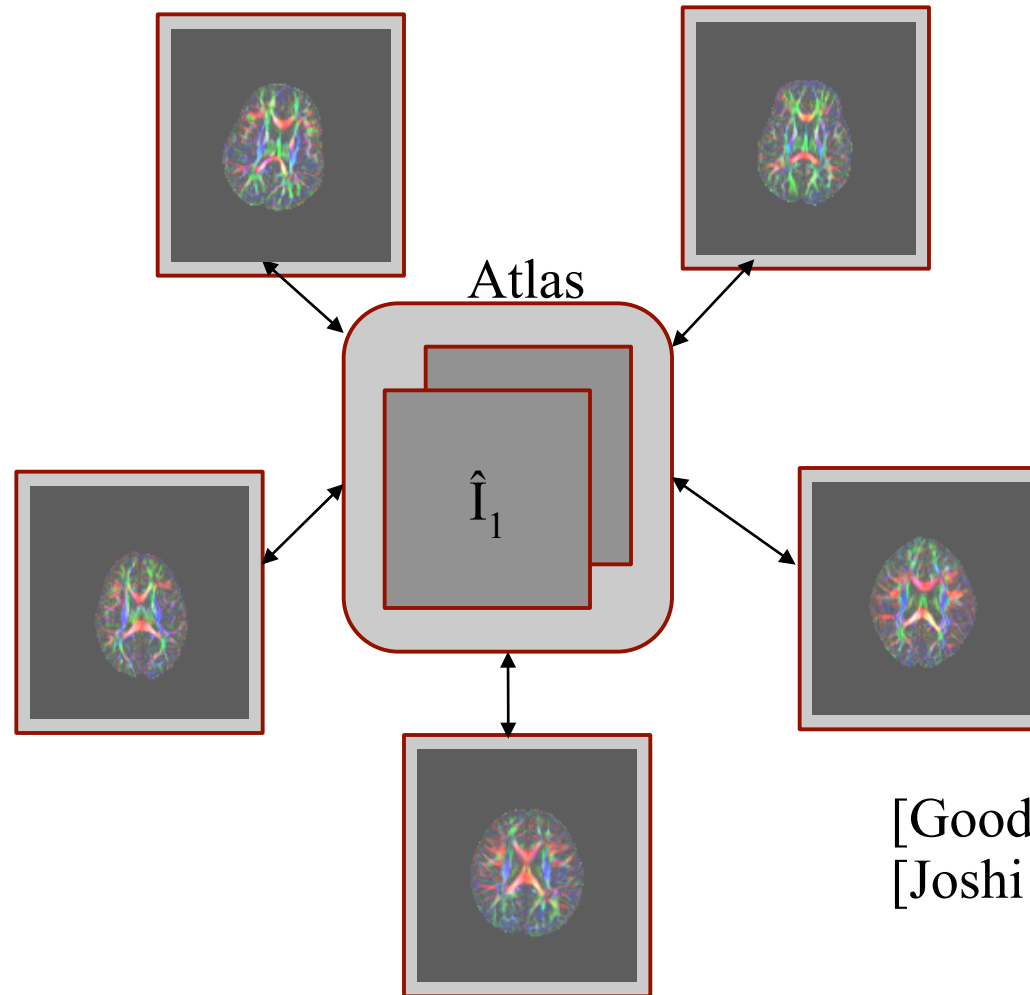
Sampled Functions



Functional Statistics



Atlas Building

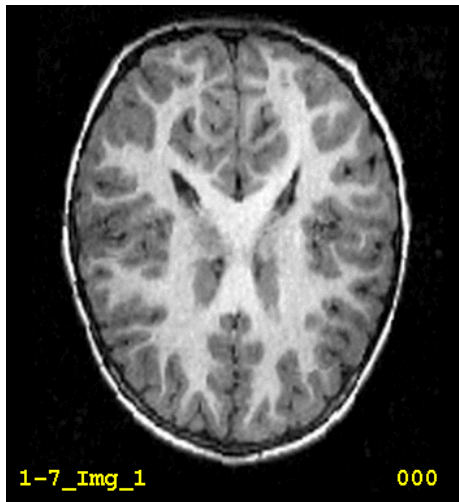


[Goodlett et al 2006]
[Joshi et al 2004]



Unbiased Diffeomorphic Atlas Construction for Computational Anatomy (Joshi, Davis, Lorenzen)

Image 1



Mean

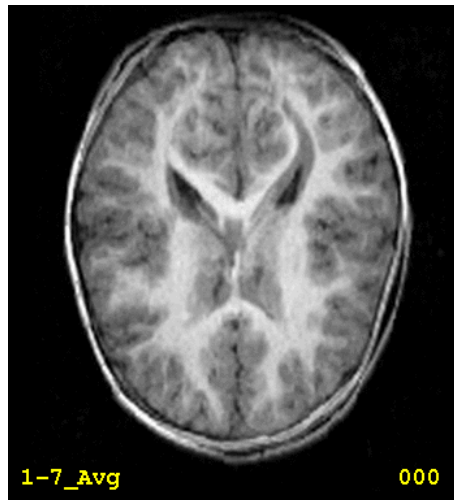
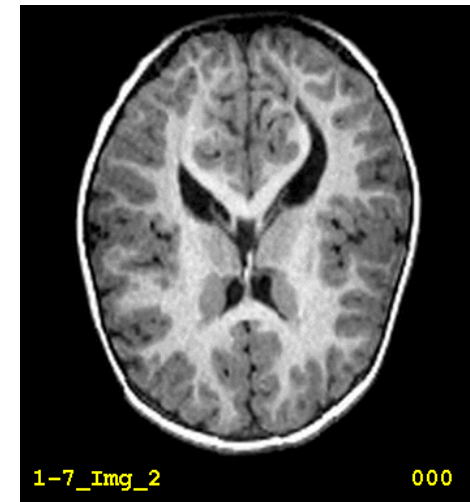
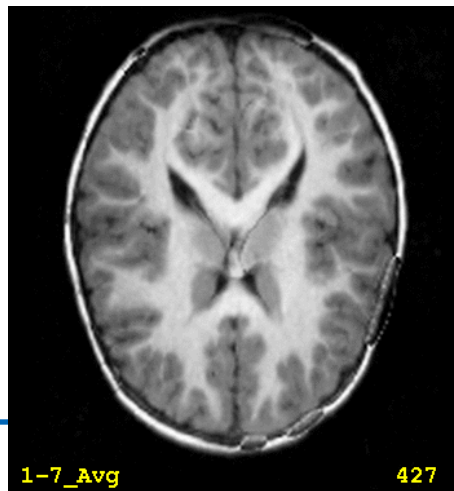


Image 2



Mean by Warping

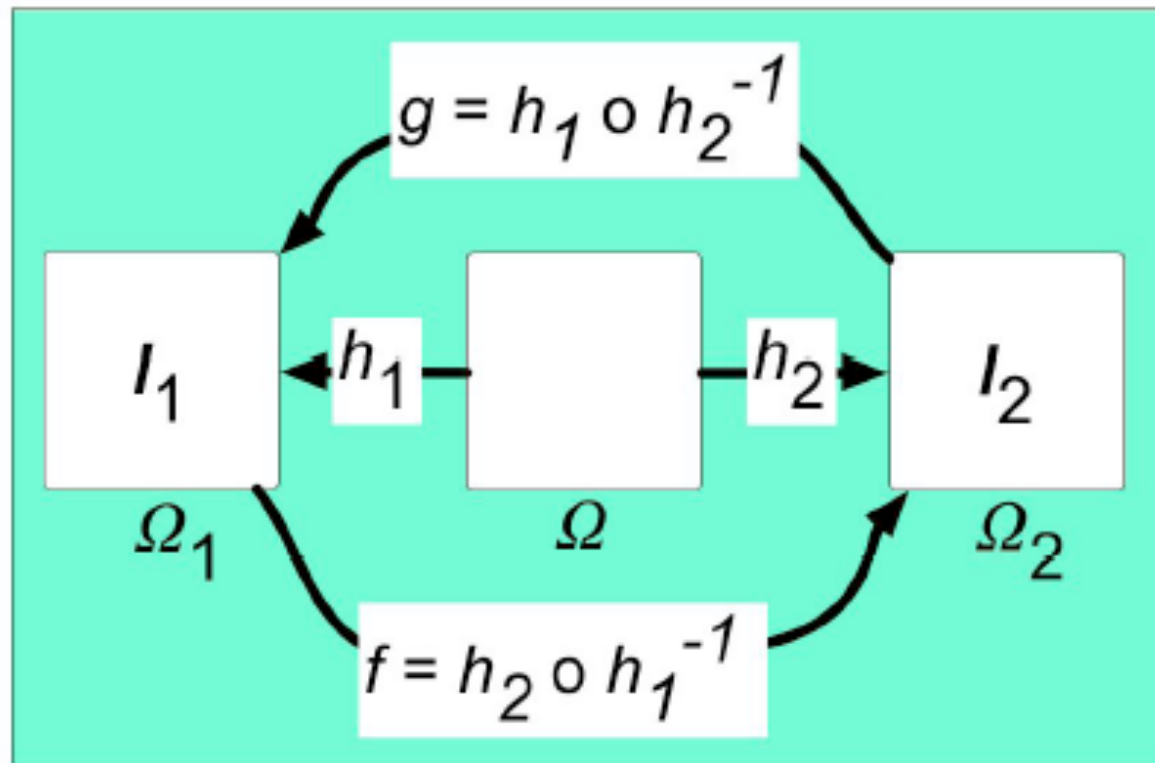


$h_1(x)$

$h_2(x)$



Atlas Formation: Symmetric Registration

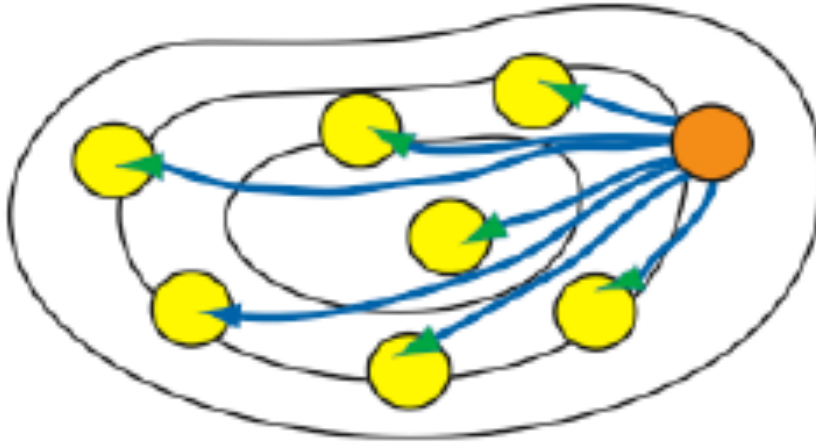


Symmetric Registration Framework

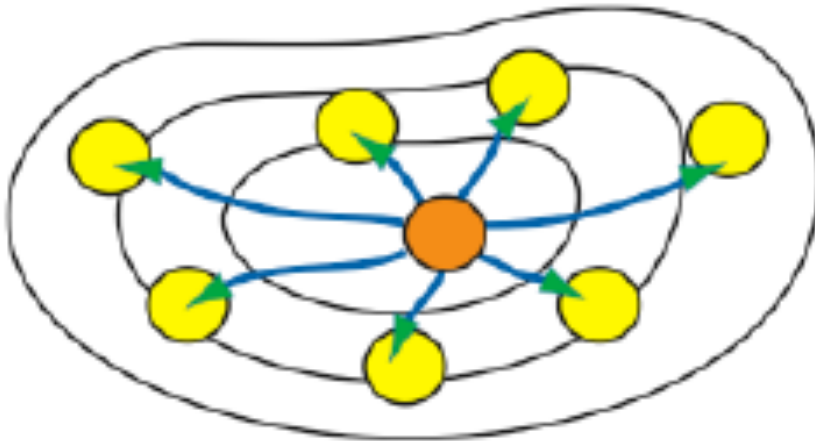
$$f \circ g = h_2 \circ h_1^{-1} \circ h_1 \circ h_2^{-1} = \text{Id}$$



Group-wise Atlas Building



A) Choice of template:
Analysis is biased by choice
of template.



B) Unbiased atlas building:
Minimize total distance
between population and
template
(Gee & Avants,
Joshi&Fletcher)



Averaging Anatomies'

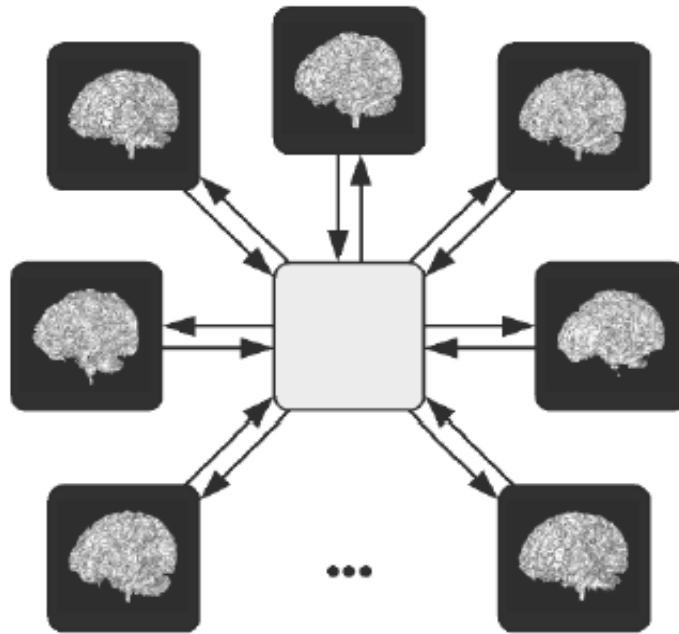


Figure 1. Template Construction Framework

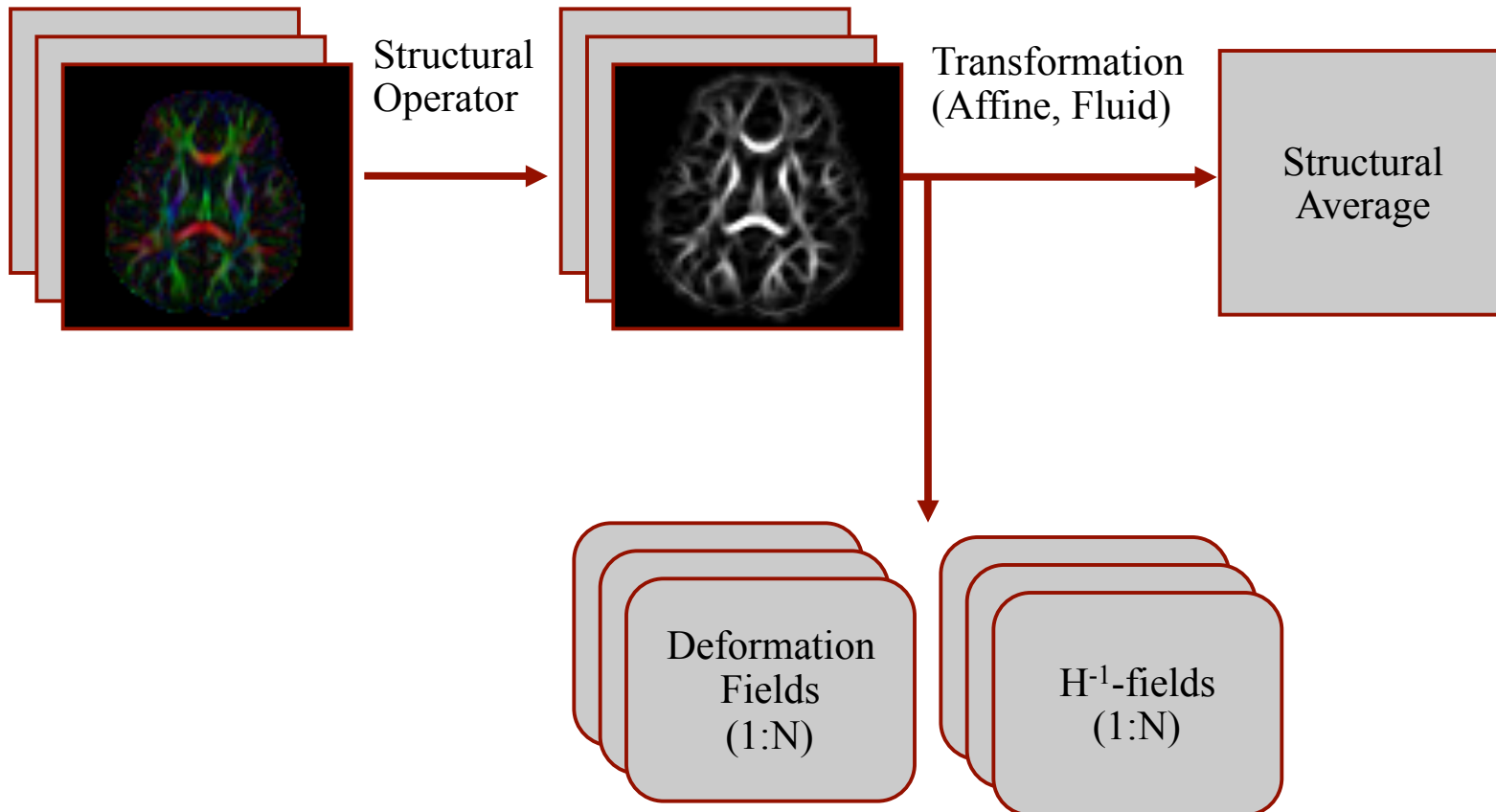
Motivation:

- Map population into common coordinate space
- Learn about normal variability
- Describe difference from normal
- Use as normative atlas for segmentation

Sarang Joshi, Brad Davis, Matthieu Jomier, Guido Gerig, Unbiased Diffeomorphic Atlas Construction for Computational Anatomy, vol. 23, NeuroImage 2004

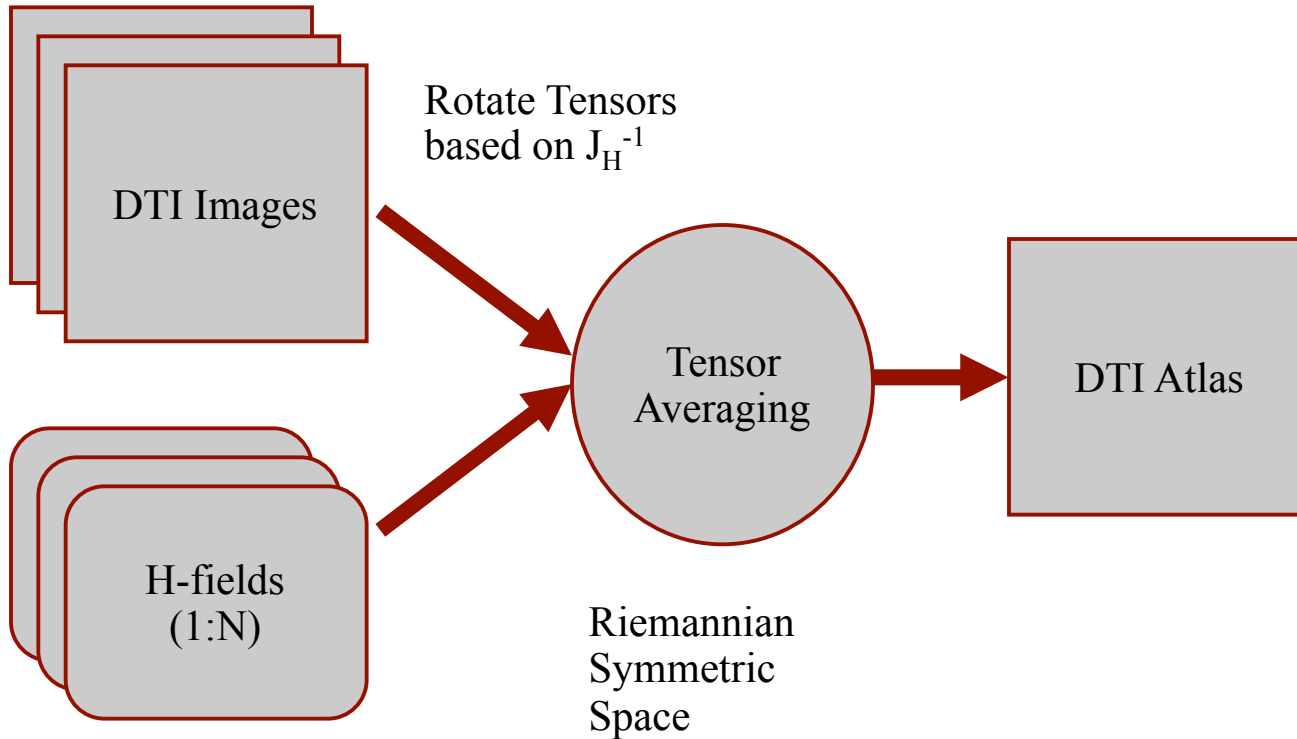


DTI: Estimation of coordinate transformations



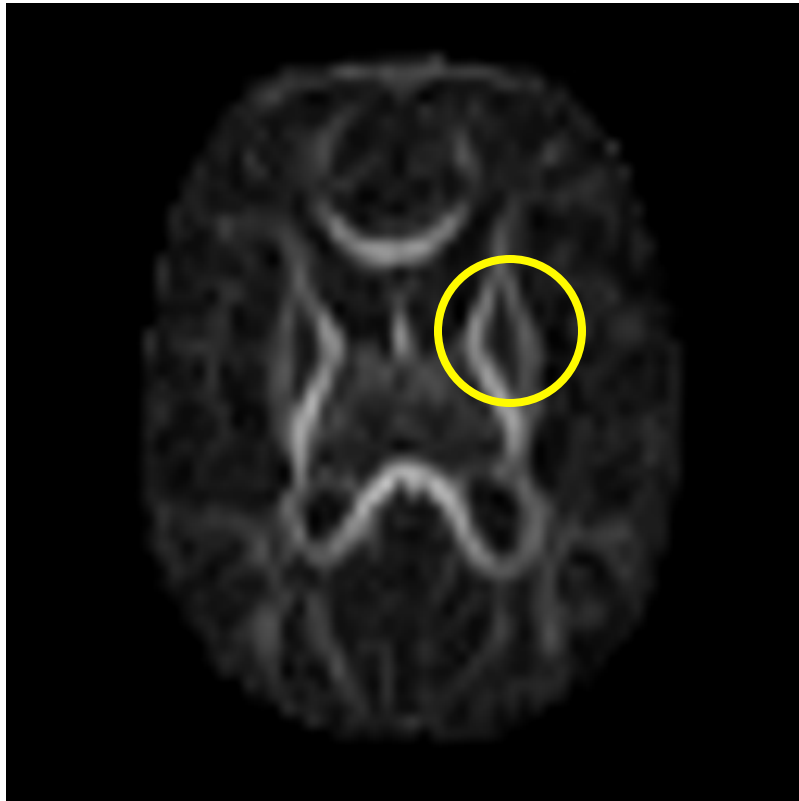


Computation of tensor means

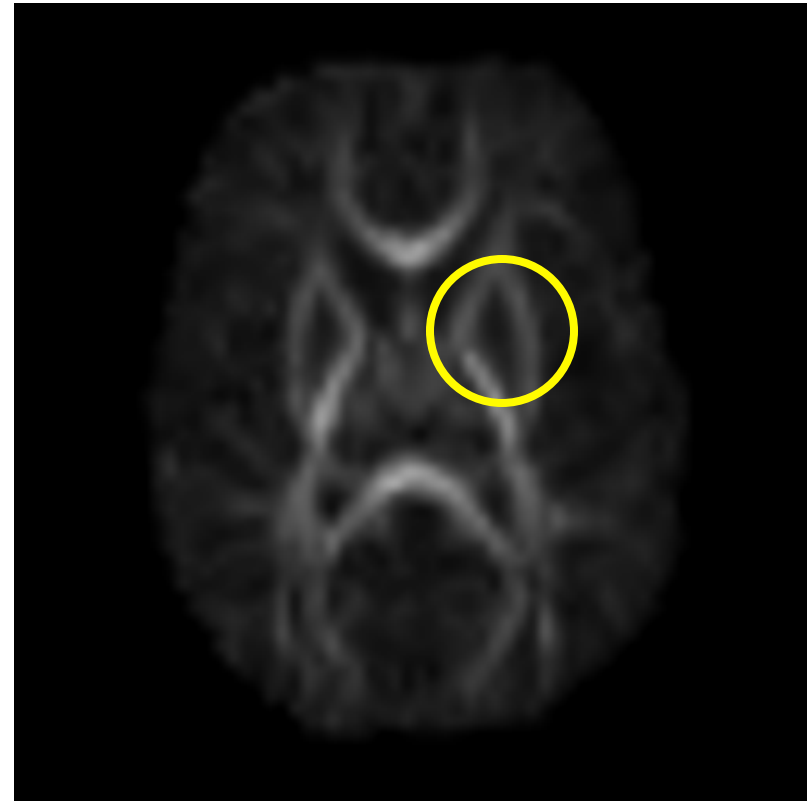




Co-registration: From linear to nonlinear



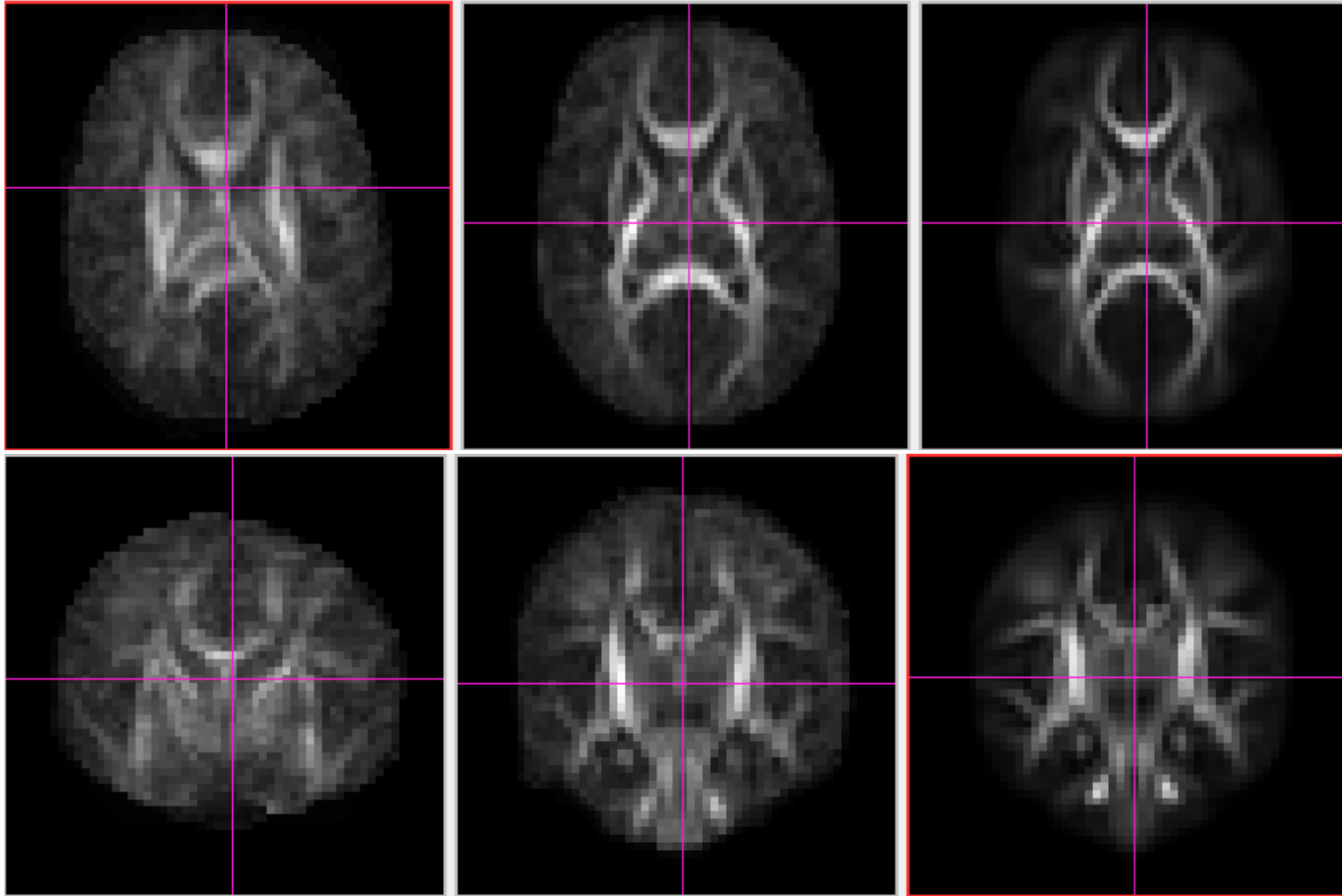
Linear registration (affine)



Nonlinear registration (fluid)

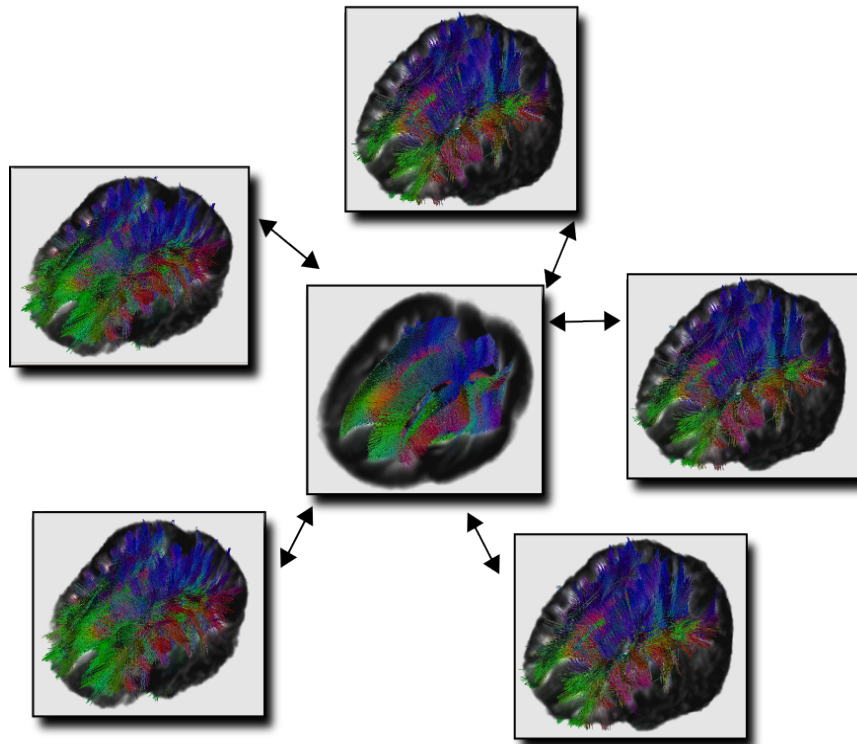


Atlas Building





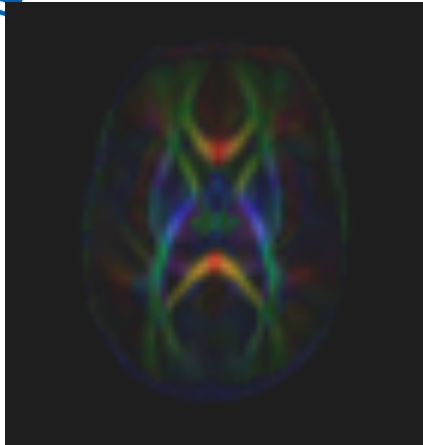
Population Coordinates: DTI Atlas Building



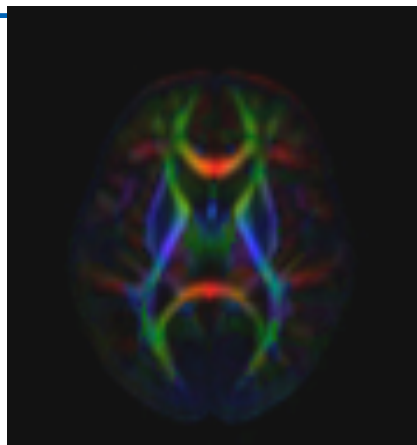
- Balci, Golland, Wells. *Non-rigid Groupwise Registration using B-Spline Deformation Model*. ITK Workshop 2007.
 - Available in sandbox
MultiImageRegistration
- Goodlett et al. *Improved correspondence for DTI population studies via unbiased atlas building*. MICCAI 2006, Neuroimage 2009.
 - Tensor processing tools –
DTIprocess (NeuroLib),
Teem, Slicer 3



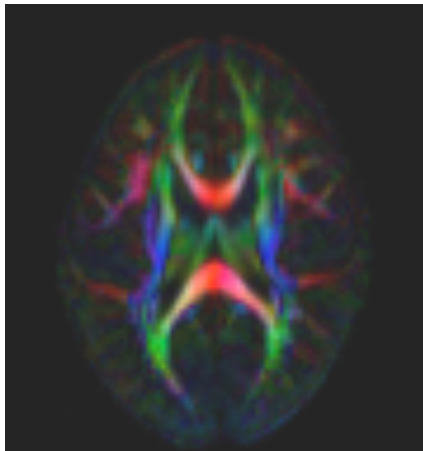
Application: Neurodevelopmental Statistical Atlases



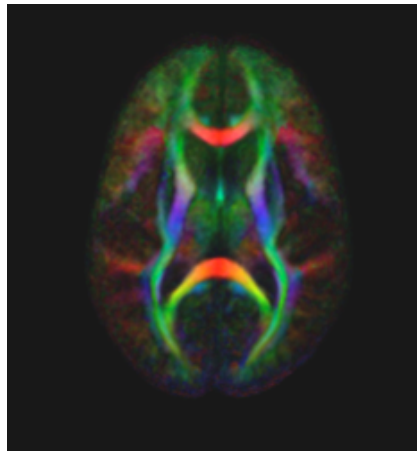
Neonate (N=95)



1 year (N=25)



2 year (N=25)



Adult (N=24)

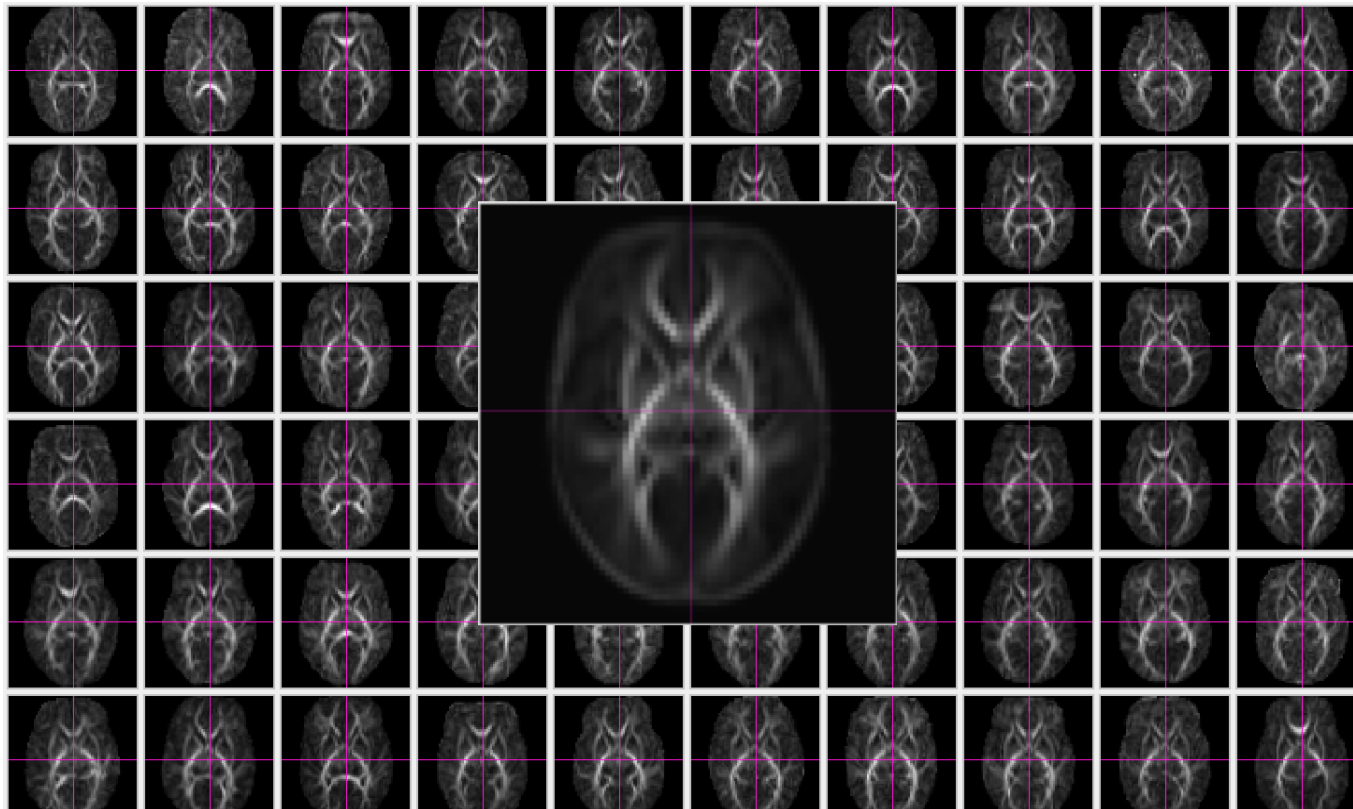


Collaborative research on studying the early developing brain with John H. Gilmore and Weili Lin, UNC Chapel Hill



Population-based analysis of fiber tracts

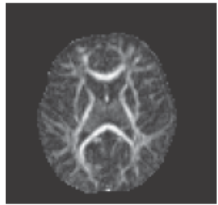
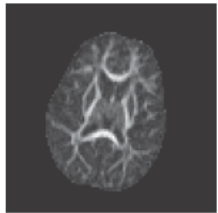
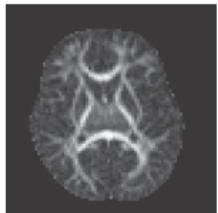
Example: 150 neonate DTI mapped to unbiased atlas



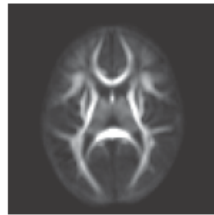
Goodlett,
Joshi,
Gouttard,
Gerig,
(MICCAI' 06,
MICCAI' 08,
NeuroImage
' 09)



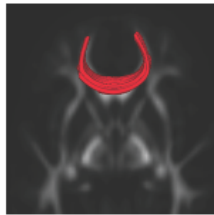
Group statistics of DTI fiber bundles



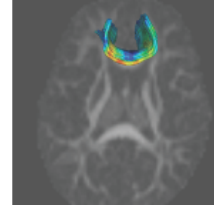
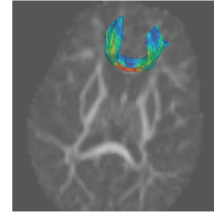
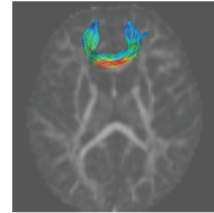
Images



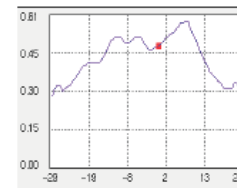
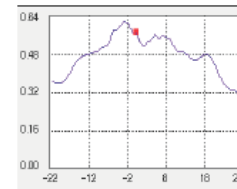
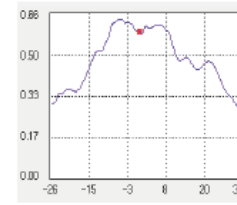
Atlas



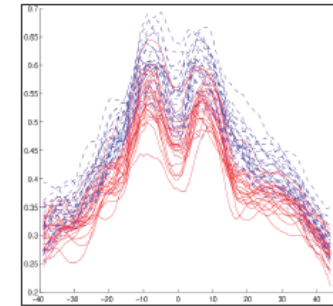
Atlas Tract



Mapped Tracts



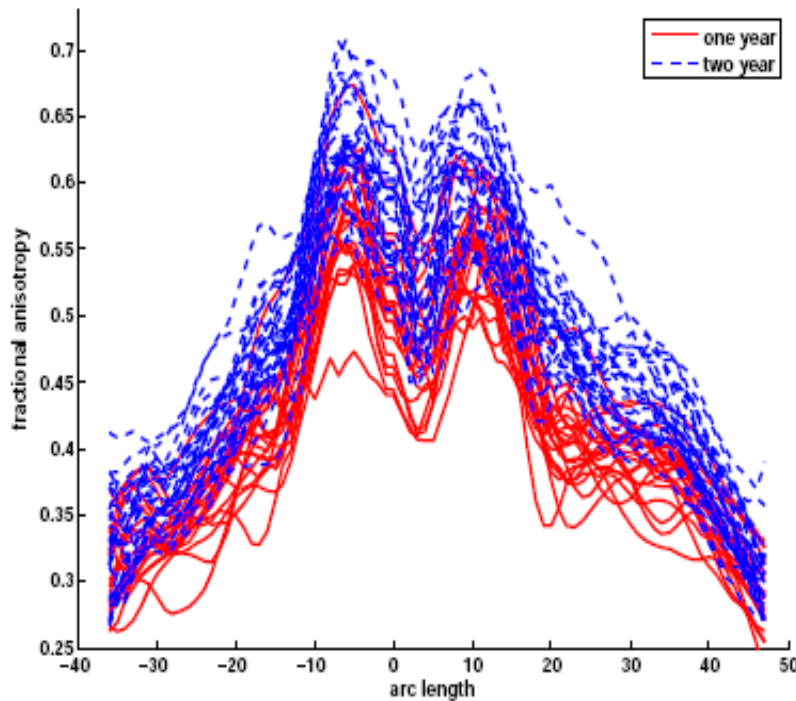
Sampled Functions



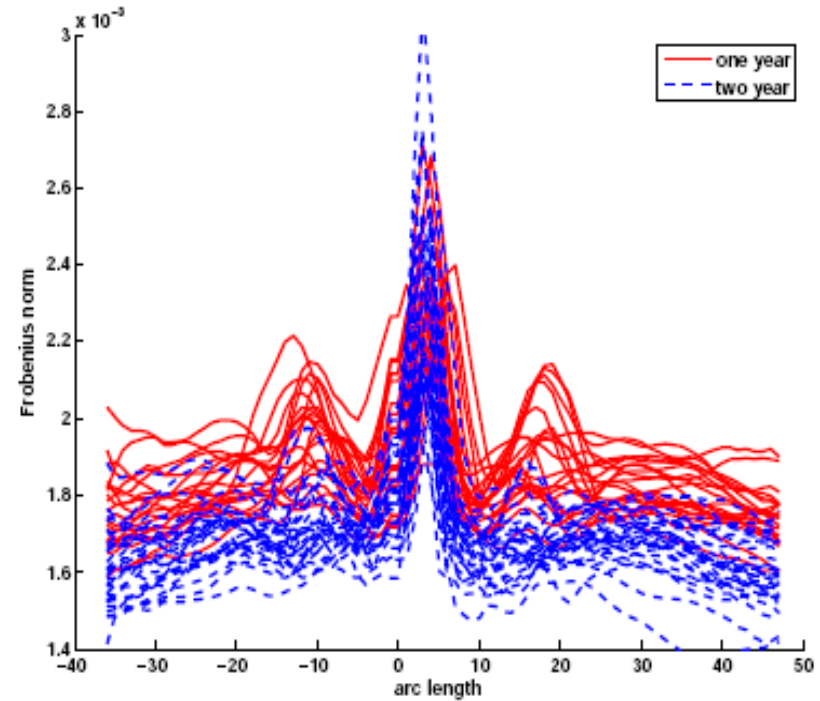
Functional Statistics



Splenium track, 1yr to 2yr infants



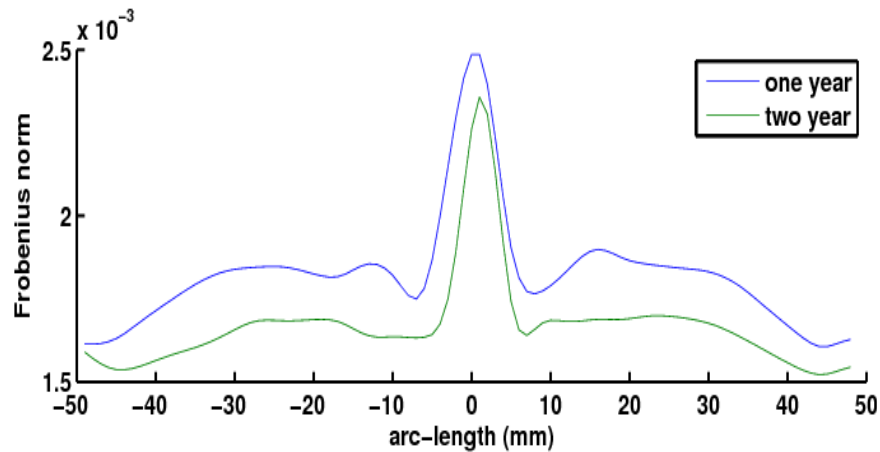
(b) All FA curves



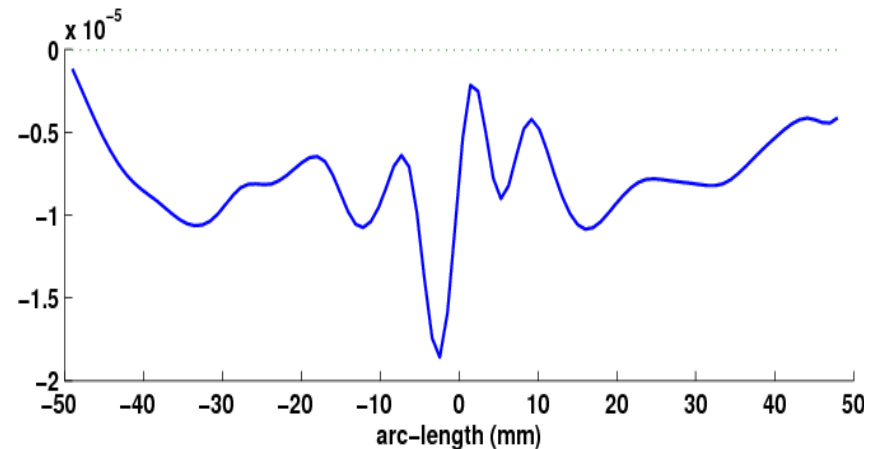
(c) All norm curves



Development from 1 to 2 years – Genu Discrimination of Norm



Group Means

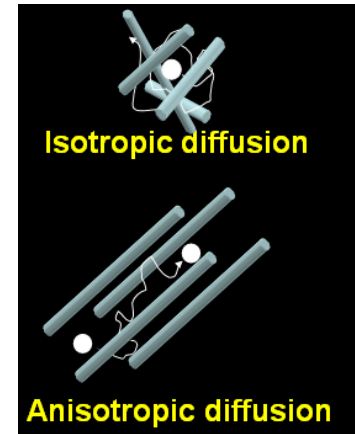
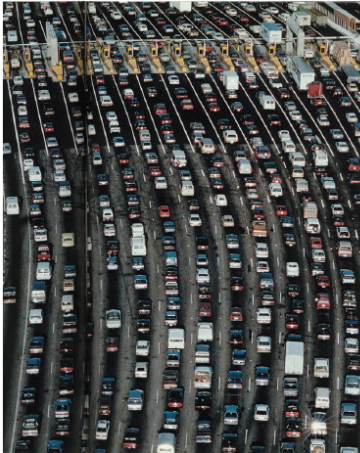


Discriminant

Goodlett et al., Neuroimage 2009



Summary: What do we measure?



- DWI measures local diffusivity pattern.
- Local diffusivity pattern is shaped by tissue type, axon structuring, myelination etc.
- Curves and streamlines from tractography are NOT AXONS but possible paths in vector/tensor field.
- “Fiber counting” is scientifically questionable, # is method specific.
- **DWI DOESN’ T MEASURE AXONS or GLOBAL CONNECTIVITY !**

